

# Exploiting macauff cross-matches with two new Rubin software packages: birnam and banquo

Tom J Wilson (he/him) and Tim Naylor  
with the LSST:UK DAC team  
t.j.wilson@exeter.ac.uk  
University of Exeter

LSST@Europe6 – In-Kind Contributions, 17/Sep/24

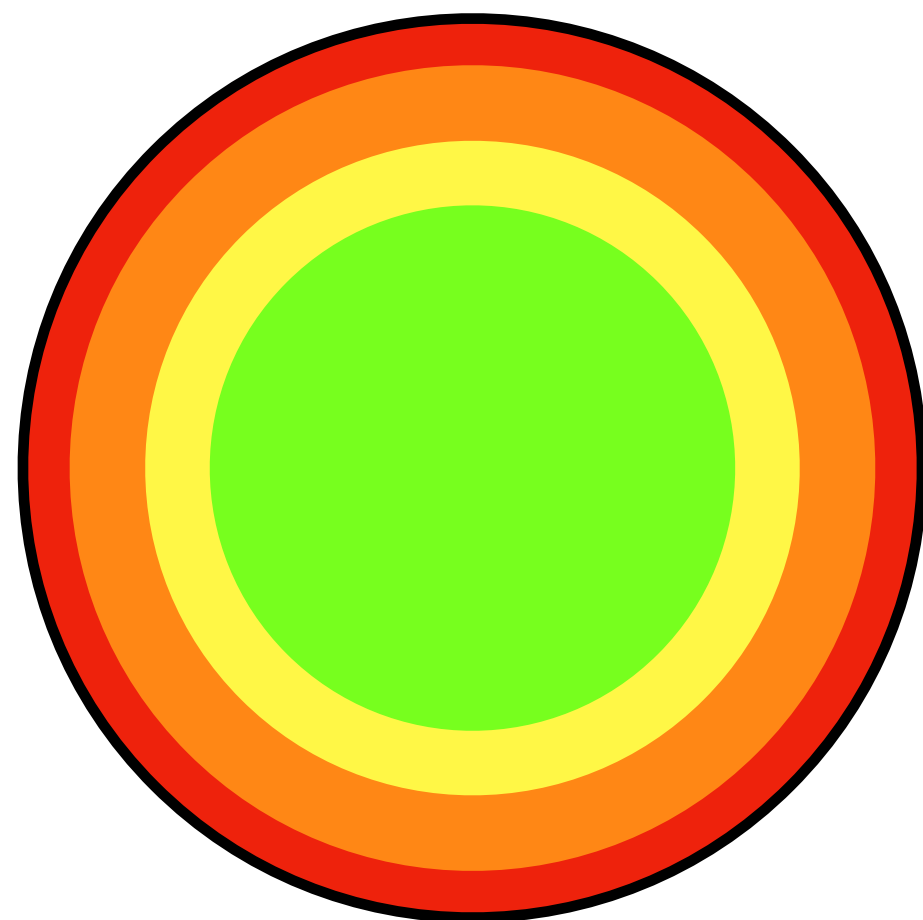


 [@Onoddil](#) [@pm.me](mailto:tom@onoddil.pm.me)   
[.github.io](https://github.com/Onoddil) 

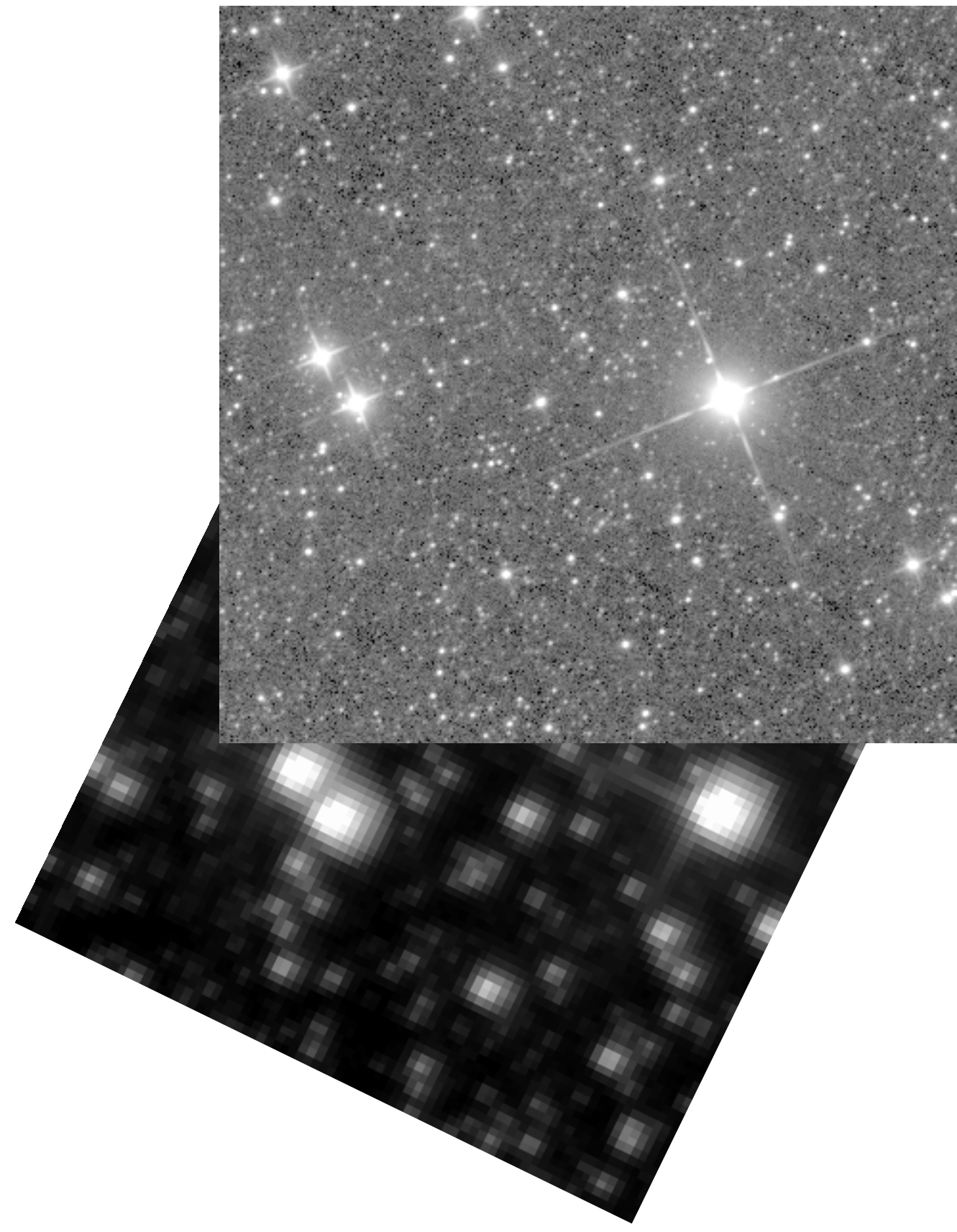
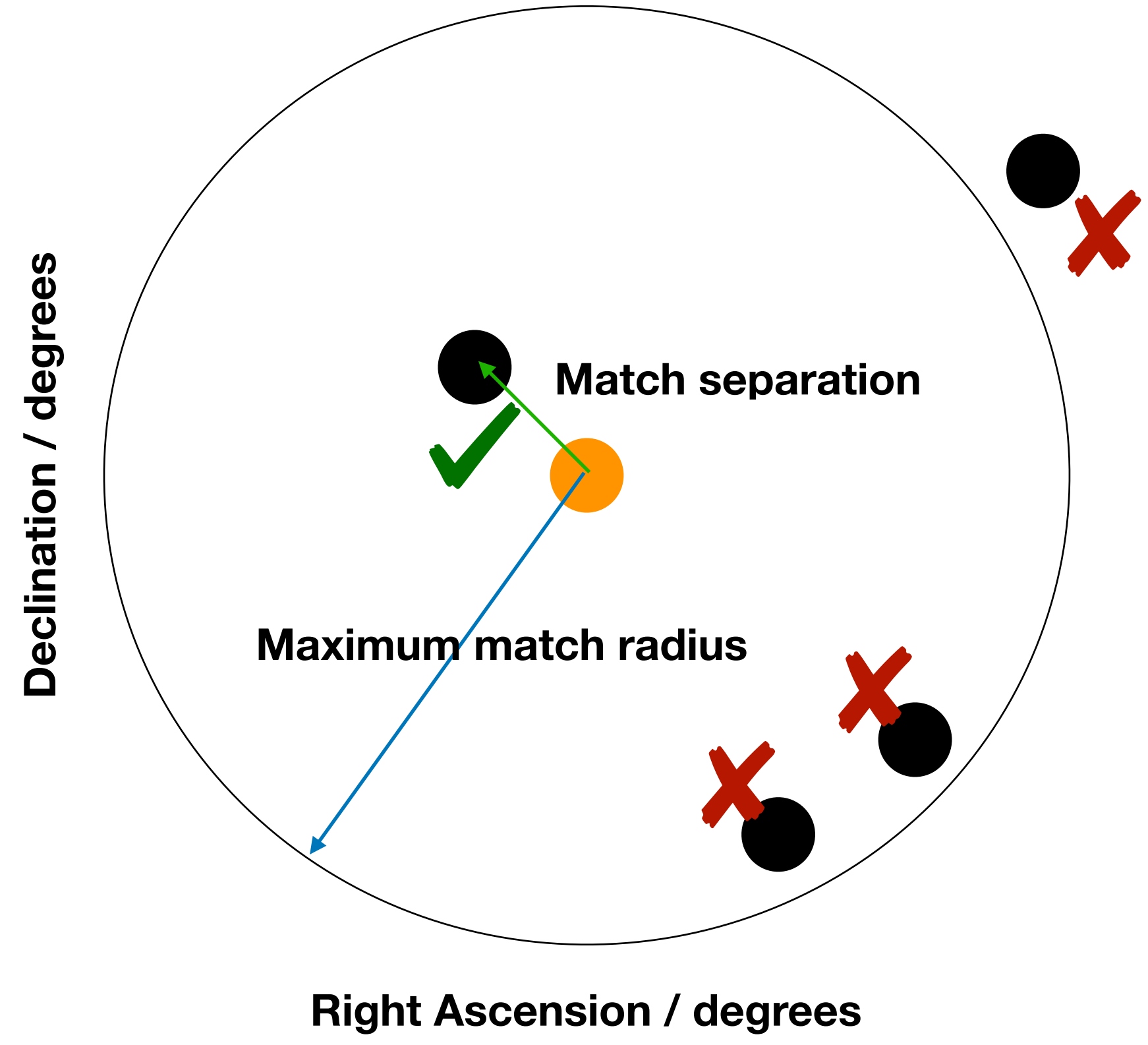
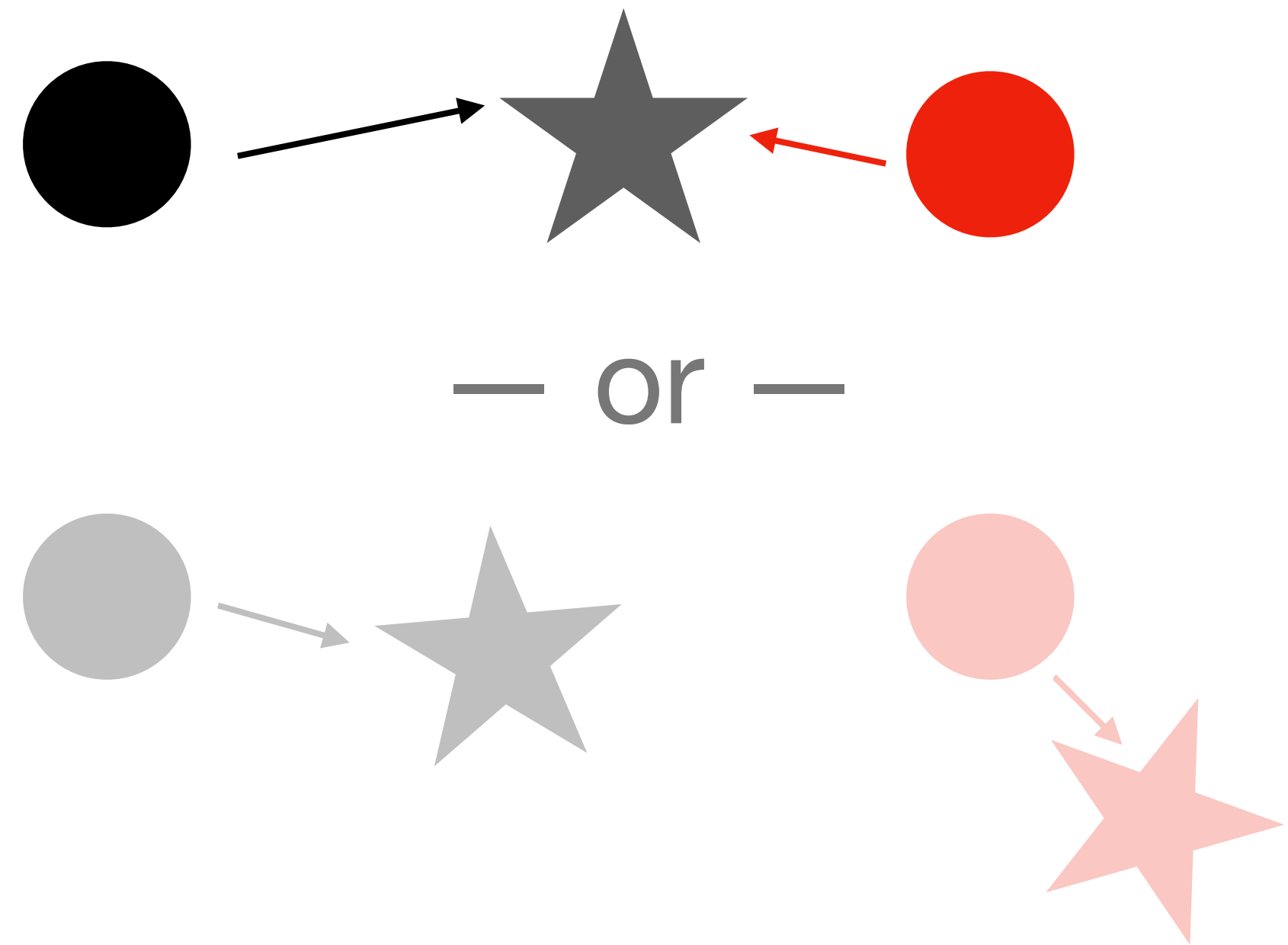


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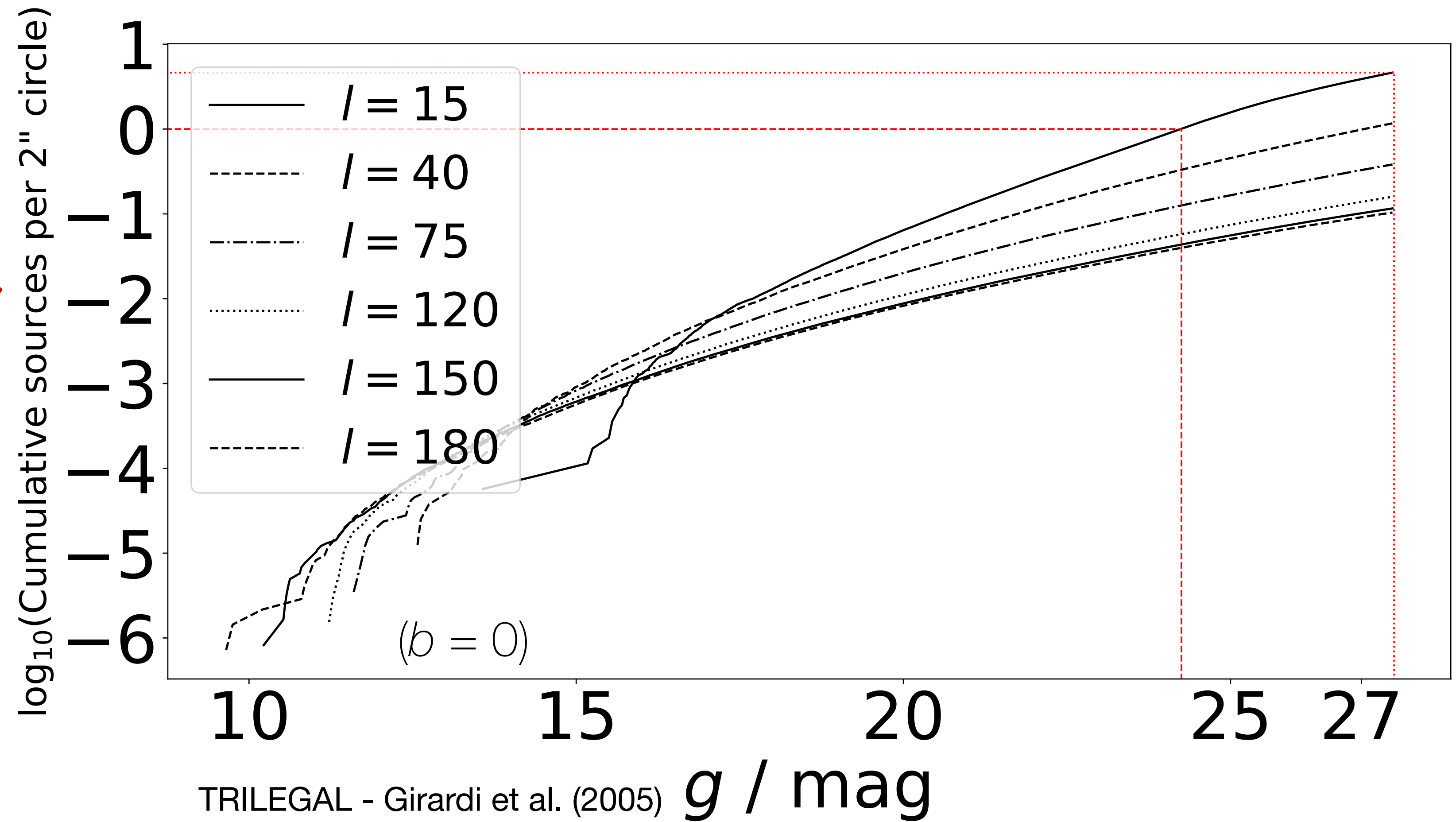
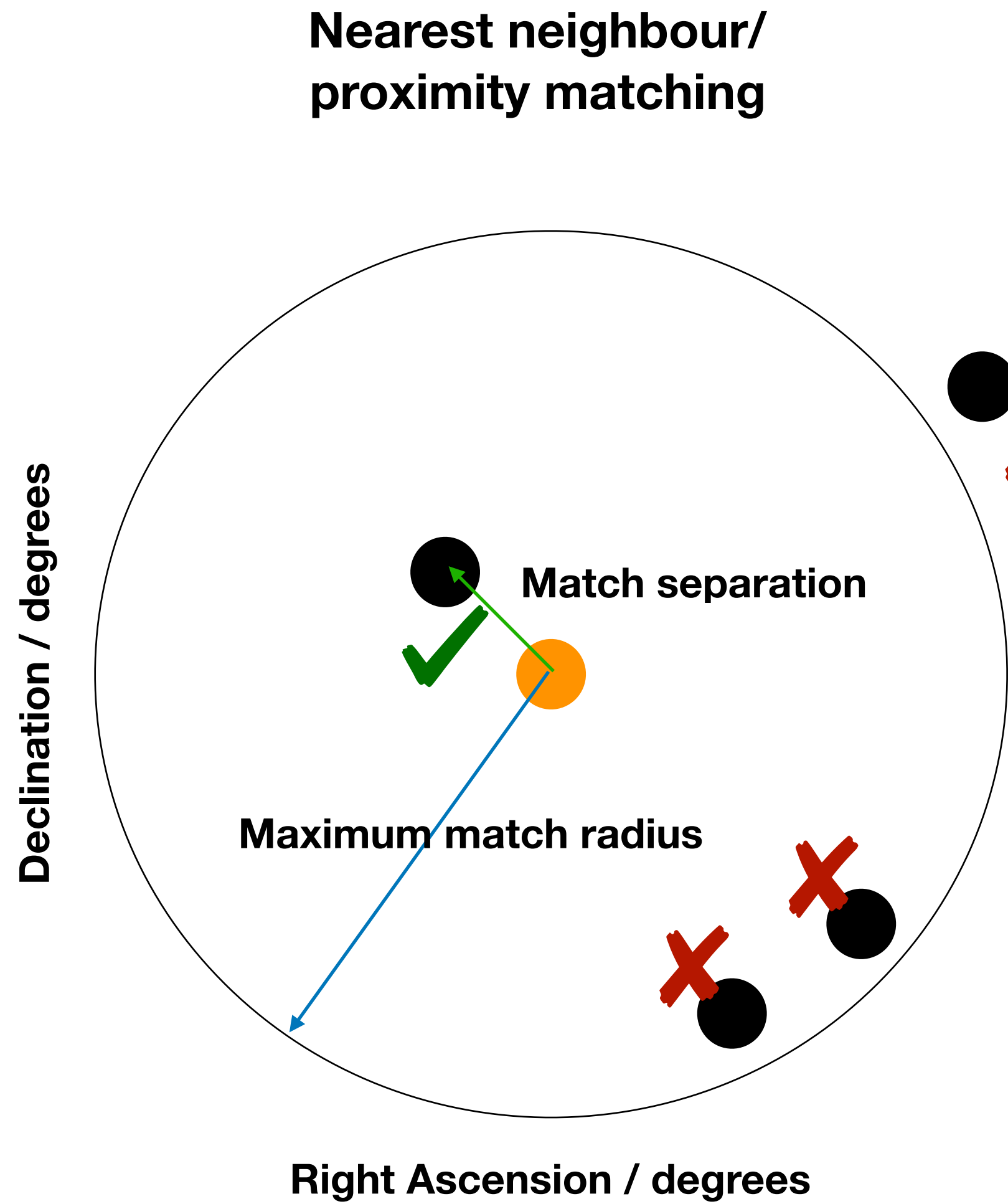
# Cross-Match Science, Methodology, Background



# “Simple” Cross-Matching



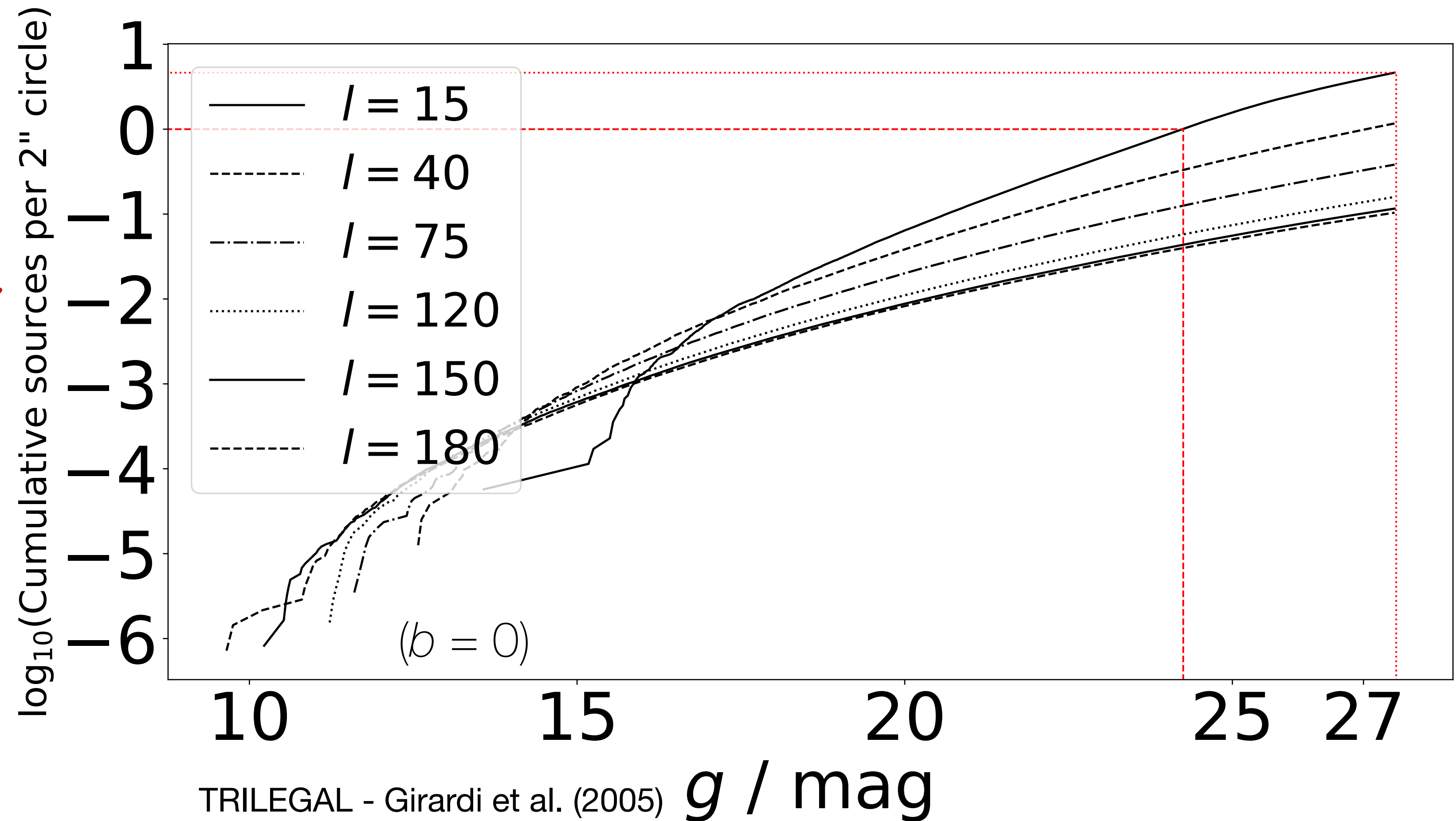
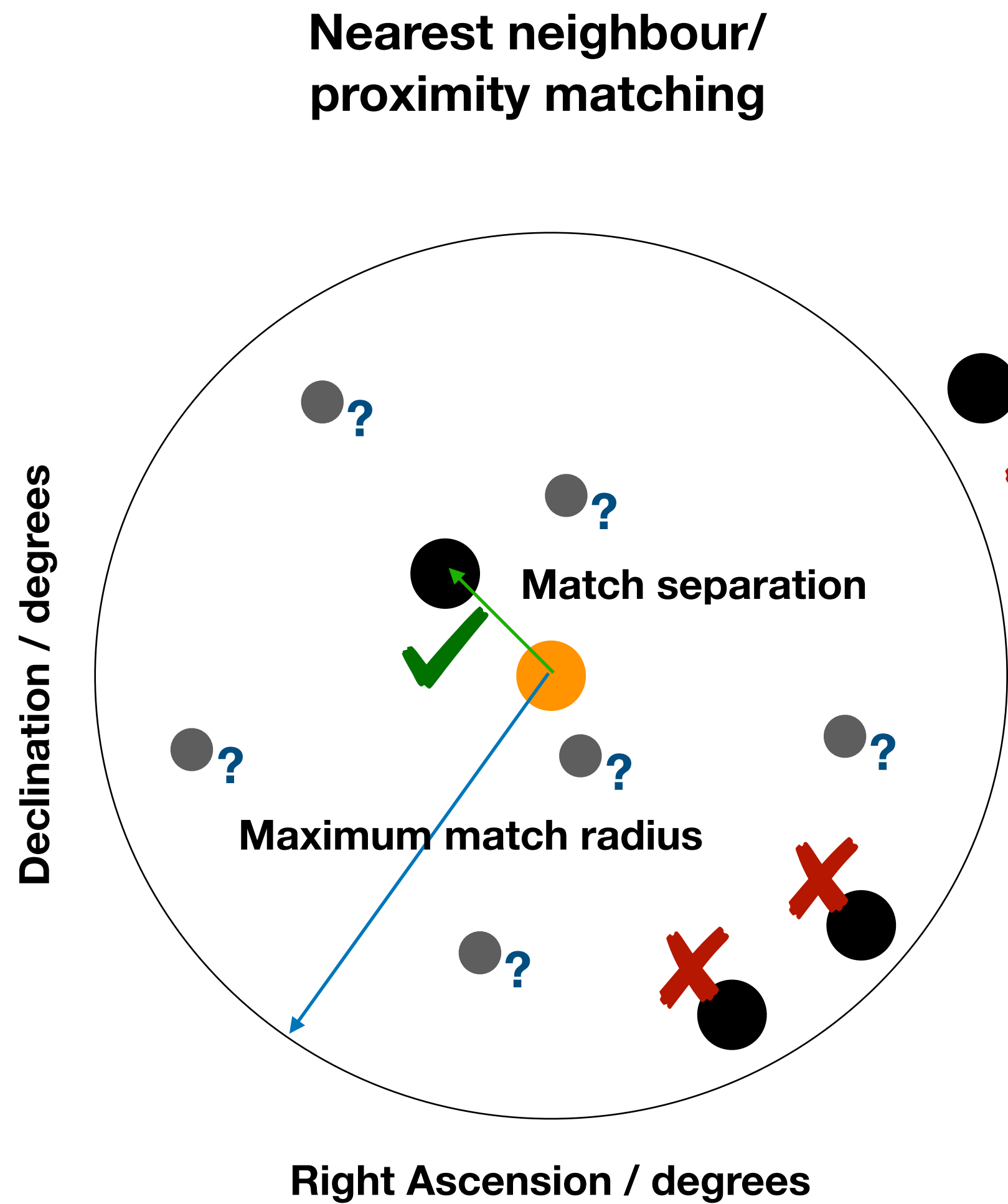
# The Problem With LSST





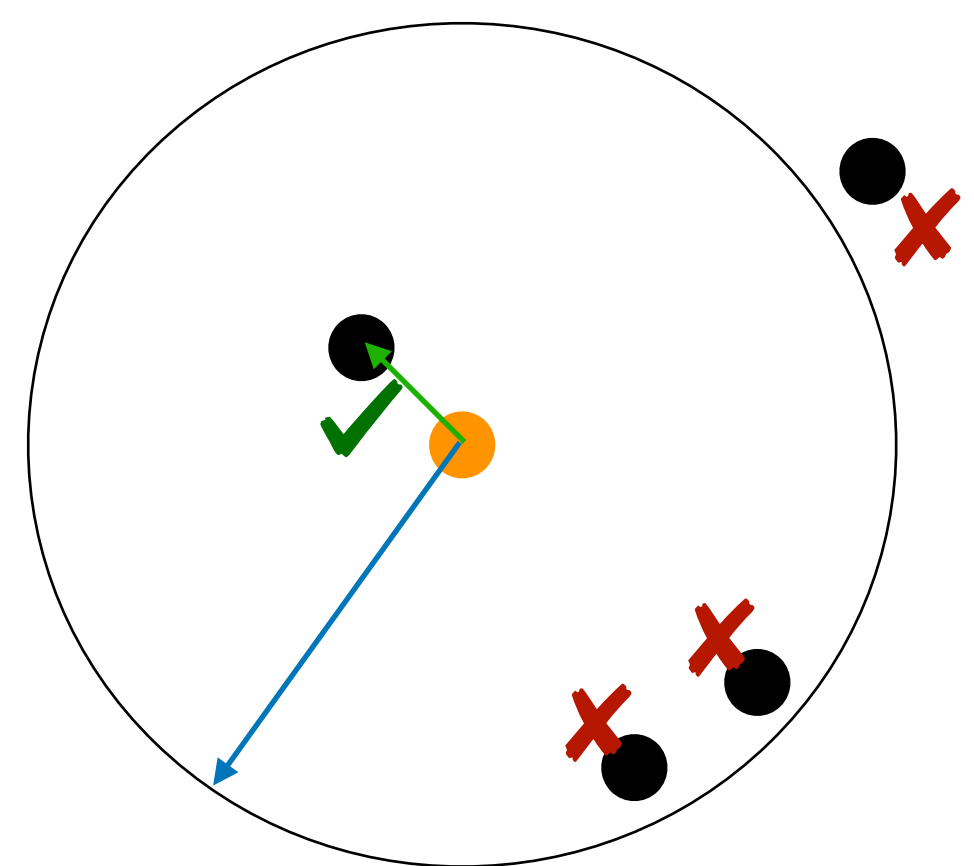
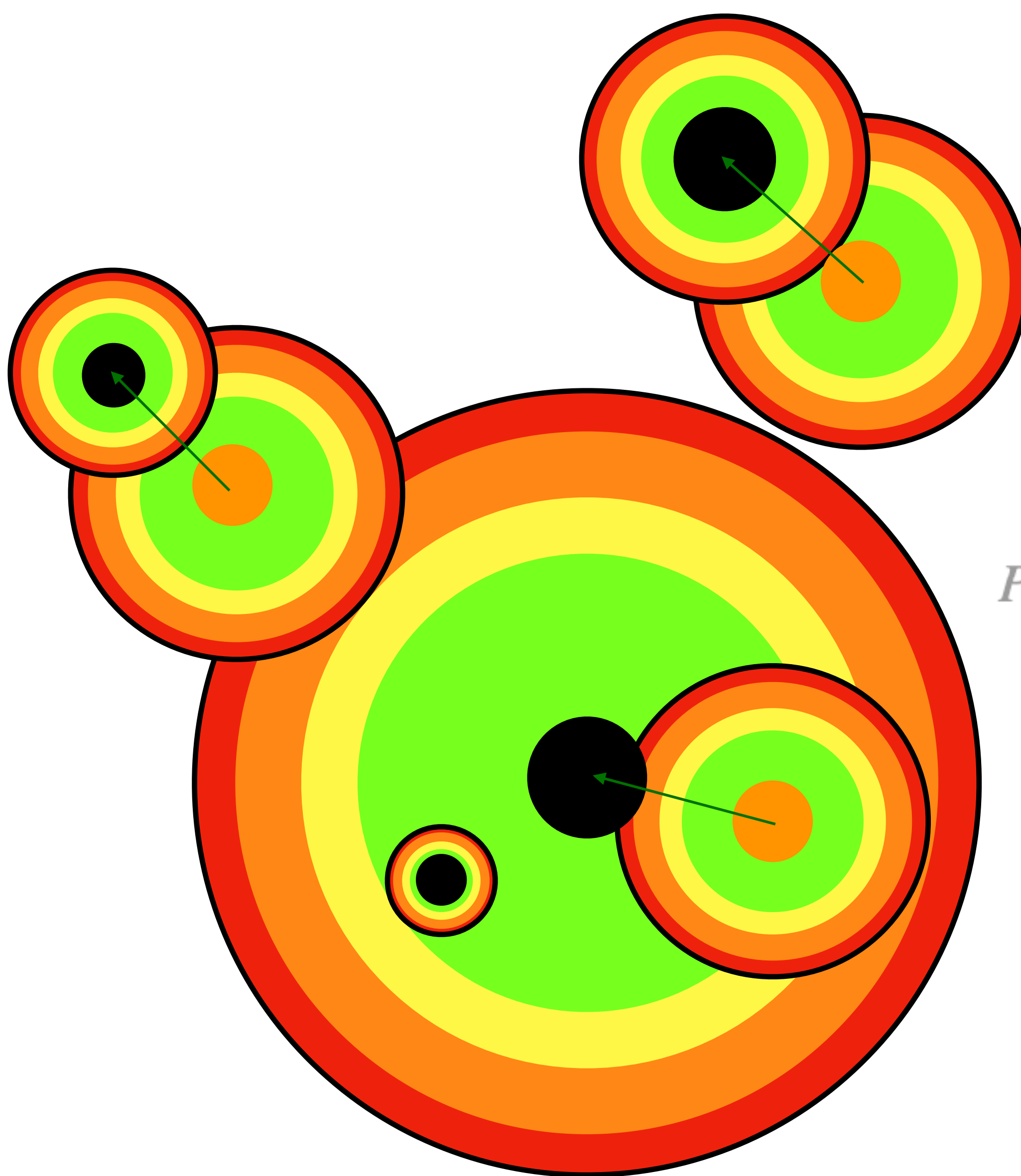
# The Problem With LSST

(It's still a few randomly placed objects in every match radius at high Galactic latitudes)



**Nearest-neighbour matching *will not* work in the era of Rubin!**

# Probabilistic Cross-Matching



Probability of two sources having their on-sky separation given the hypothesis they are counterparts

$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \delta \in \gamma} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \omega \in \phi} N_\phi f_\phi^\omega \prod_{i=1}^k N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$

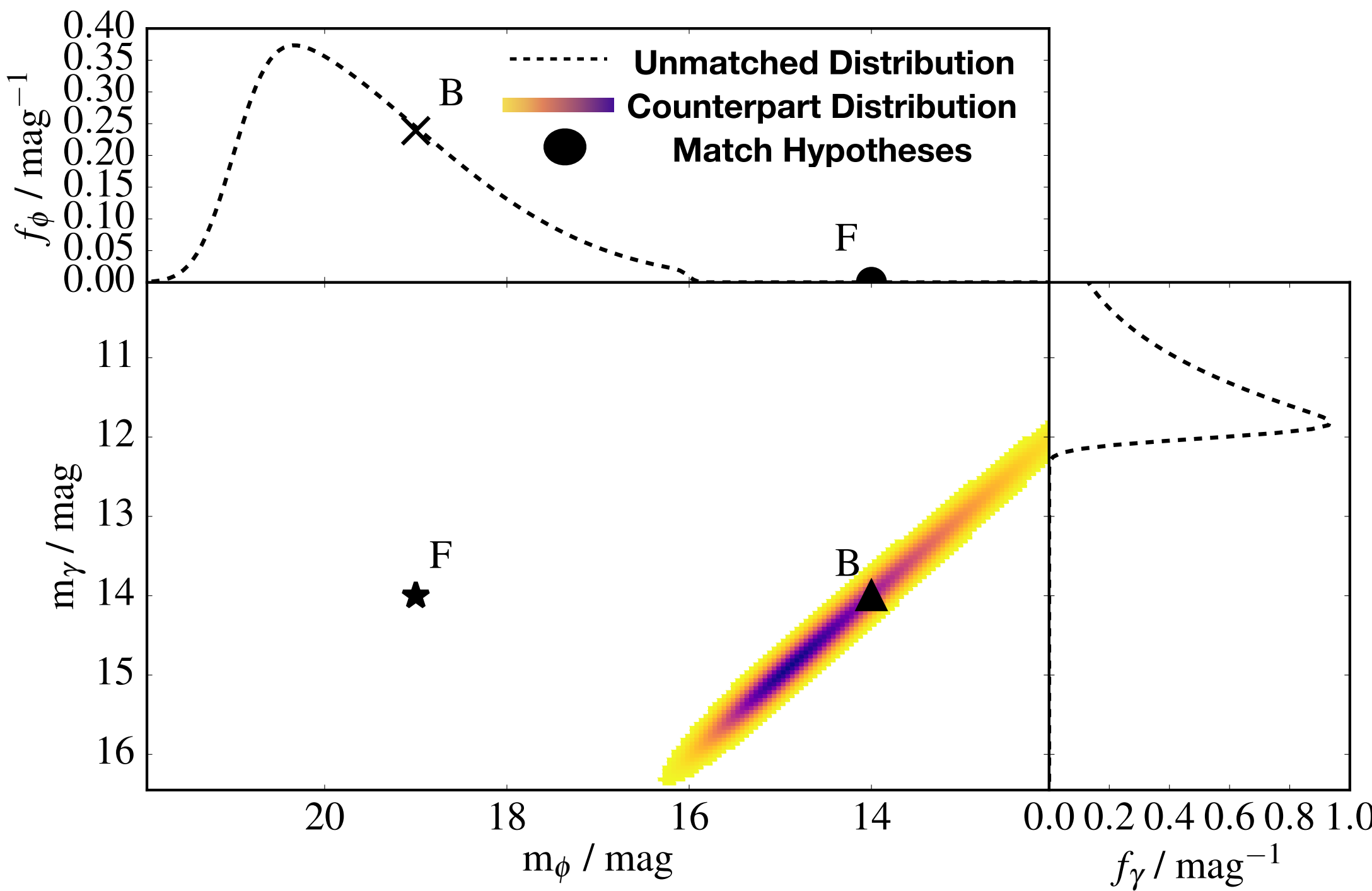
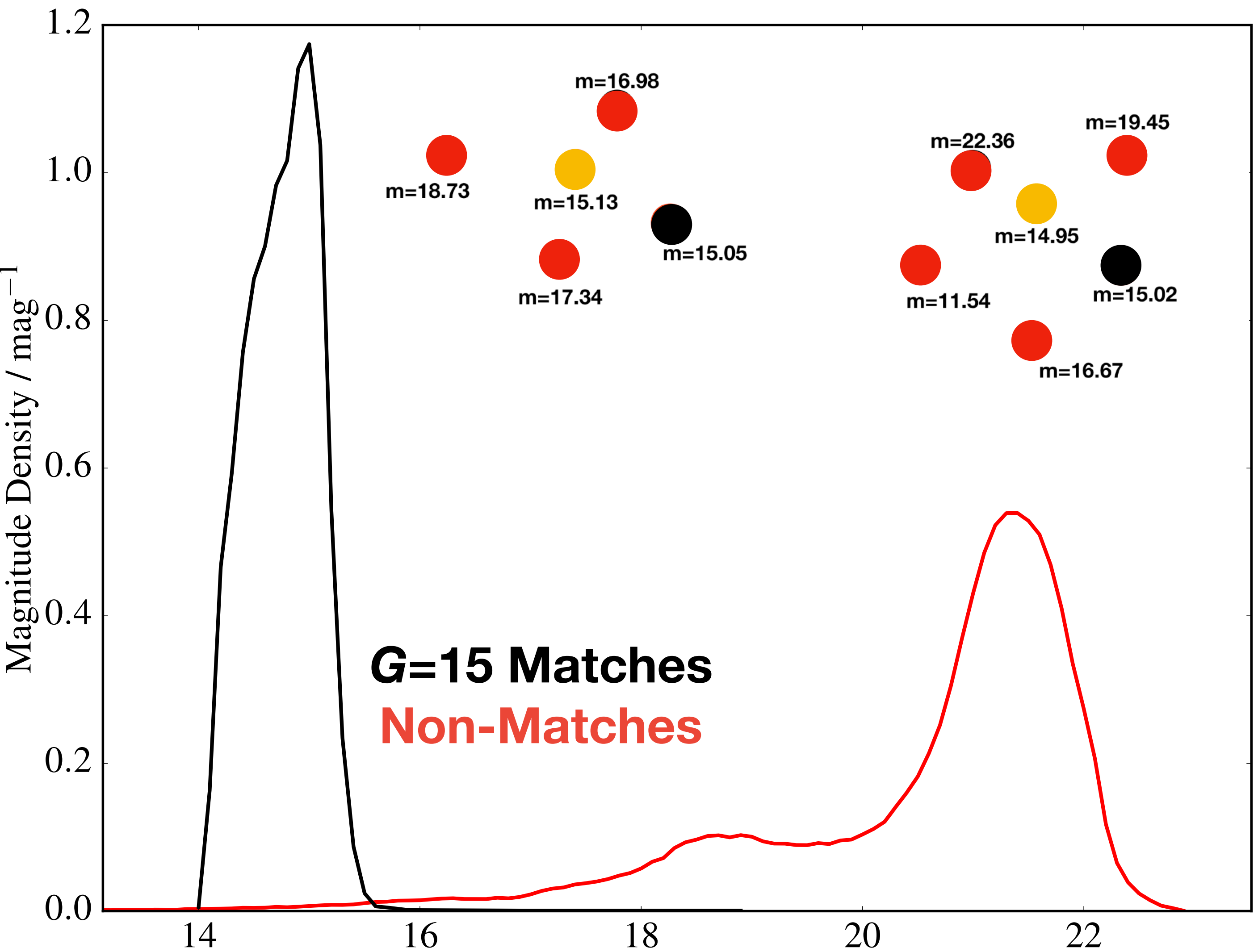
Probability of sources having their brightnesses given they are unrelated to one another (“field stars”)

Probability of sources having their brightnesses given they are counterparts

Wilson & Naylor (2018a)

# Photometry: Rejecting False Positives

$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \neq \zeta} N_{\gamma} f_{\gamma}^{\delta} \prod_{\omega \neq \lambda} N_{\phi} f_{\phi}^{\omega} \prod_{i=1}^k N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$

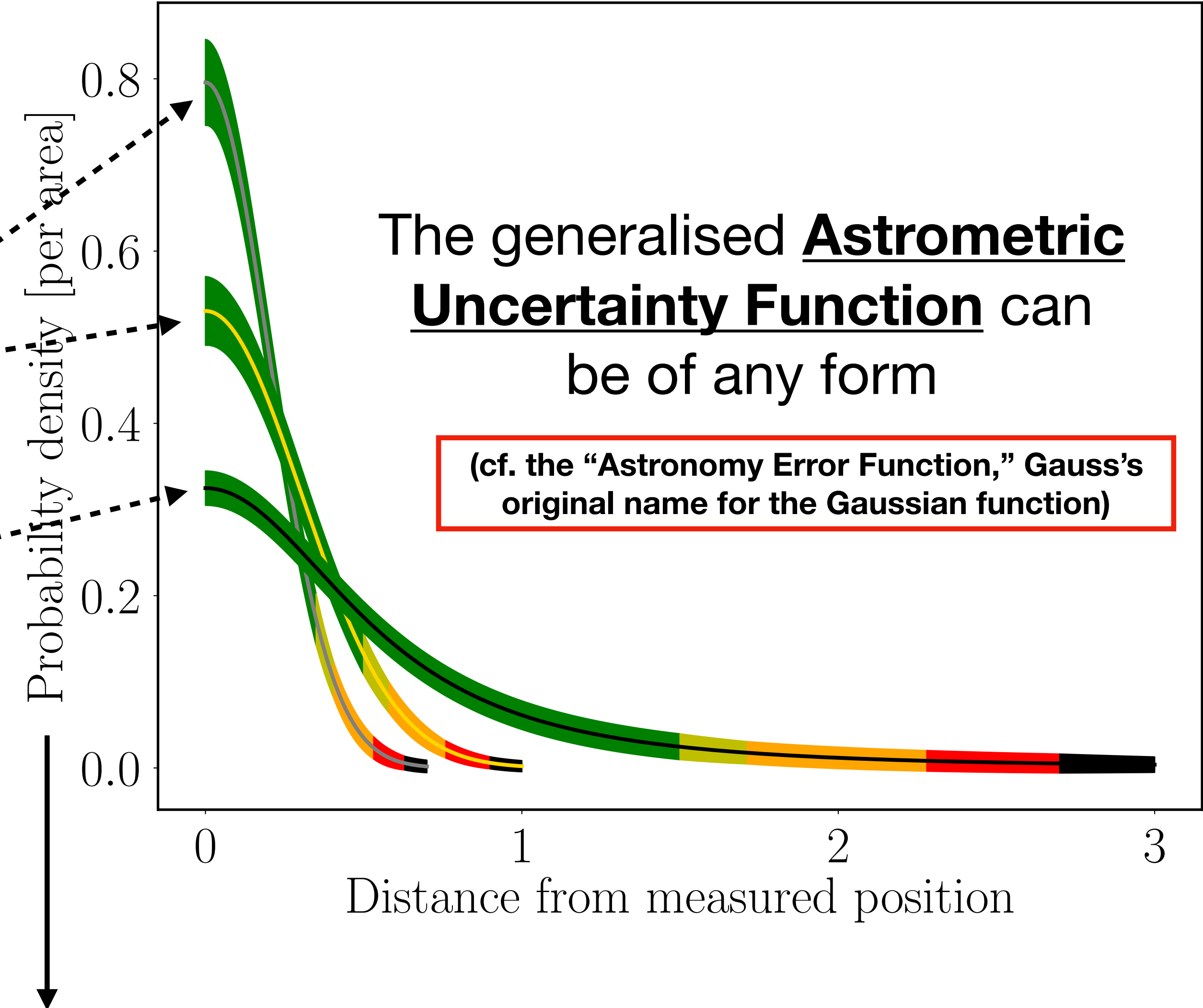
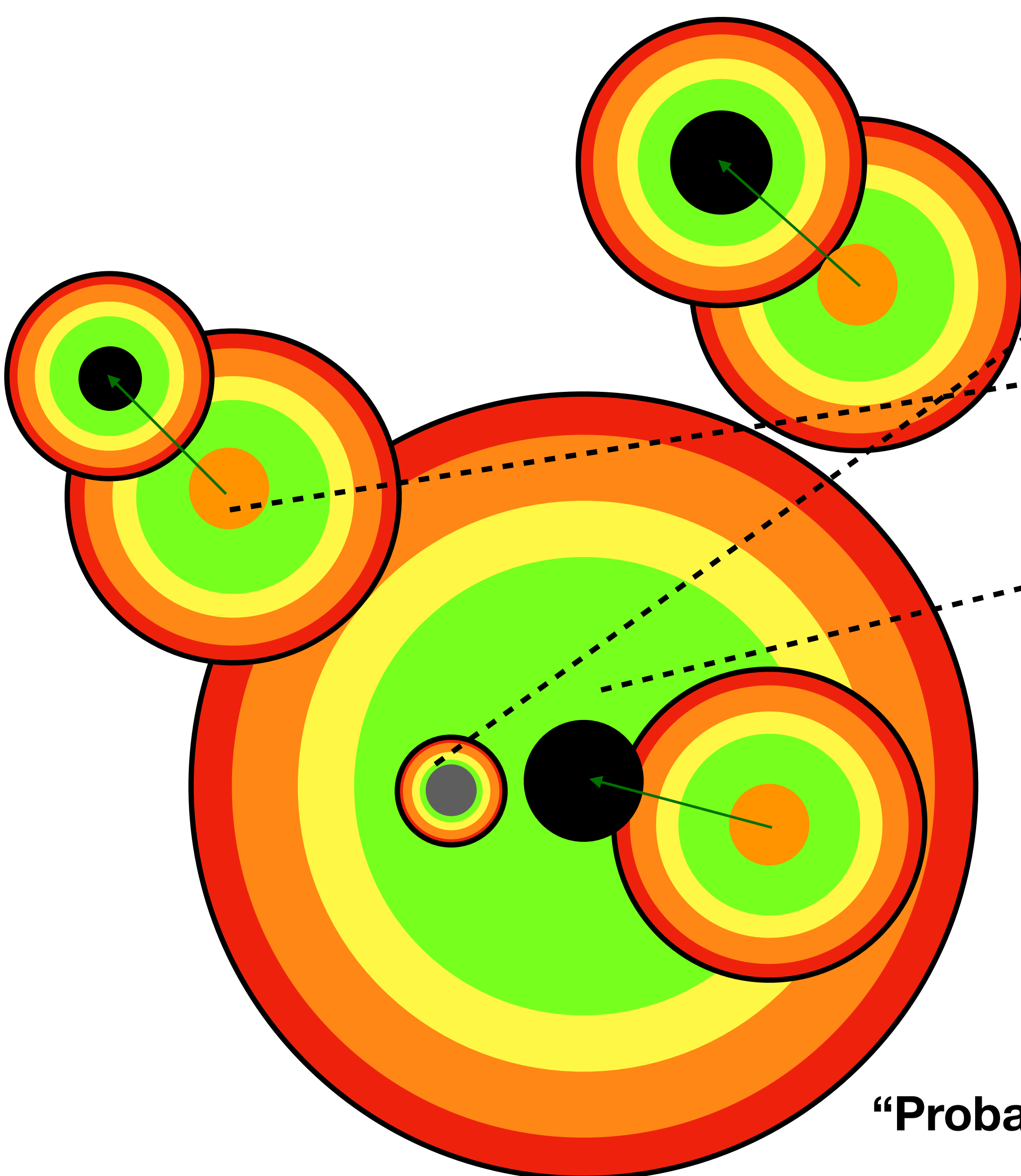


Wilson & Naylor (2018a)

**The photometry-based likelihoods ( $c$  and  $f$ ) allow us to mitigate high false positive rate in crowded fields, but now we need the position-based likelihood  $G$**

IPHAS - Barentsen et al. (2014)  
 Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

# Probabilistic Cross-Matching: the AUF



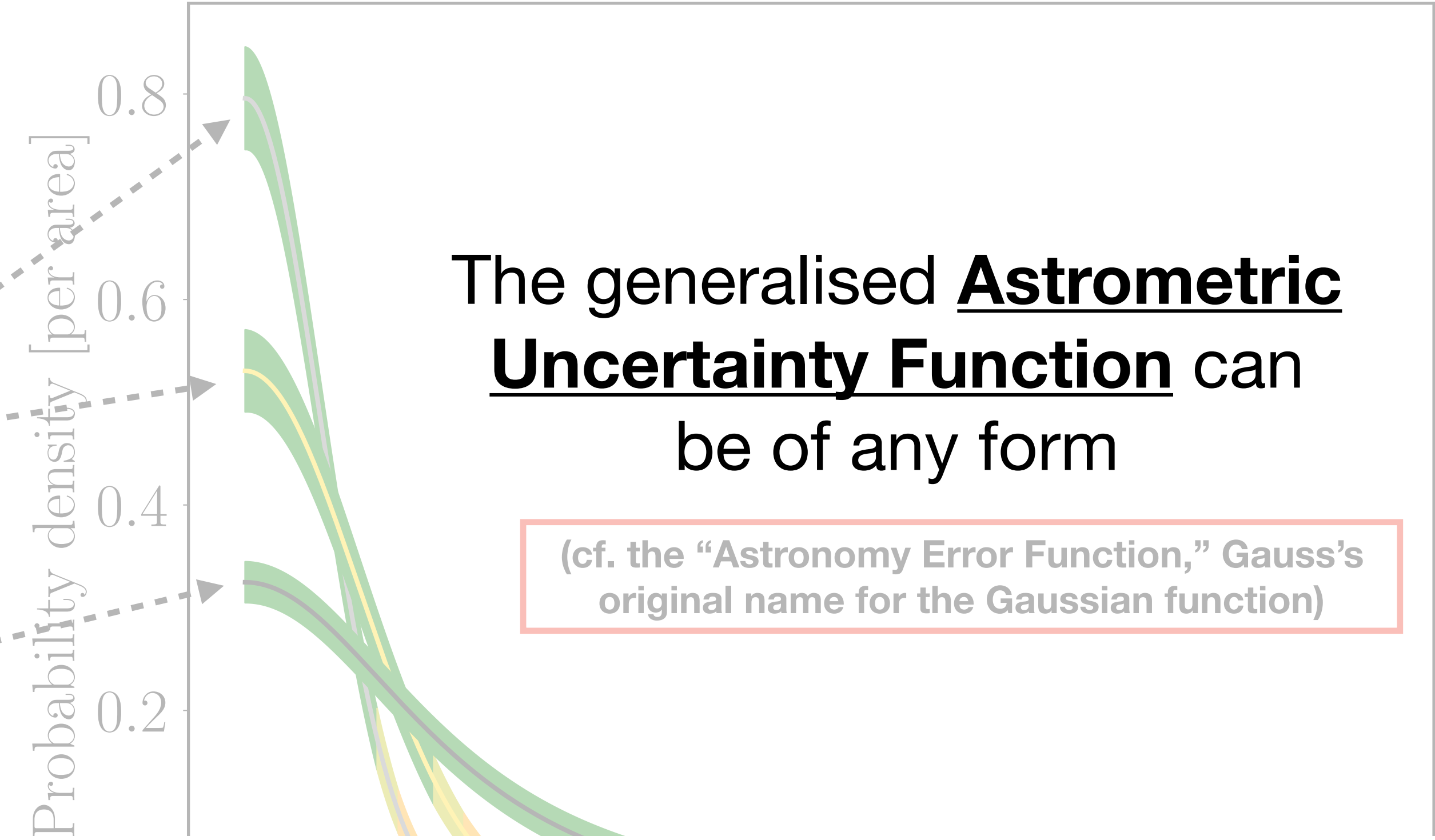
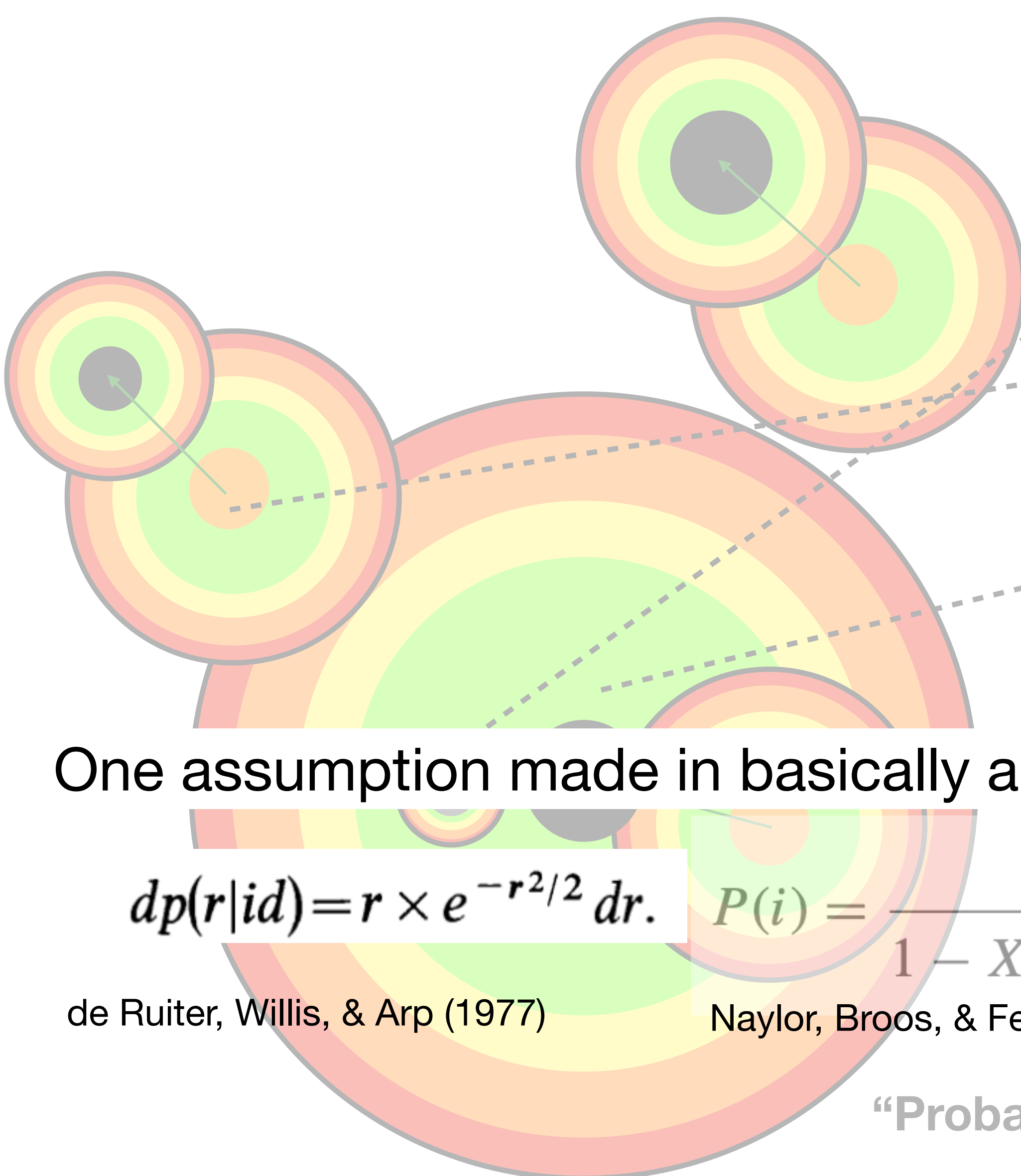
The generalised **Astrometric Uncertainty Function** can be of any form

(cf. the “Astronomy Error Function,” Gauss’s original name for the Gaussian function)

“Probability of True Position being this far from the Measured Position”



# Probabilistic Cross-Matching: the AUF



One assumption made in basically all literature: positional errors of sources are Gaussian!

$$dp(r|id) = r \times e^{-r^2/2} dr.$$

de Ruiter, Willis, & Arp (1977)

$$P(i) = \frac{\frac{Xc(m_i) g(\Delta x_i, \Delta y_i)}{Nf(m_i)}}{1 - X + \sum_j \frac{Xc(m_j) g(\Delta x_j, \Delta y_j)}{Nf(m_j)}}$$

Naylor, Broos, & Feigelson (2013)

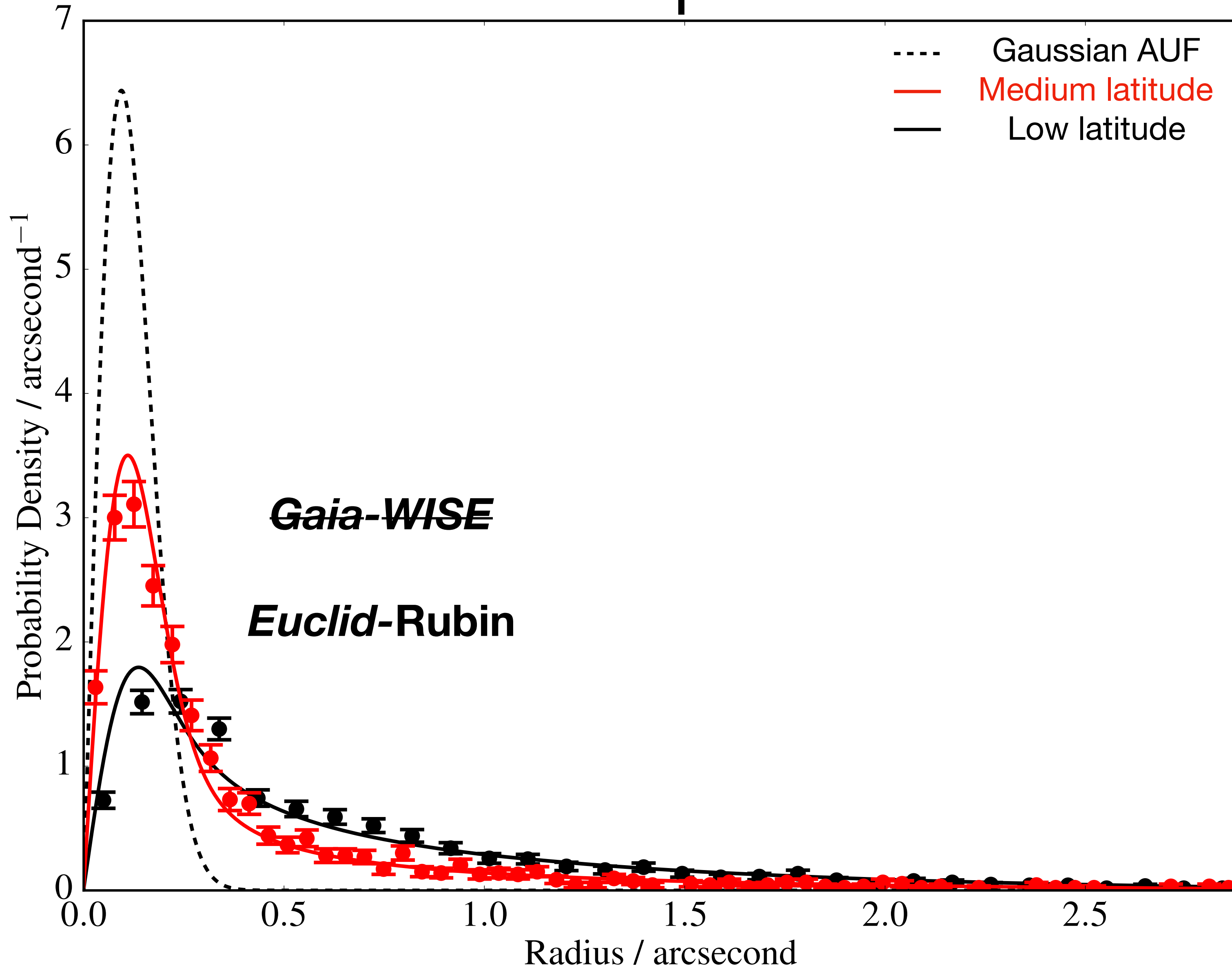
$$p(D|H) = \int p(m|H) \prod_{i=1}^n p_i(x_i|m, H) d^3m$$

Budavári & Szalay (2008)

“Probability of True Position being this far from the Measured Position”

# Additional Components of the AUF

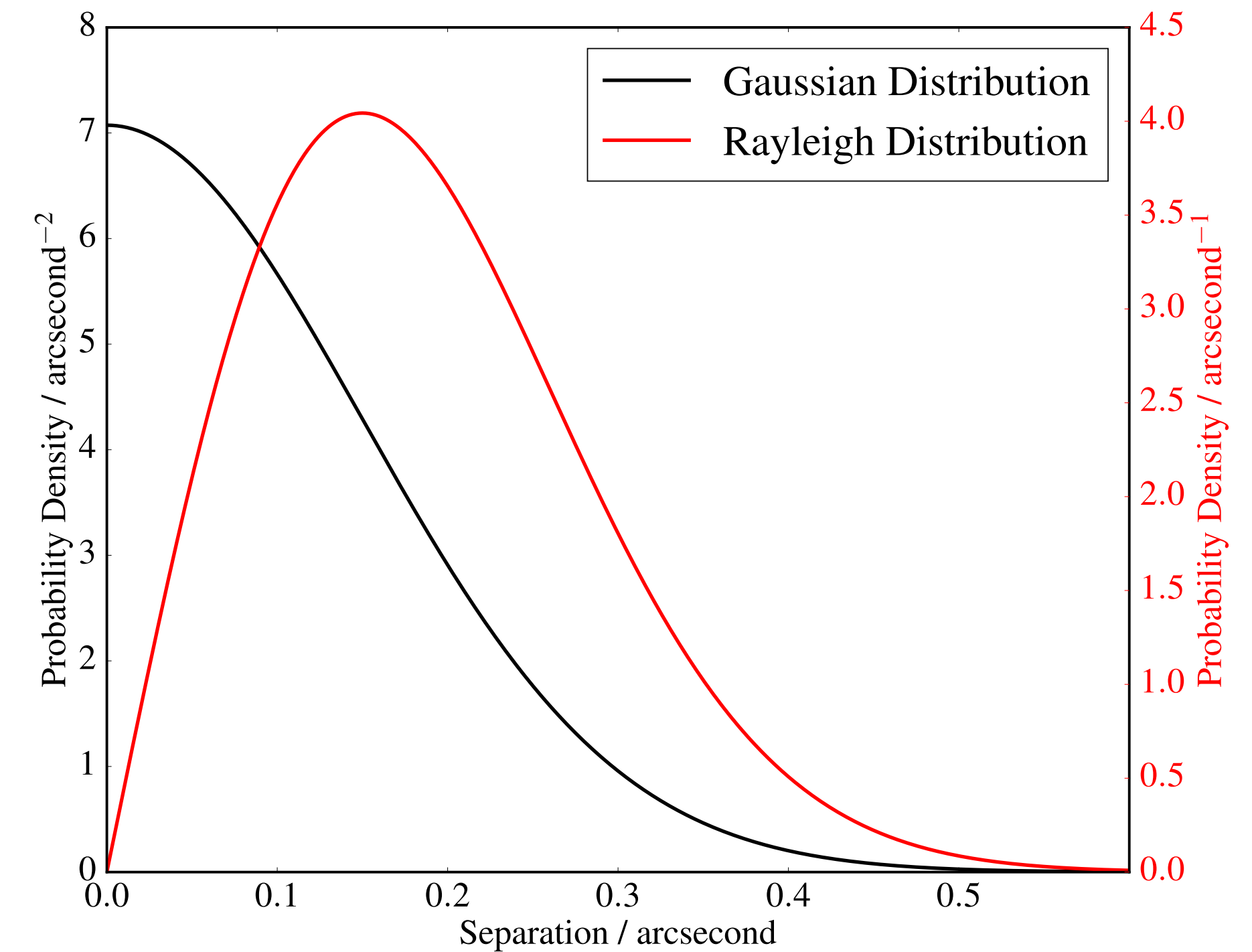
$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \neq \zeta} N_{\gamma} f_{\gamma}^{\delta} \prod_{\omega \neq \lambda} N_{\phi} f_{\phi}^{\omega} \prod_{i=1}^k N_c G_{\gamma \phi}^{\zeta_i \lambda_i} c_{\gamma \phi}^{\zeta_i \lambda_i}$$



$$g(x, y, \sigma) = (2\pi\sigma^2)^{-1} \exp\left(-\frac{1}{2} \frac{x^2 + y^2}{\sigma^2}\right)$$

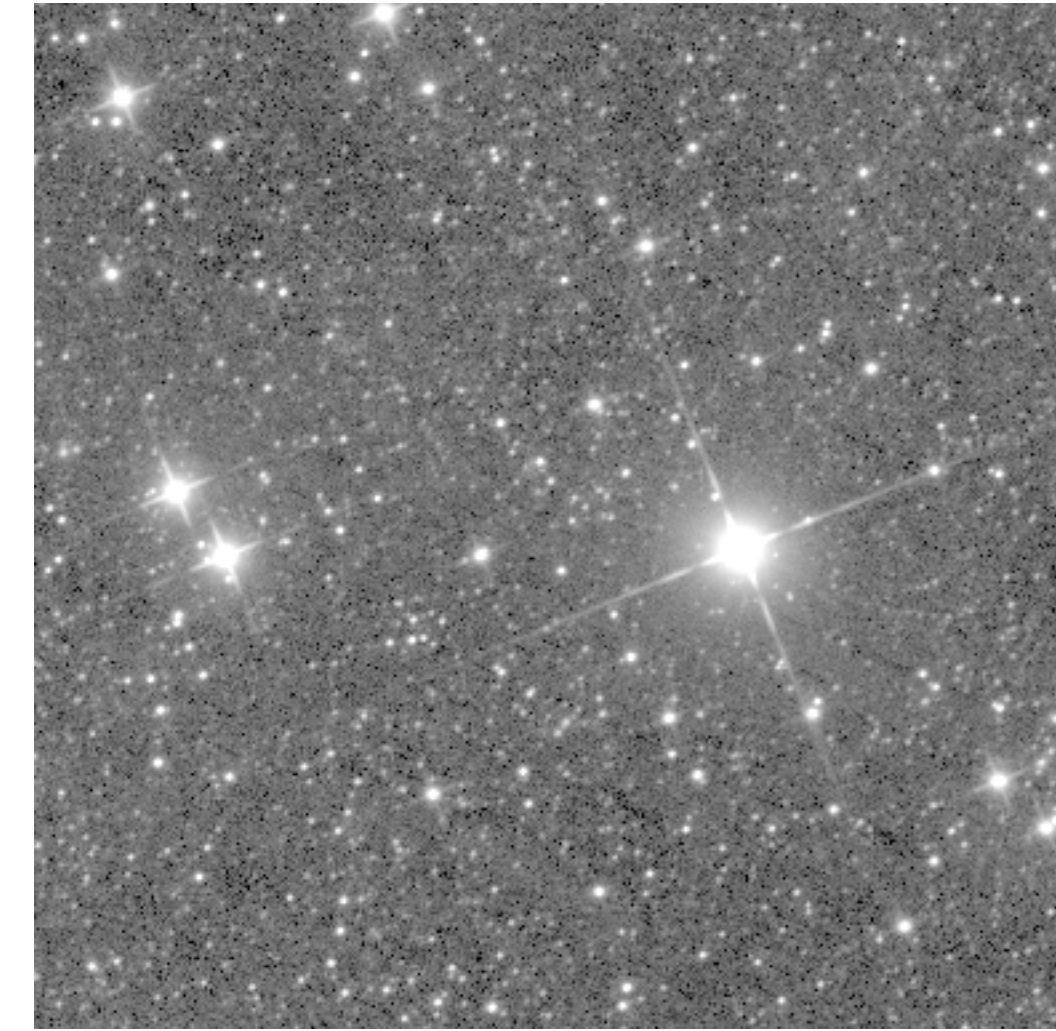
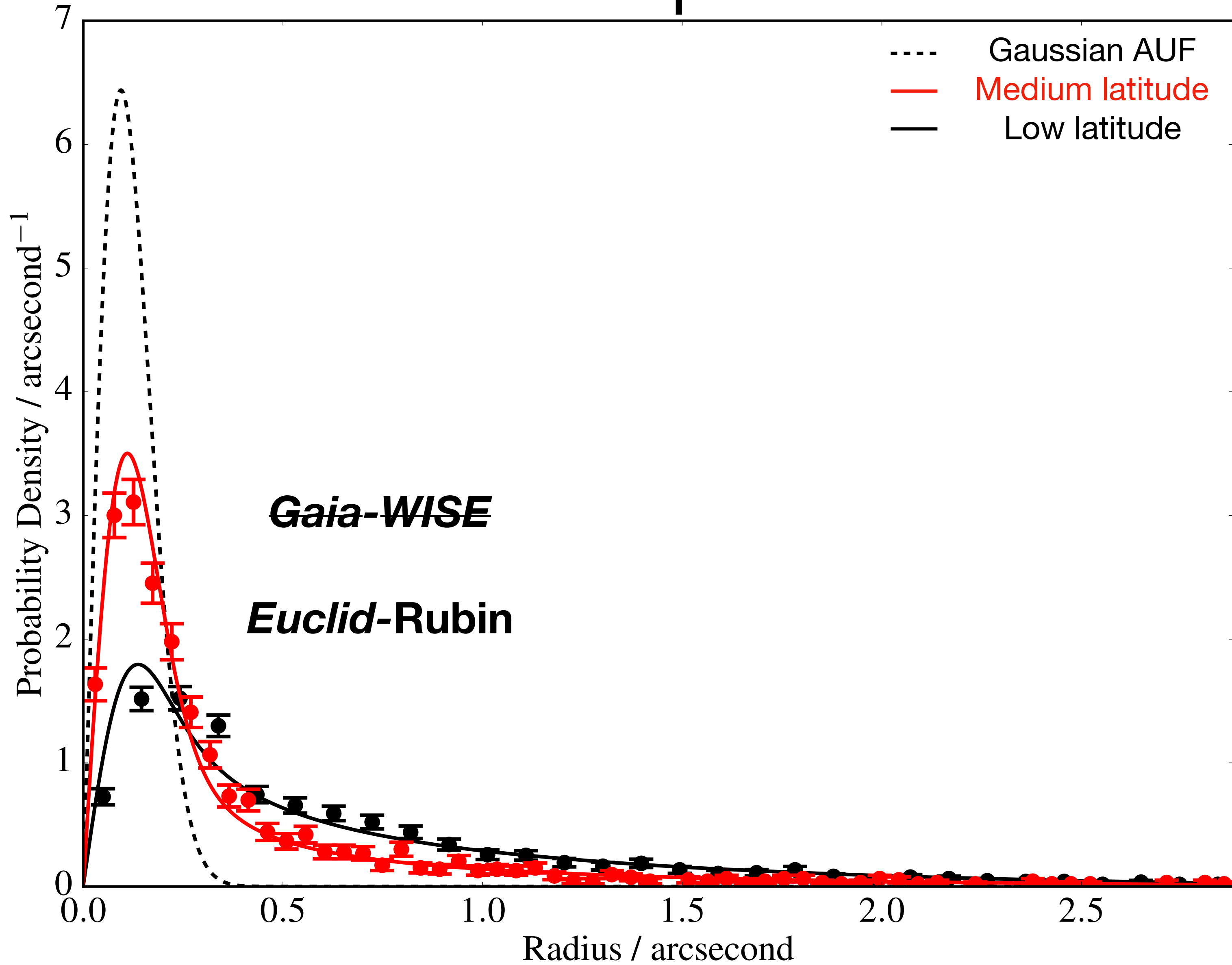
↓

$$g(r, \sigma) = \frac{r}{\sigma^2} \exp\left(-\frac{1}{2} \frac{r^2}{\sigma^2}\right)$$



# Additional Components of the AUF

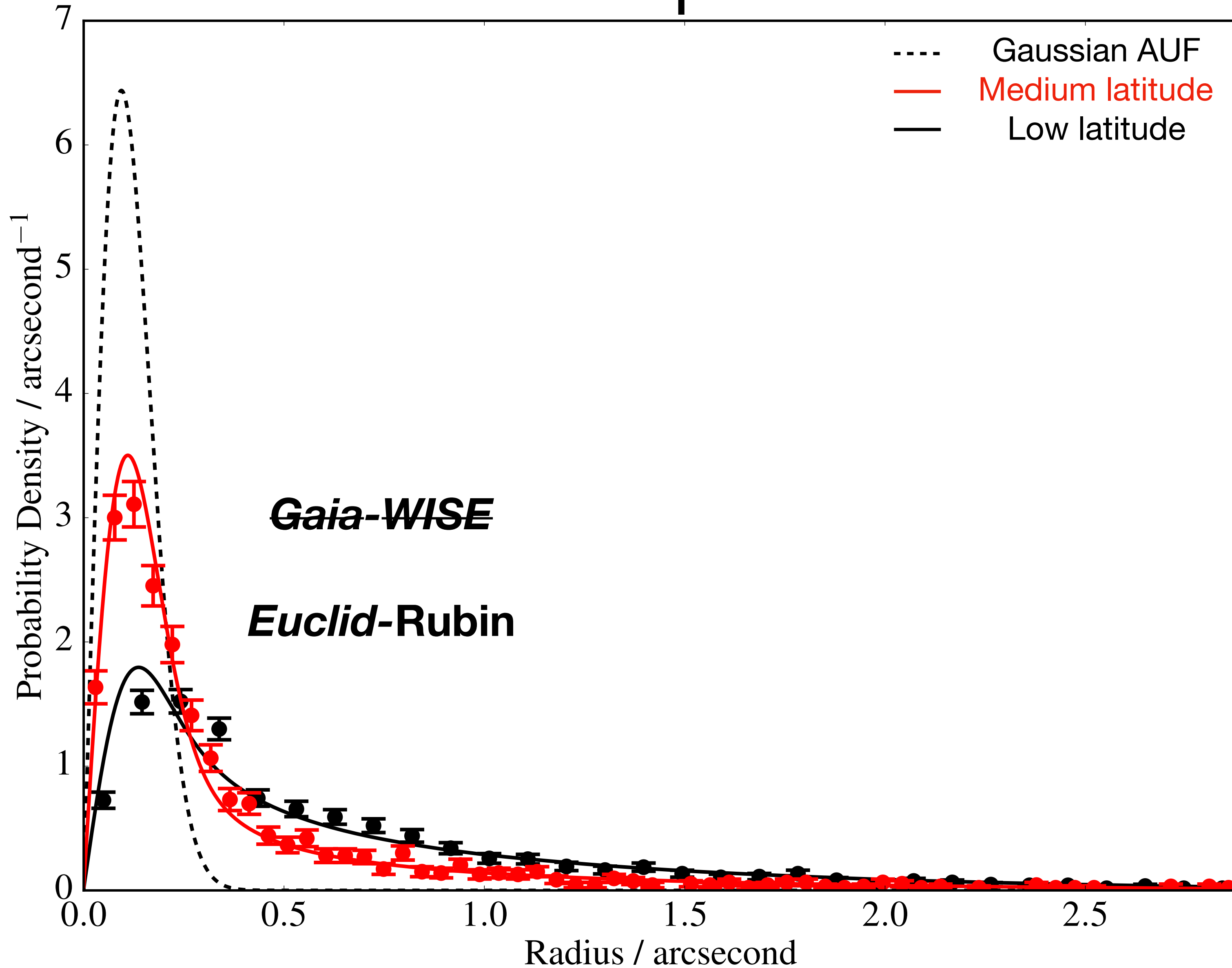
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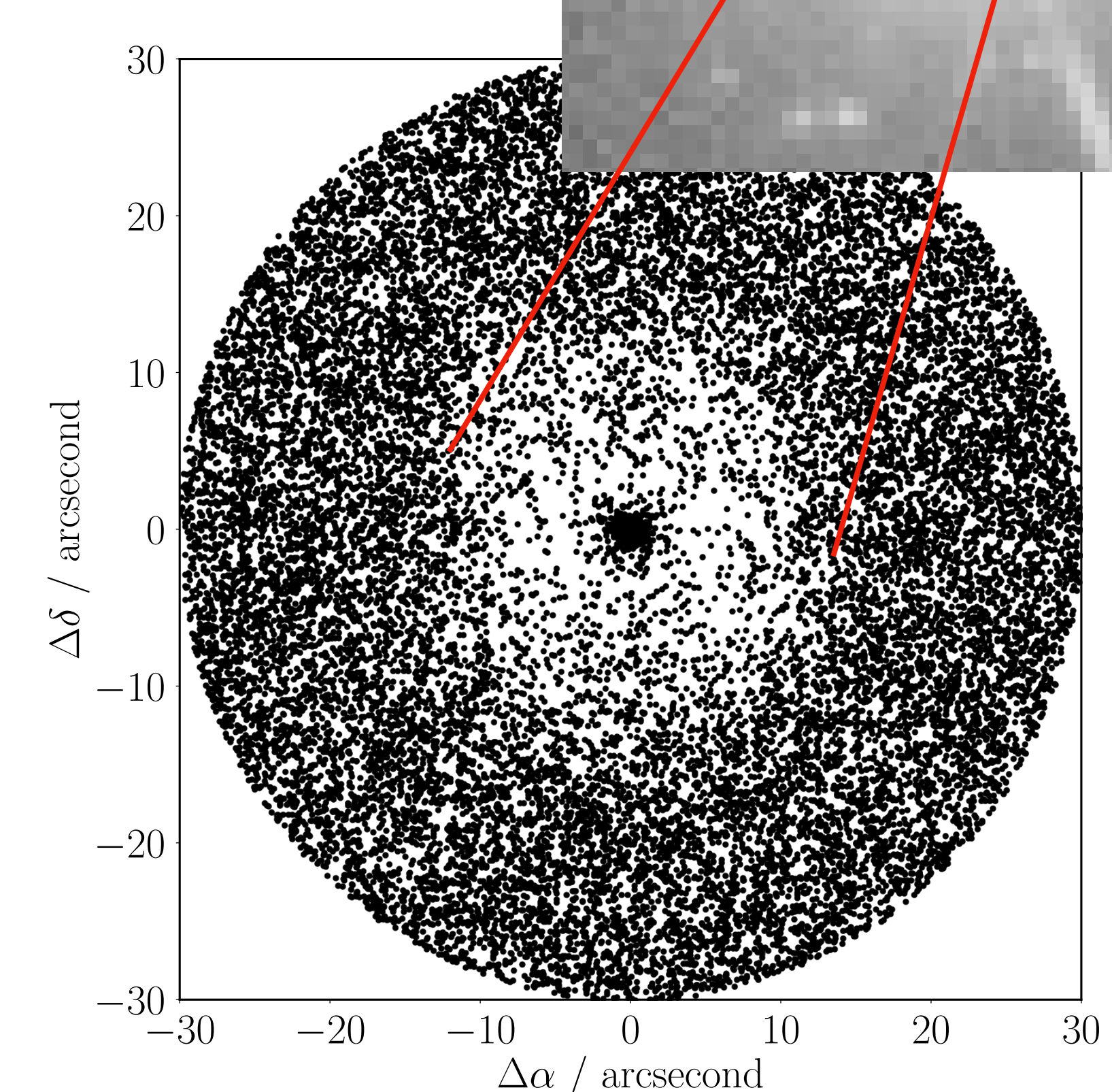


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(and any other systematic — e.g. proper motions, cf. Wilson 2023, RASTI)



WISE - Wright et al. (2010)

Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

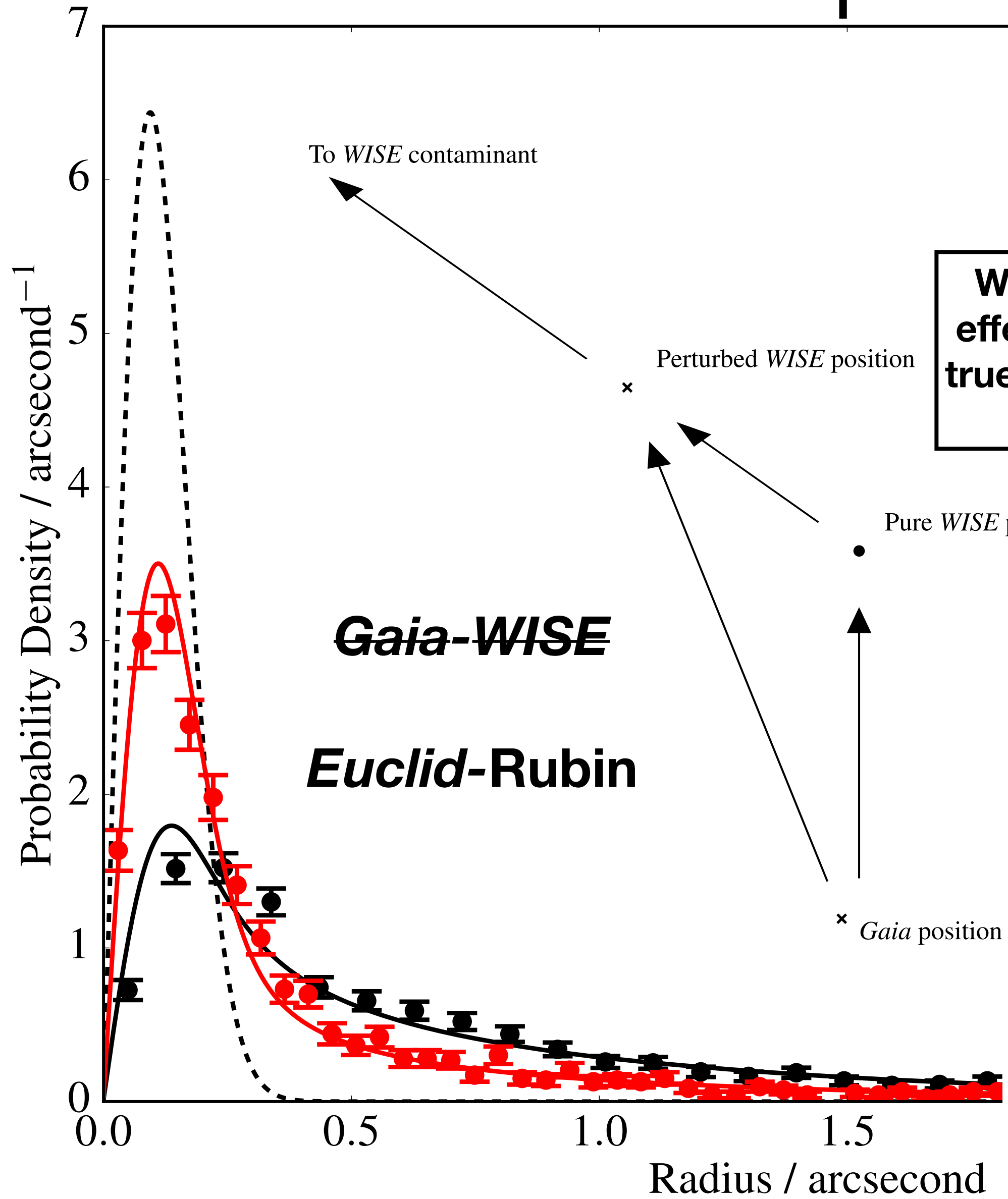
Wilson & Naylor (2017)

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# Additional Components of the AUF

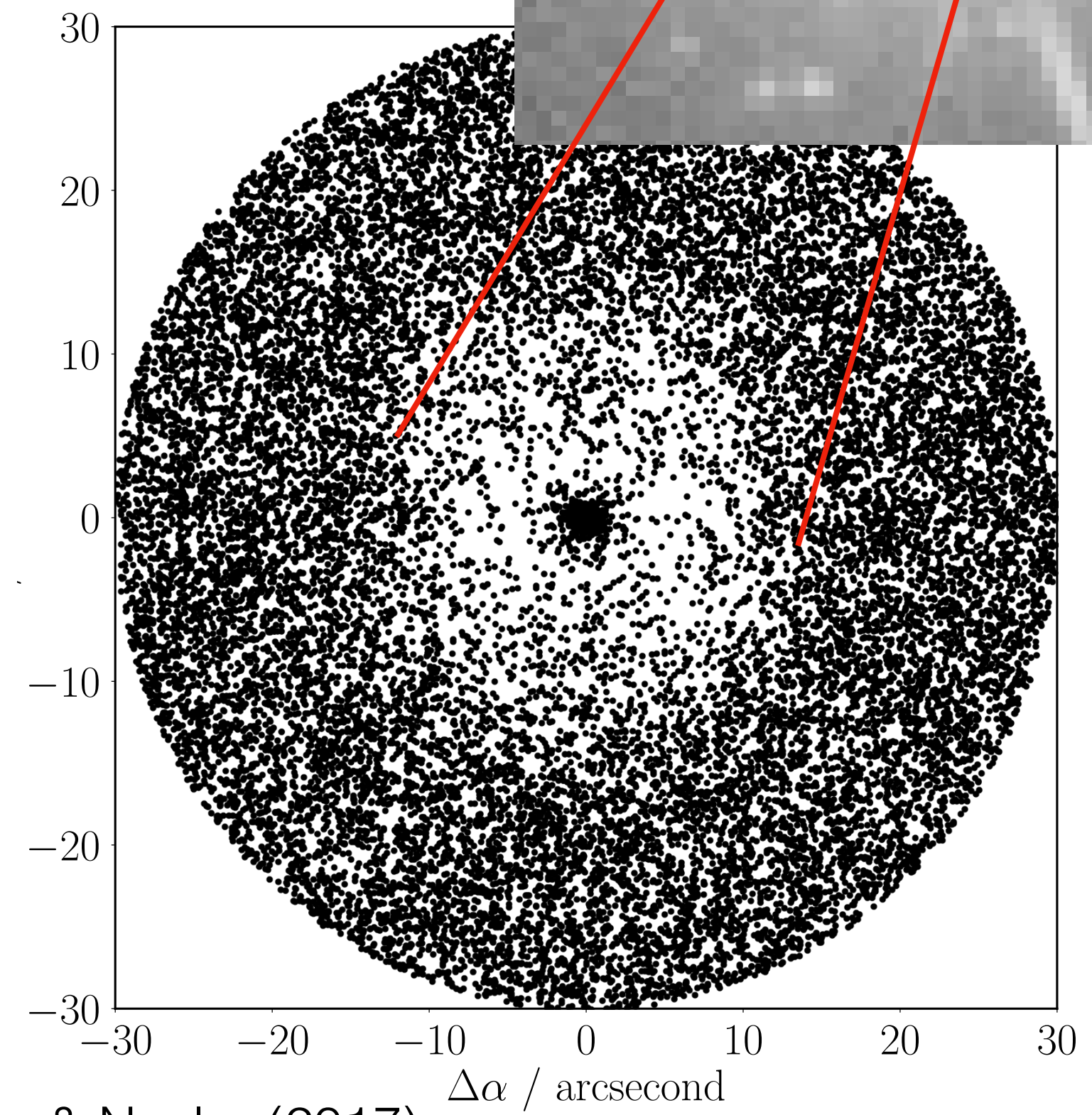
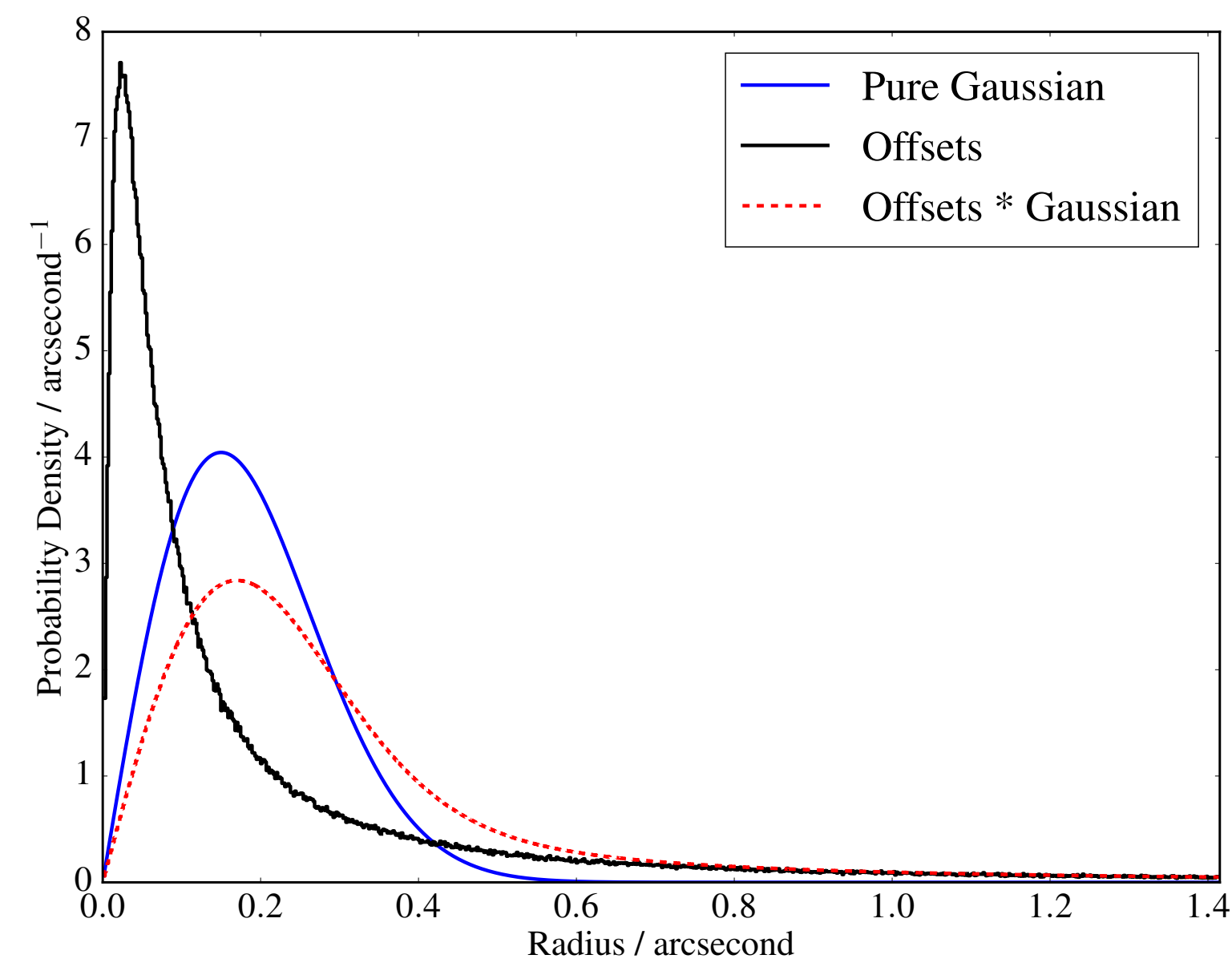
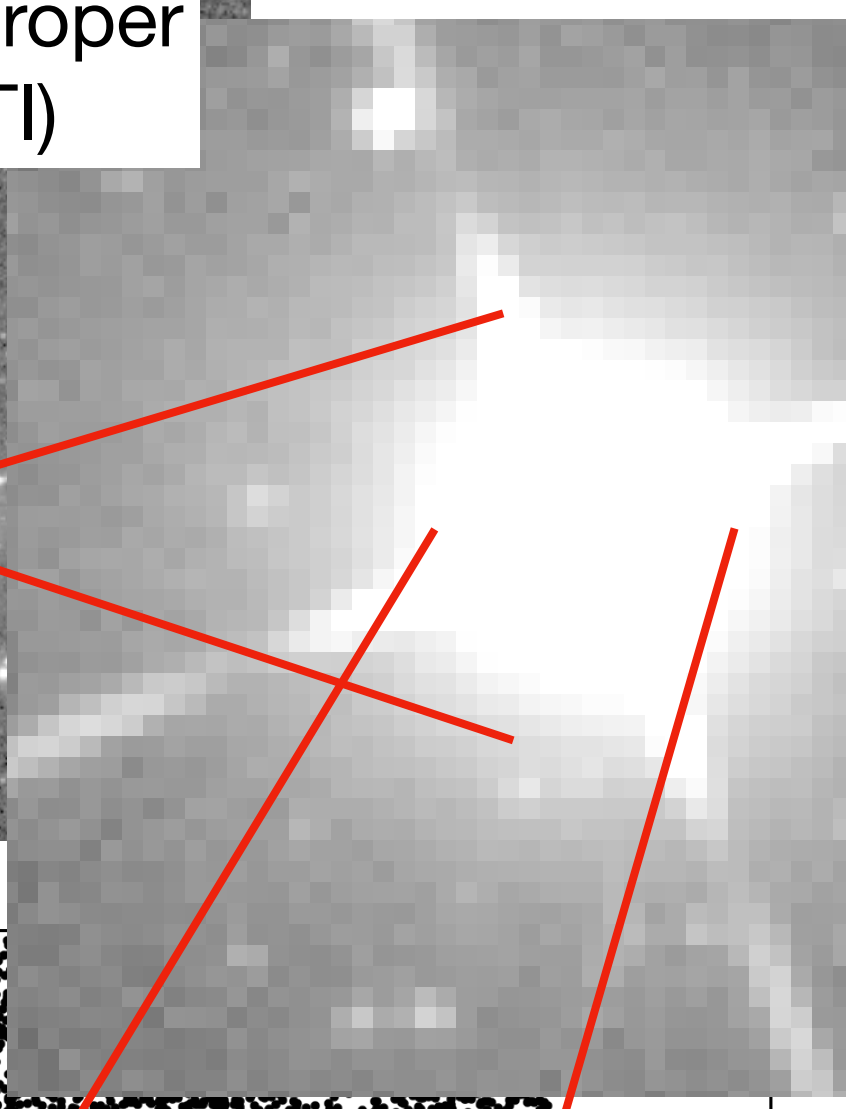
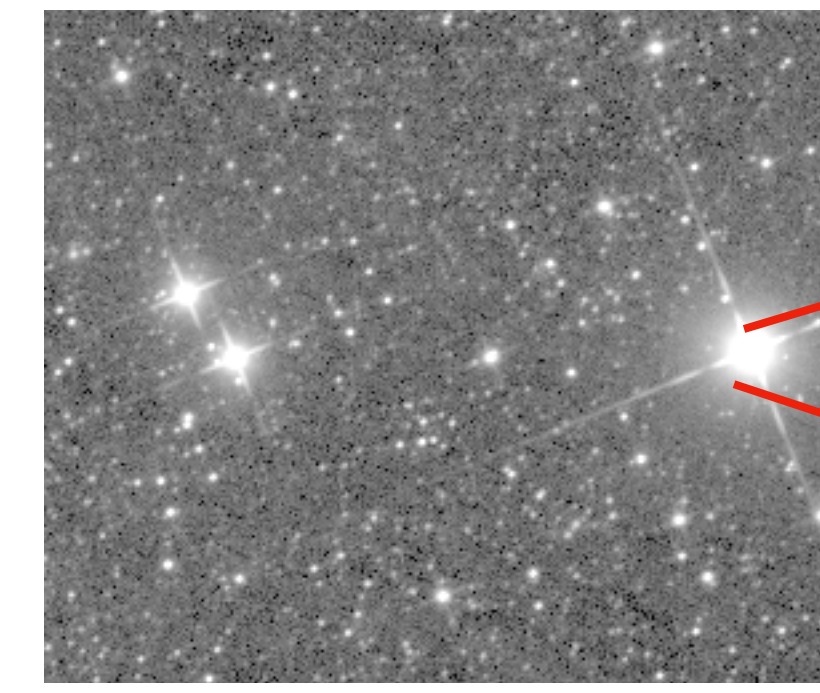
$$P(\zeta, \lambda, k | \gamma, \phi) = \frac{1}{K} \times \prod_{\delta \neq \zeta} N_{\gamma} f_{\gamma}^{\delta} \prod_{\omega \neq \lambda} N_{\phi} f_{\phi}^{\omega} \prod_{i=1}^k N_c G_{\gamma \phi}^{\zeta_i \lambda_i} c_{\gamma \phi}^{\zeta_i \lambda_i}$$



- Gaussian AUF
- Medium latitude
- Low latitude

**Without modelling this extra effect, we fail to recover many true pairings, with an artificially high false negative rate!**

(and any other systematic — e.g. proper motions, cf. Wilson 2023, RASTI)



WISE - Wright et al. (2010)

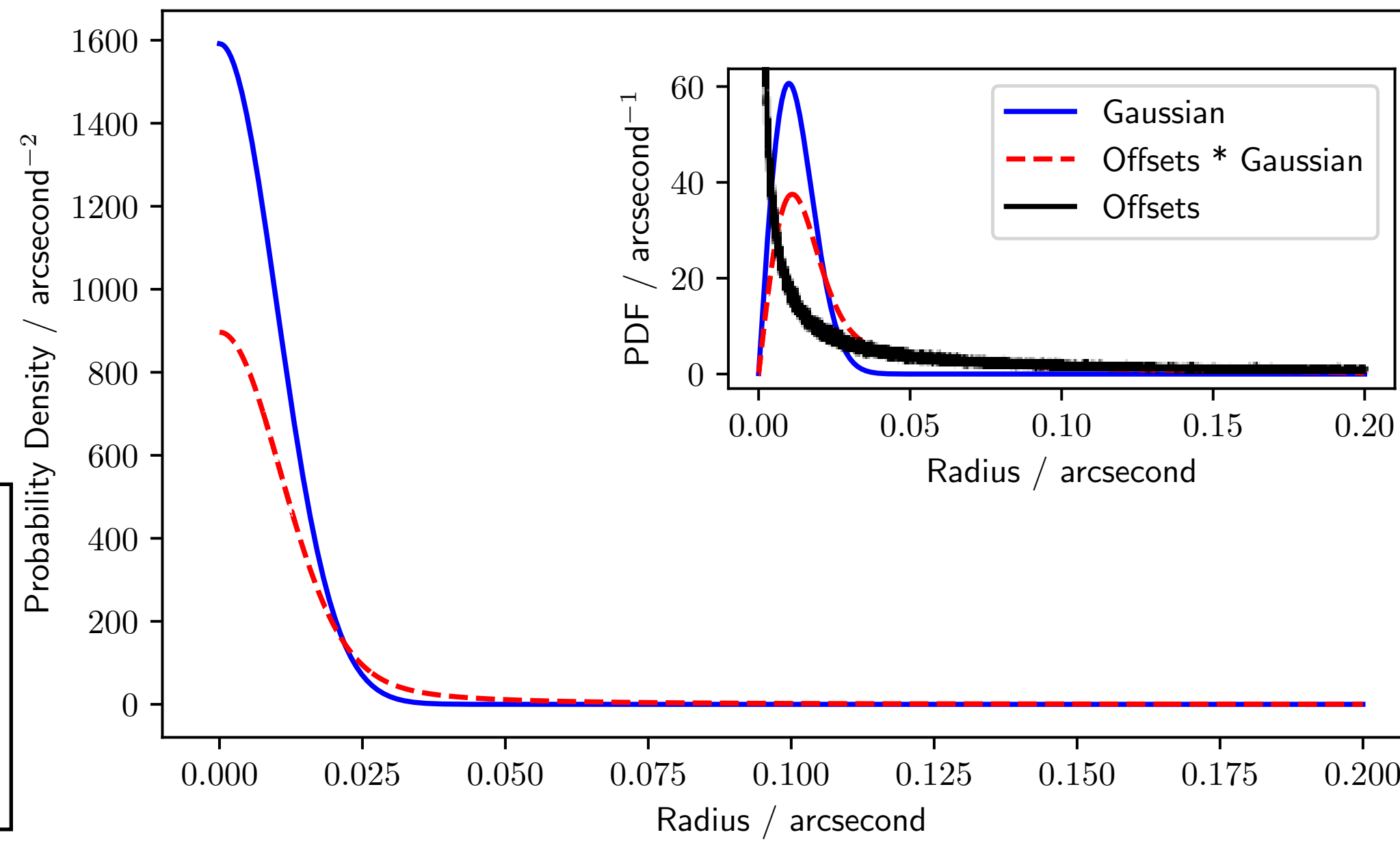
Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

Wilson & Naylor (2018b)

Wilson & Naylor (2017)

# The Rubin AUF: Galactic Plane

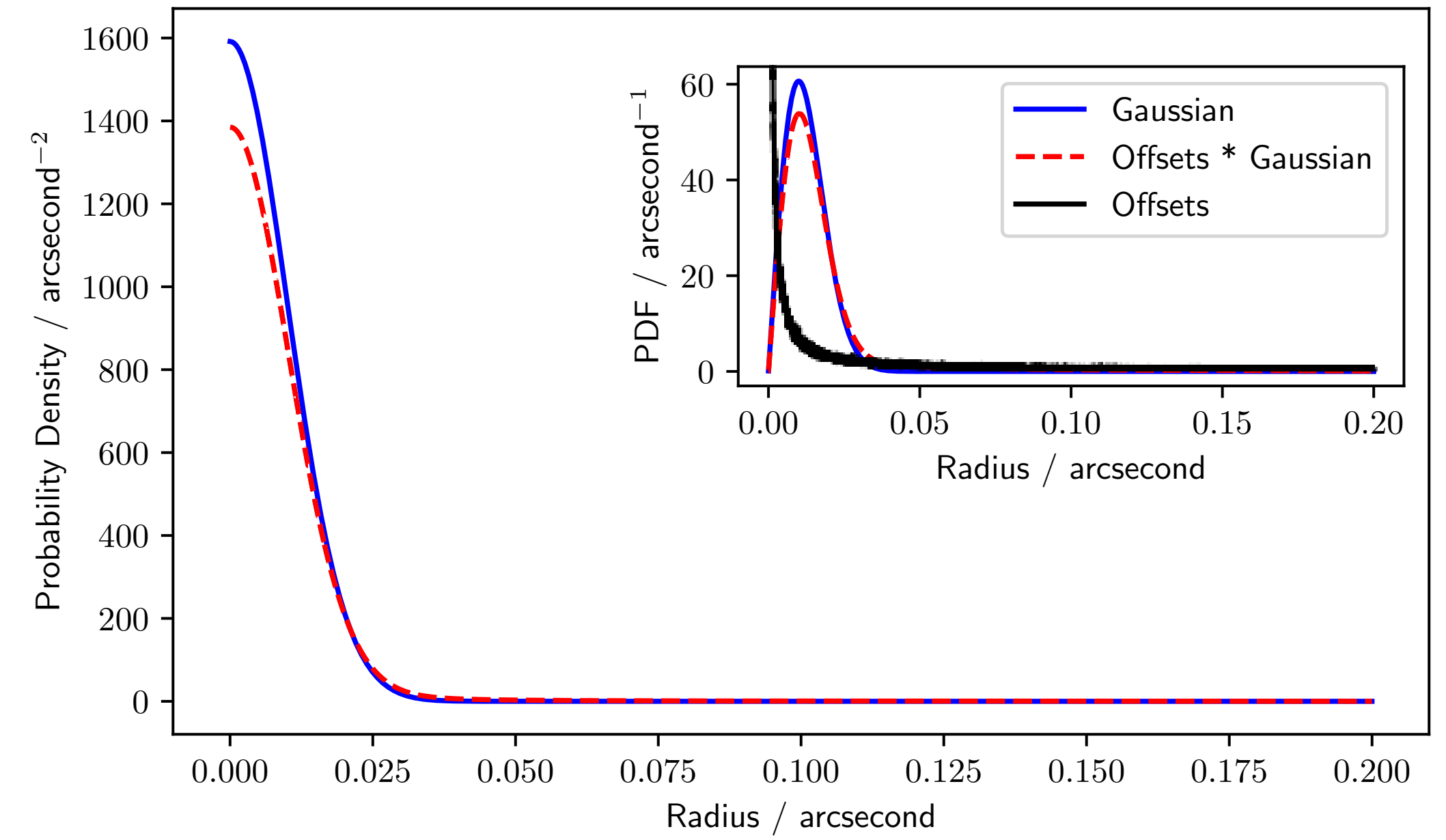
## Galactic Centre



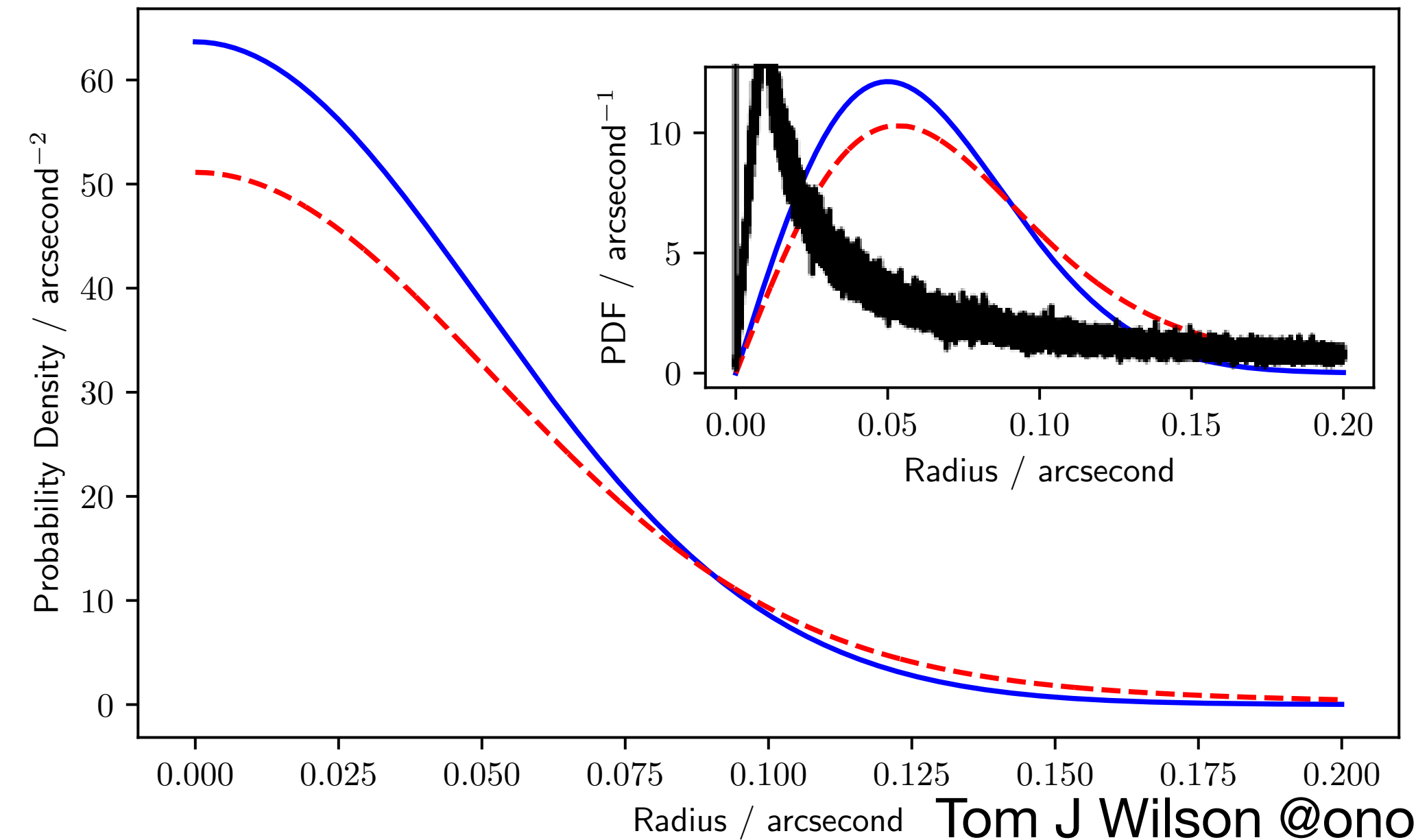
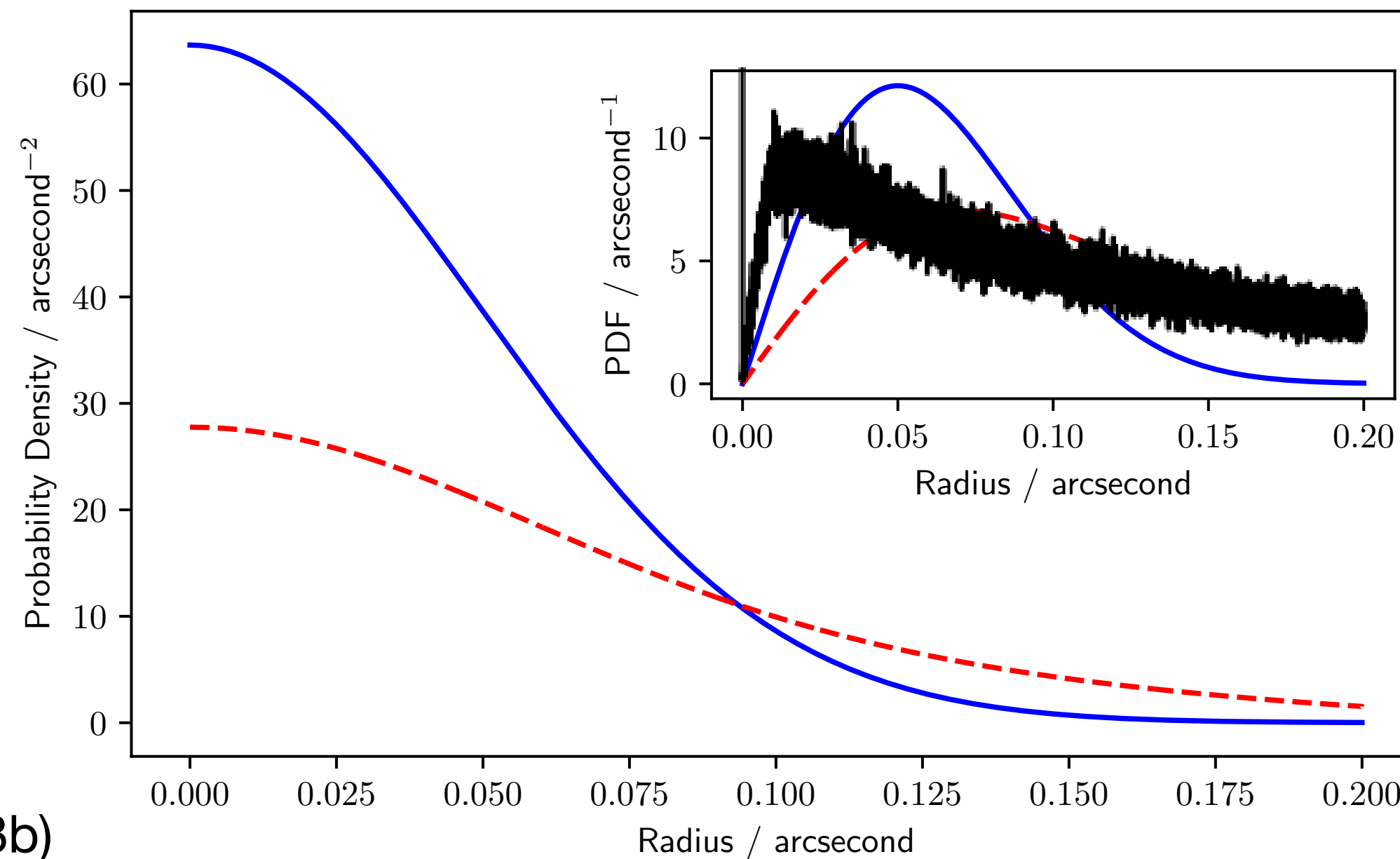
**Single-visit**

**Without modelling this extra effect, we fail to recover many true pairings, with an artificially high false negative rate!**

## Not the Galactic Centre

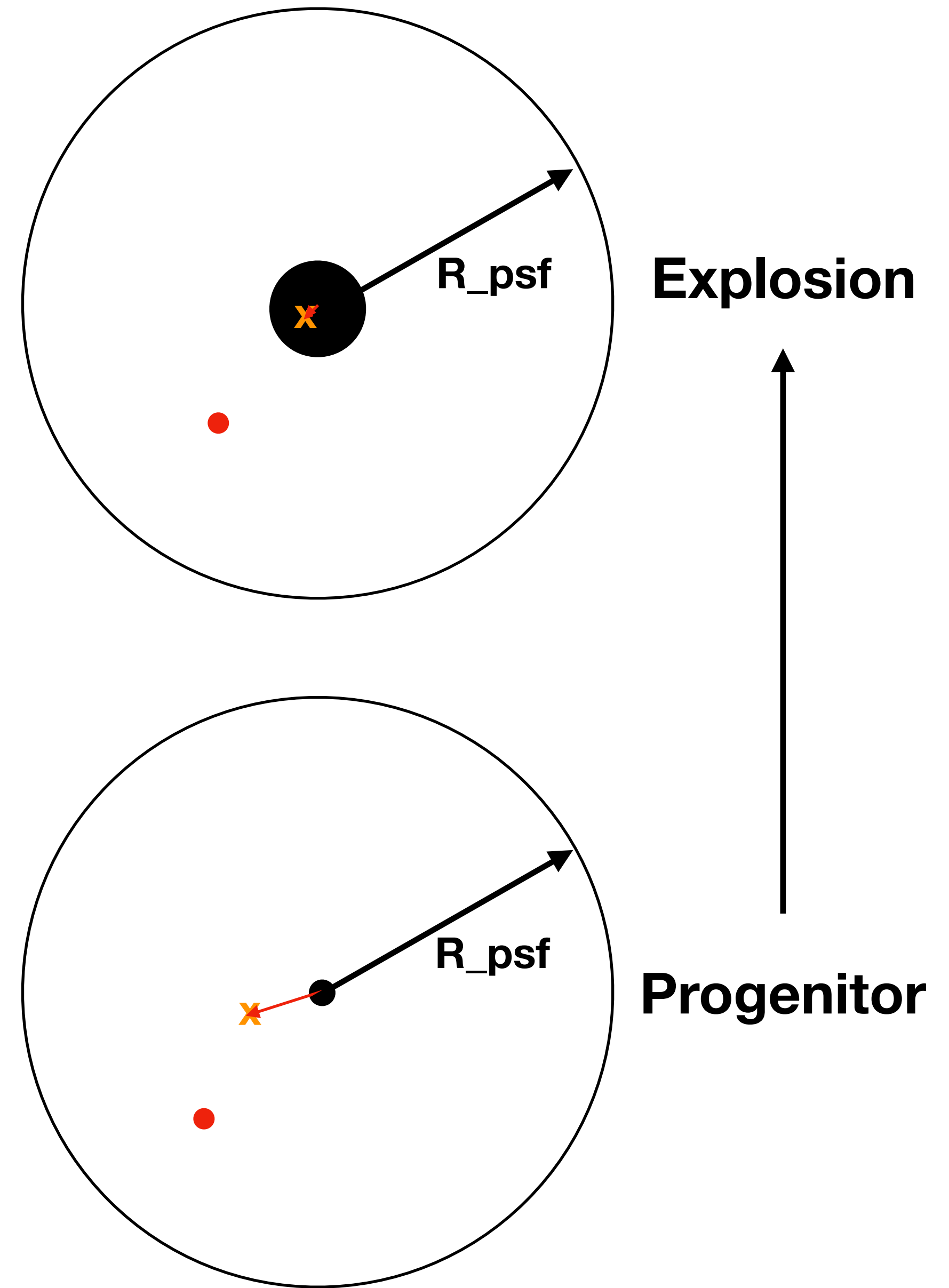
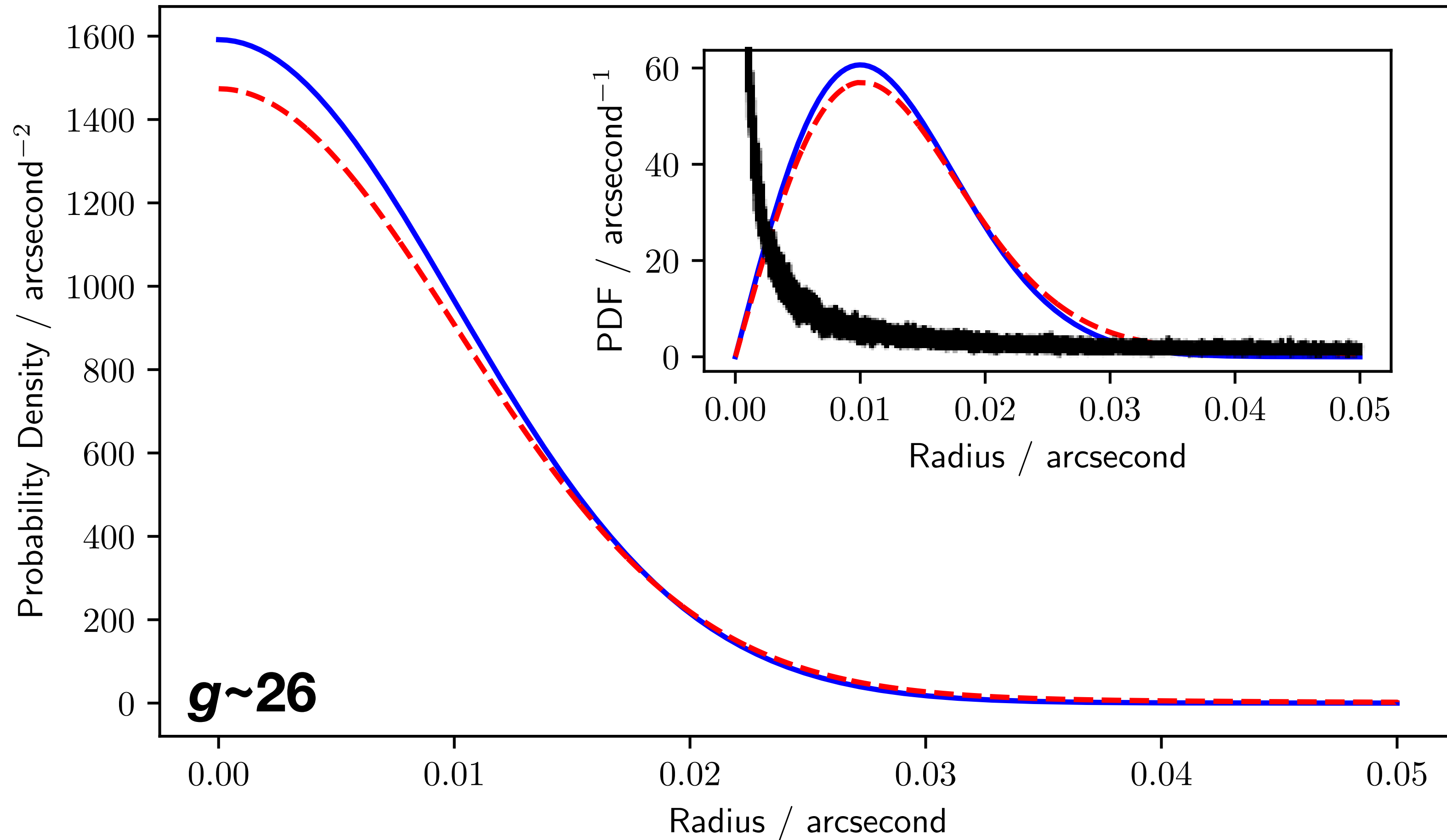


**Co-add**

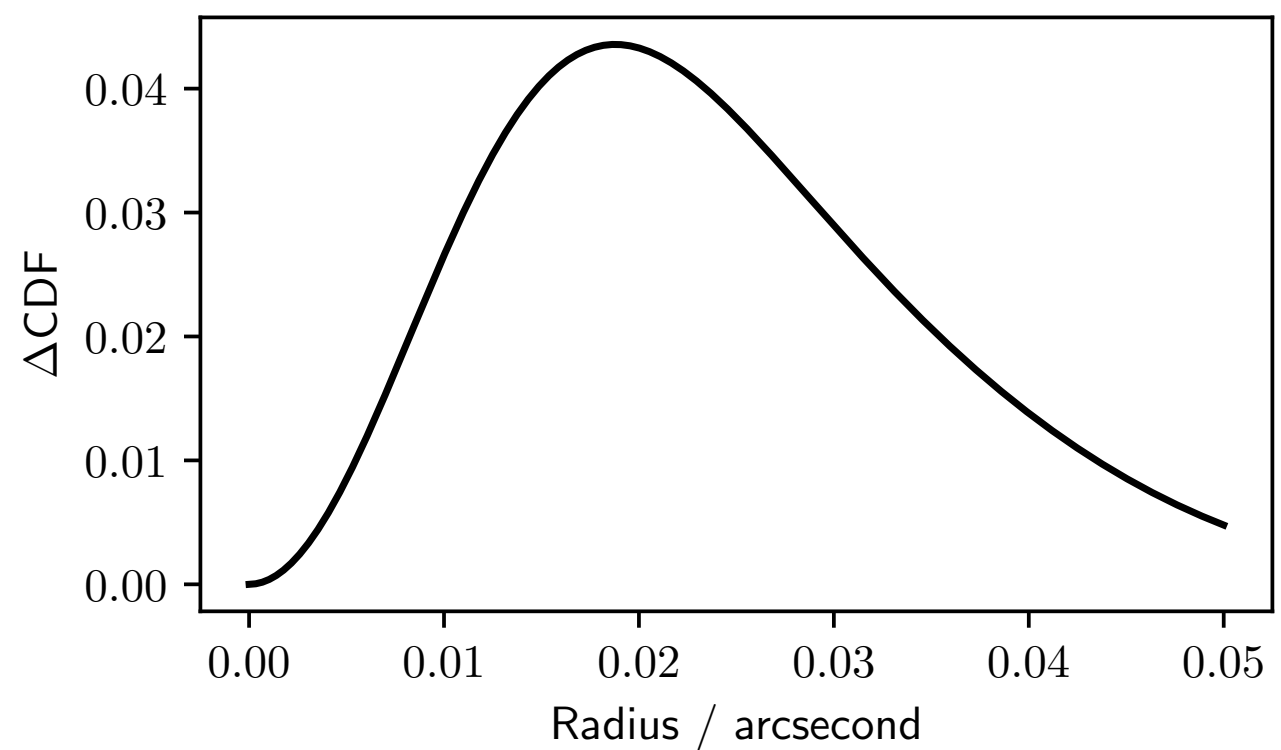




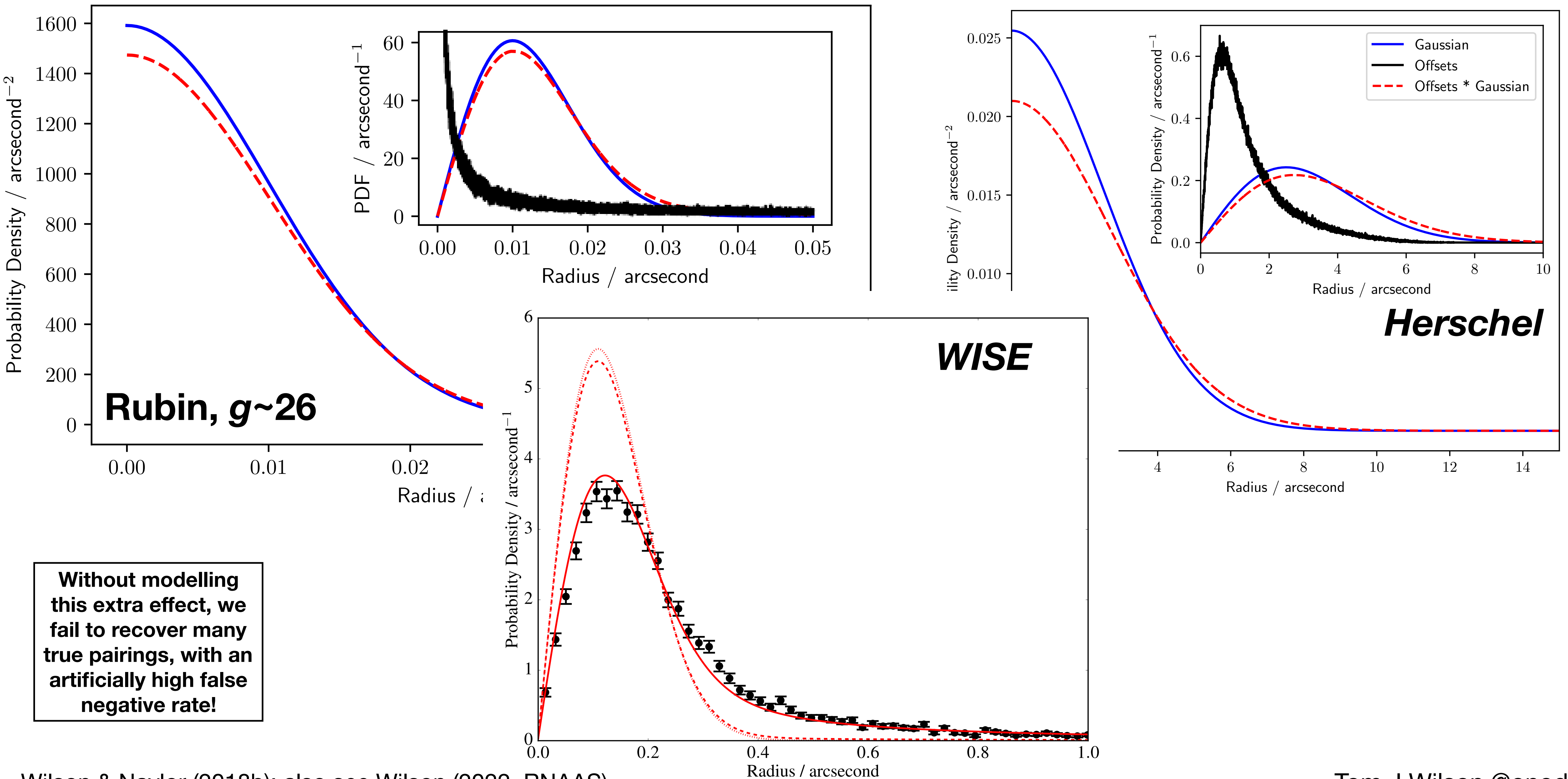
# The Rubin AUF: Extra-Galactic, Transients



Without modelling this extra effect, we fail to recover many true pairings, with an artificially high false negative rate!



# The Rubin AUF: Extra-Galactic, Transients





# Matching Across Catalogues using the Astrometric Uncertainty Function and Flux



<https://github.com/macauff/macauff>





## Cross-Match Tools, Framework, Usage



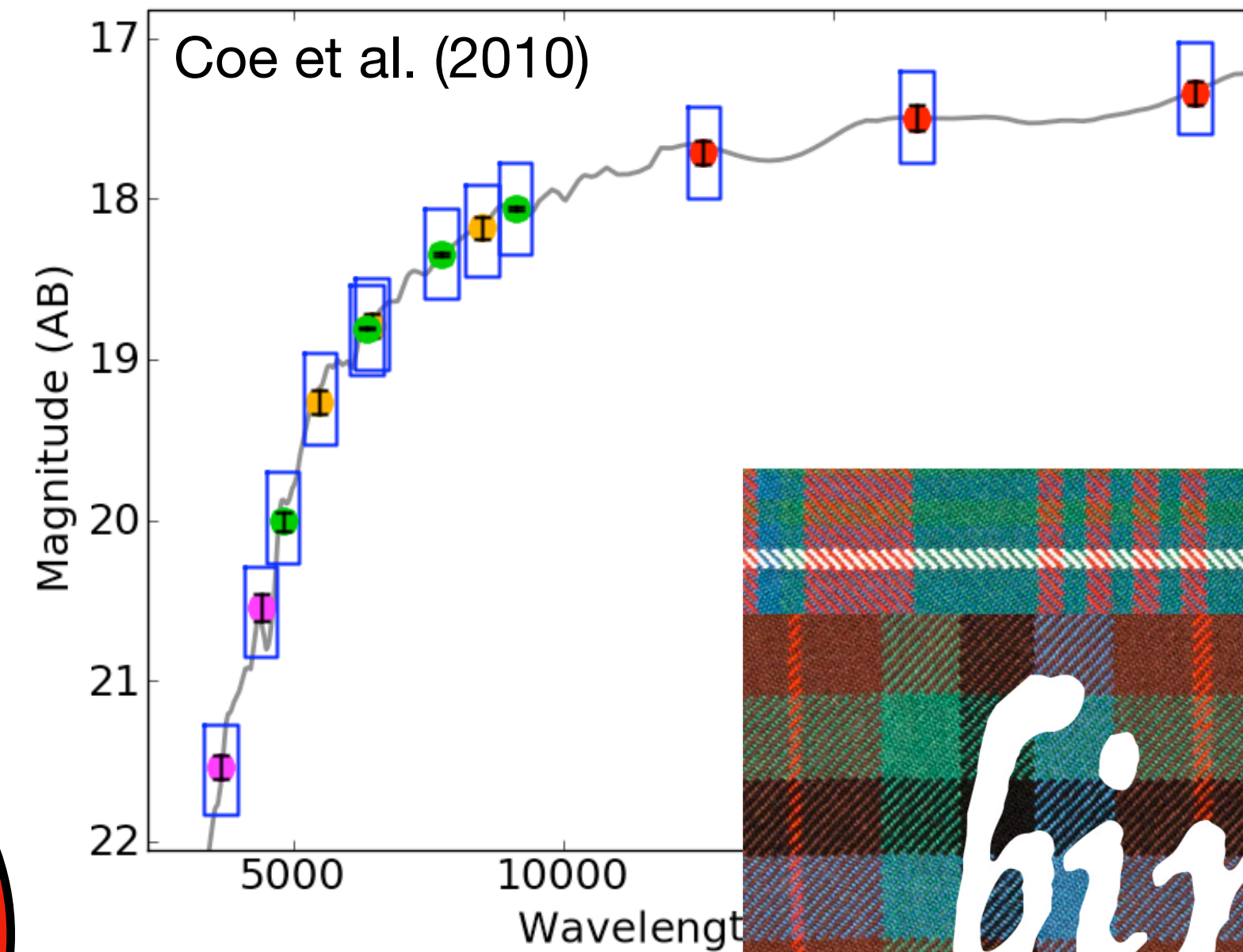
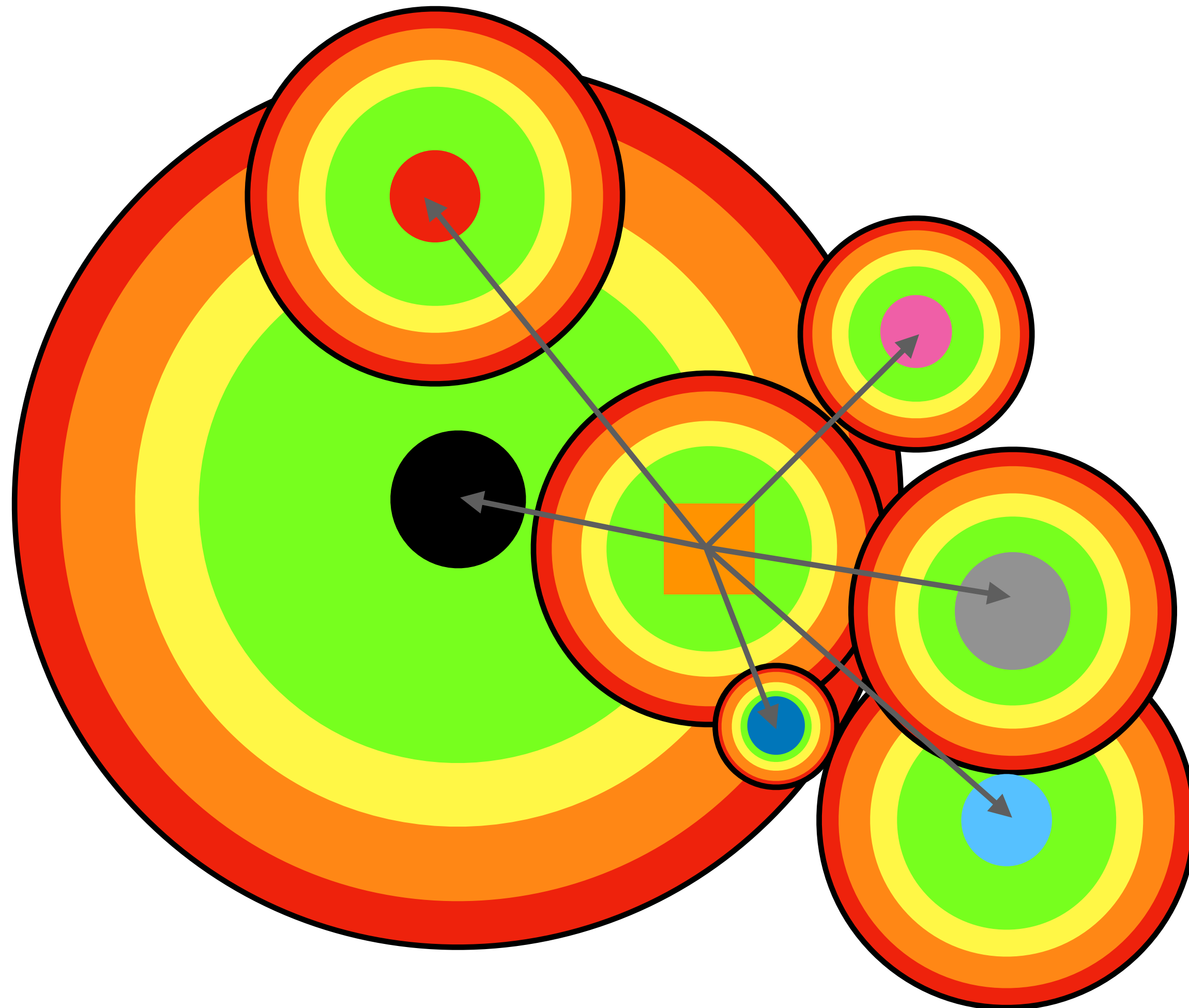


# The Rubin “Super-Match”

Bringing Independent Results together to Notify of Associations across Multiple catalogues

LSST -> *Gaia*, *WISE*, *VISTA*, *Euclid*, *SDSS*, ... matches

Quick and easy construction of spectral energy distributions for each LSST source  
Includes SED probabilities, individual match reliability, contamination statistics etc.



Wilson & Naylor (in prep.)  
Pineau et al. (2017)

<https://github.com/macauff/macauff>  
<https://github.com/macauff/birnam>

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LSST -> *Gaia*, *WISE*, *VISTA*, *Euclid*, *SDSS*, ... matches

Quick and easy construction of spectral energy distributions for each LSST source

Includes SED probabilities, individual match reliability, contamination statistics etc.

$$P(H_{\gamma\phi\rho}|D) = \frac{1}{K} N_{\gamma\phi} G_{\gamma\phi} N_{\gamma\rho} G_{\gamma\rho} = A_{\gamma\phi} A_{\gamma\rho},$$

$$P(H_{\gamma\phi\_ \rho}|D) = \frac{1}{K} N_{\gamma\phi} G_{\gamma\phi} N_{\gamma} N_{\rho} = B_{\gamma\phi} A_{\gamma\rho},$$

$$P(H_{\gamma\_ \phi\_ \rho}|D) = \frac{1}{K} N_{\gamma} N_{\phi} N_{\gamma} N_{\rho} = B_{\gamma\phi} B_{\gamma\rho},$$

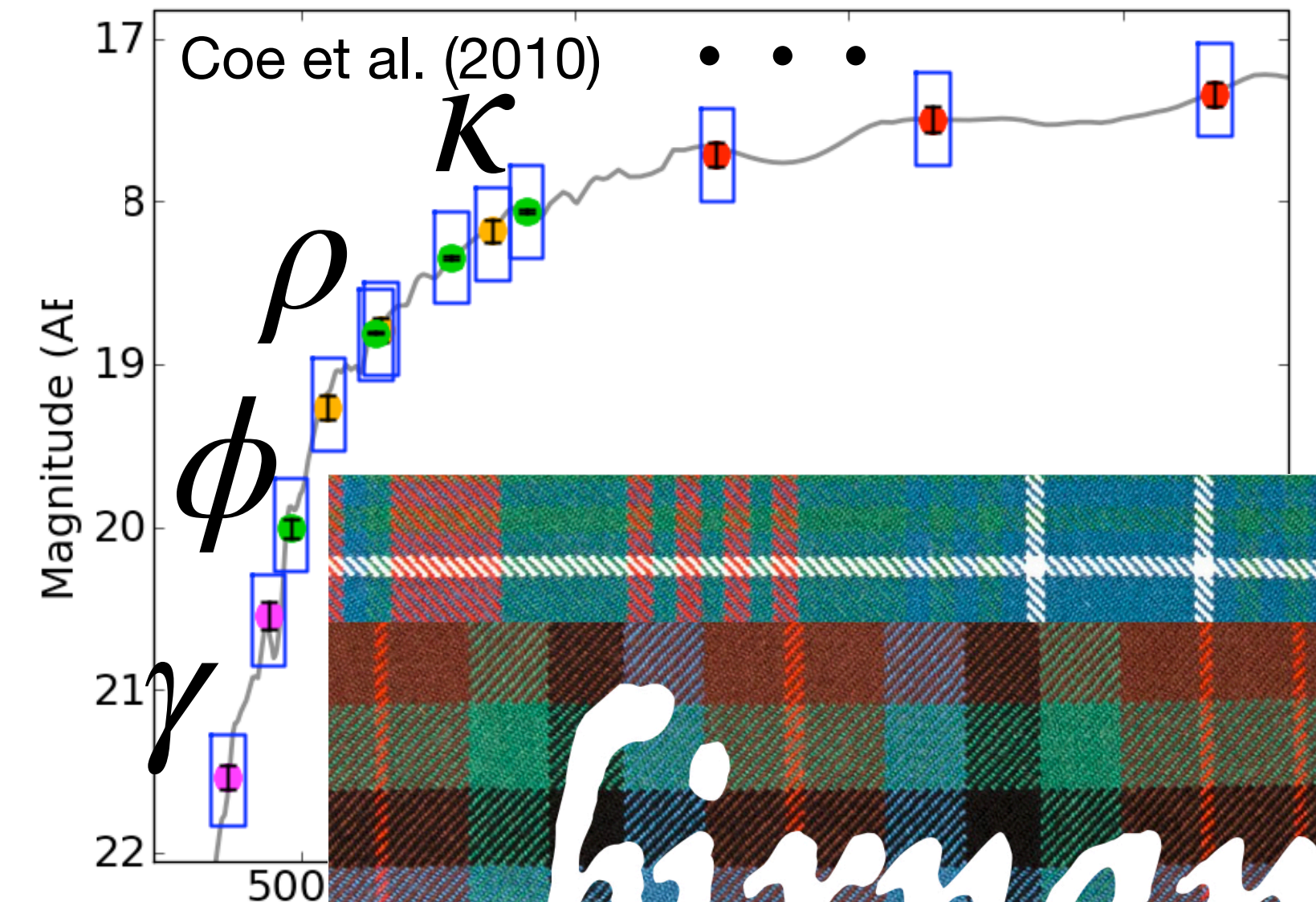
$$A_{\gamma\phi} = \frac{N_{\gamma\phi} G_{\gamma\phi}}{N_{\gamma} N_{\phi} + N_{\gamma\phi} G_{\gamma\phi}}$$

$$B_{\gamma\phi} = \frac{N_{\gamma} N_{\phi}}{N_{\gamma} N_{\phi} + N_{\gamma\phi} G_{\gamma\phi}}$$

Wilson & Naylor (2018a)

Wilson & Naylor (in prep.)

Pineau et al. (2017)



*birnam*

<https://github.com/macauff/macauff>

<https://github.com/macauff/birnam>

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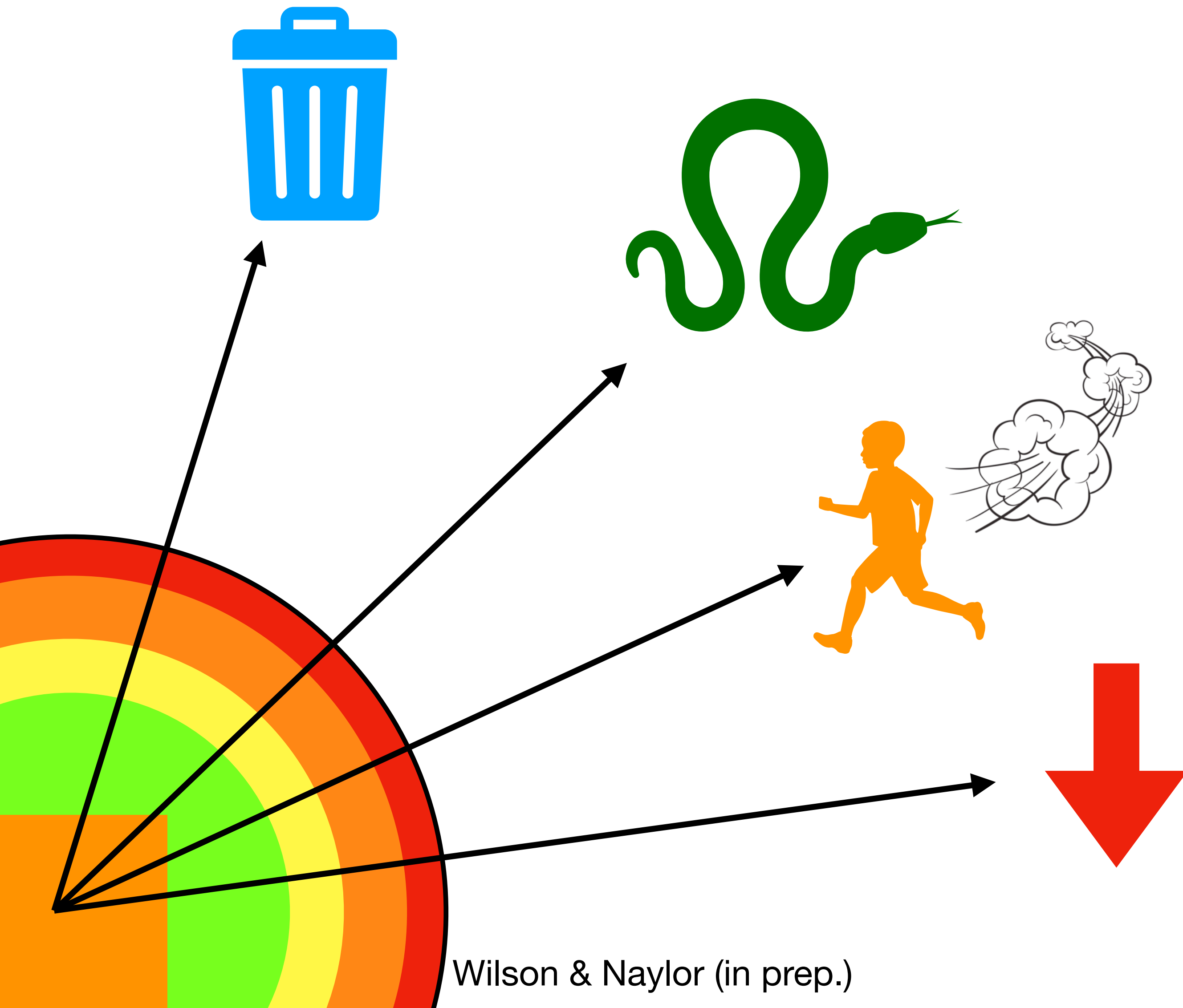


# Confirming Lonely Rubin Sources

Blanks And Near-misses, Questionable sources, Upper-limits, and Objects of varying brightness

Most LSST sources will be “lonely” with 15x as many sources as the next dataset. We will follow up all non-matches, and confirm whether these objects are:

- Image artefacts
- Astrophysically variable objects
- High proper motion sources
- Regular objects that are simply too faint to be seen in the opposing catalogue





# Confirming Lonely Rubin Sources

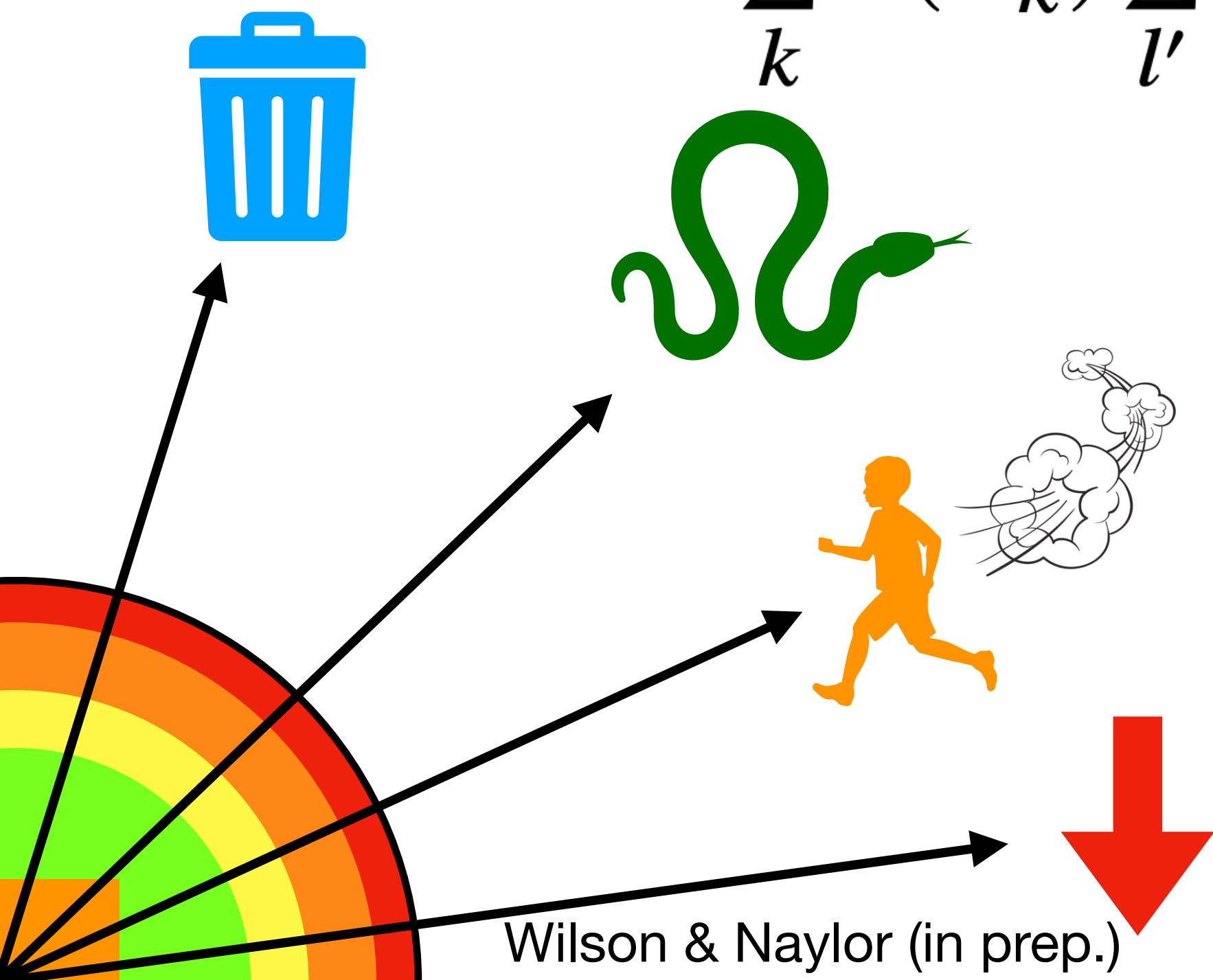
Blanks And Near-misses, Questionable sources, Upper-limits, and Objects of varying brightness

$$P(H_i, M_j | \mathbf{D}) = \frac{P(H_i)P(M_j|H_i)p(\mathbf{D}|H_i, M_j)}{p(\mathbf{D})}$$

$$P(H_i, M_j | \mathbf{D}) = \frac{P(H_i)L_j}{\sum_k P(H_k) \sum_{l'} L_{l'} + \sum_{k'} P(H_{k'})}$$

Most LSST sources will be “lonely” with 15x as many sources as the next dataset. We will follow up all non-matches, and confirm whether these objects are:

- Image artefacts
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$$L = \frac{Gc}{Nf}$$





# How To Use Our Cross-Matches

(Or, how this impacts you on a day-to-day basis)

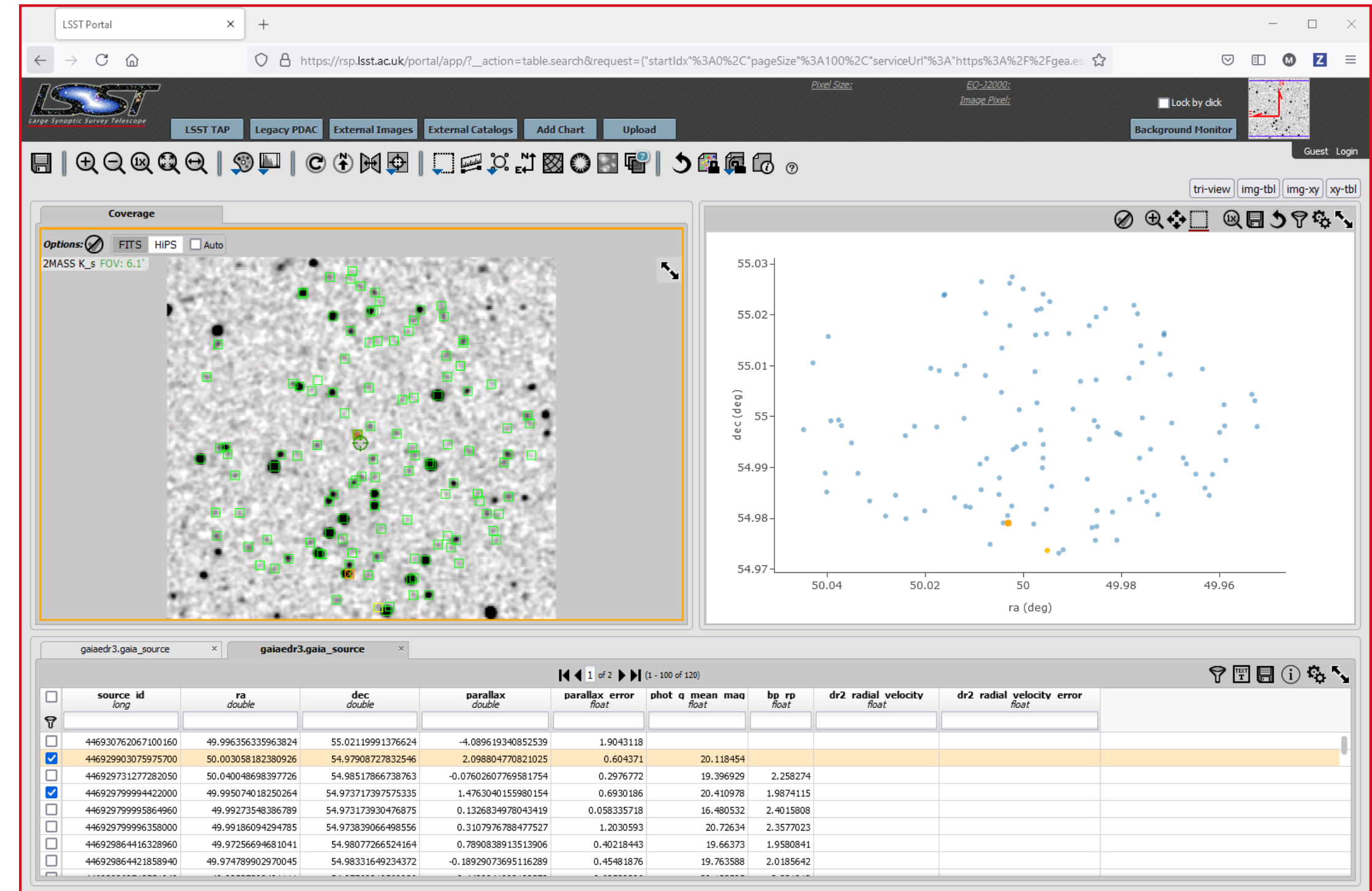


Three tables per cross-match: merged catalogue dataset, and 2x non-match dataset (one per catalogue)

## Example columns:

- Designations of the two sources (e.g., WISE J... and Gaia EDR3...)
- RA and Dec (or Galactic l/b) of the two sources
- Magnitudes (corrected for necessary effects, such as e.g. Gaia) in all bandpasses for both objects
- Match probability — probability of the most likely permutation (see equation 26 of Wilson & Naylor 2018a)
- Eta - Photometric likelihood ratio (counterpart vs non-match probability, just for brightnesses; see eq37 of WN18a)
- Xi - Astrometric likelihood ratio (just position match/non-match comparison; see eq38 of WN18a)
- Average contamination - simulated mean (percentile) brightening of the two sources, based on number density of catalogue
- Probability of sources having blended contaminant above e.g. 1% relative flux

We will provide two match runs per catalogue pair match: one with, and one without, the photometry considered, to allow for the recovery of sources with “weird” colours but otherwise agreeable astrometry





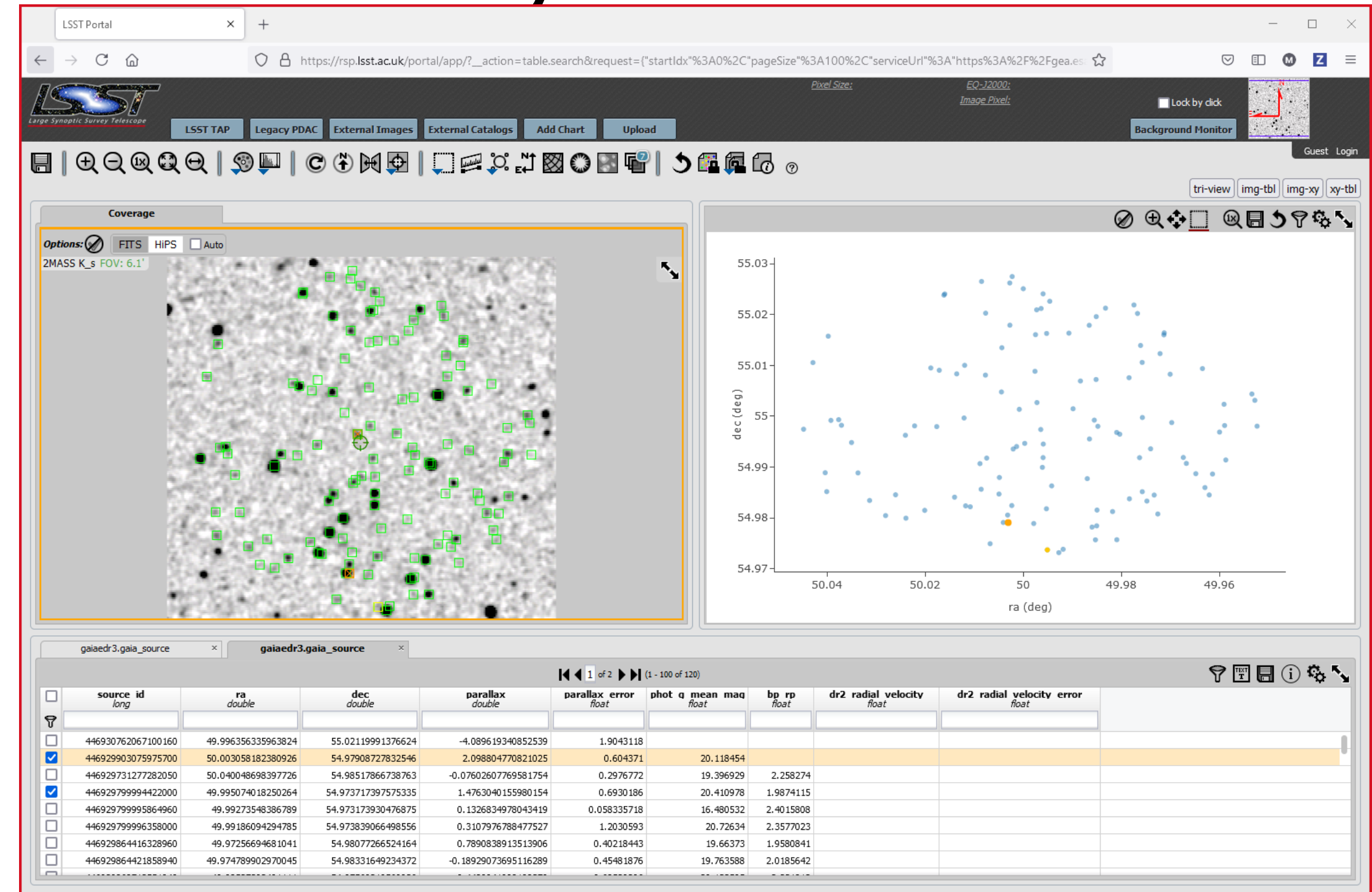
# How To Use Our Super- and Lonely-Matches

(Or, how this impacts you on a day-to-day basis)



Example columns:

- Designations of  $N$  sources (e.g., WISE J..., *Gaia* EDR3..., 2MASS J...)
- **Super-match probability** — probability of the given permutation



Example columns:

- Designations of the two sources (e.g., WISE J... and *Gaia* EDR3...)
- RA and Dec (or Galactic l/b) of the two sources
- Magnitudes in all bandpasses for both objects
- **Match probability** — different to that from a macauff cross-match!
- **Hypothesis of non-match** (proper motion, artifact, transient, ...)



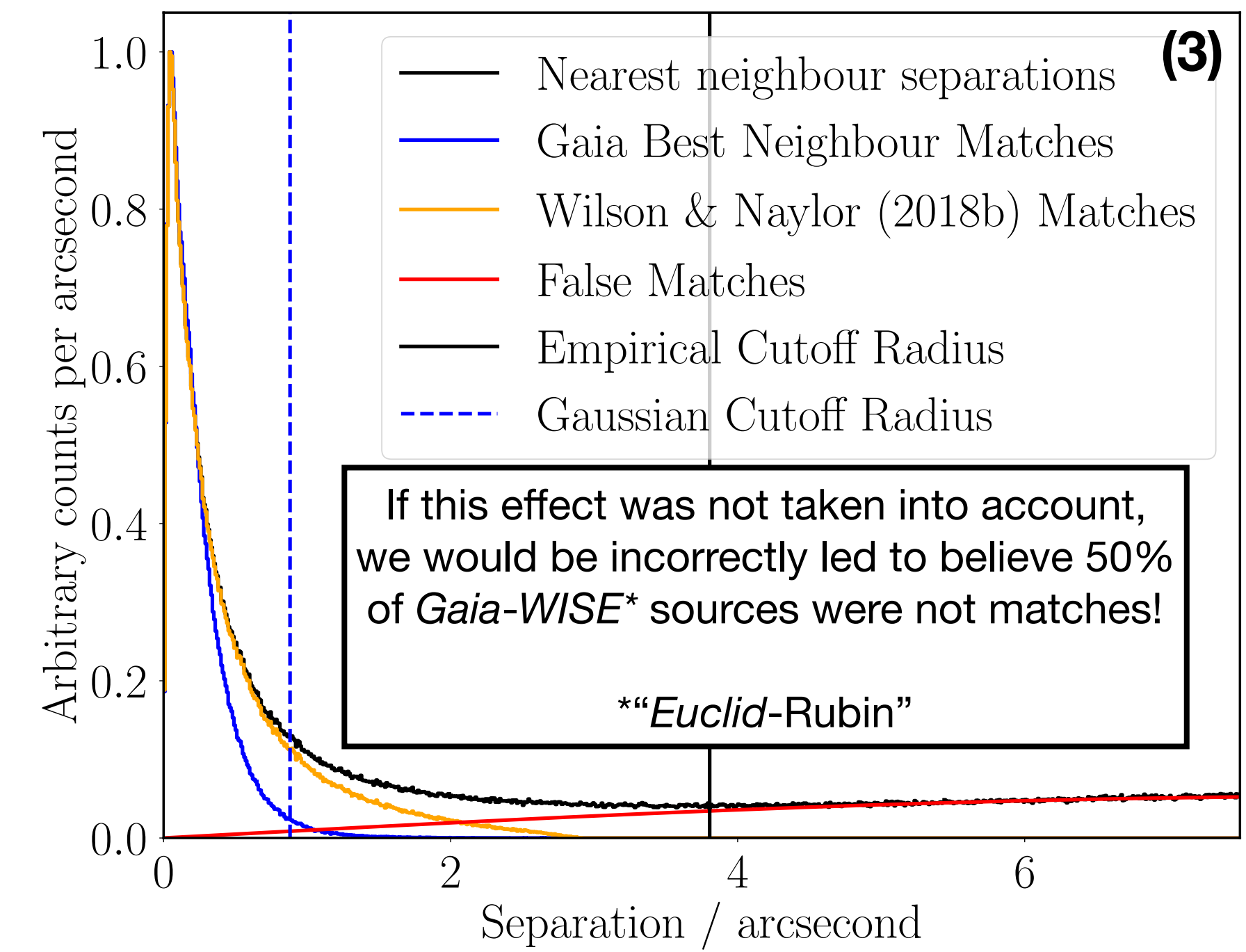
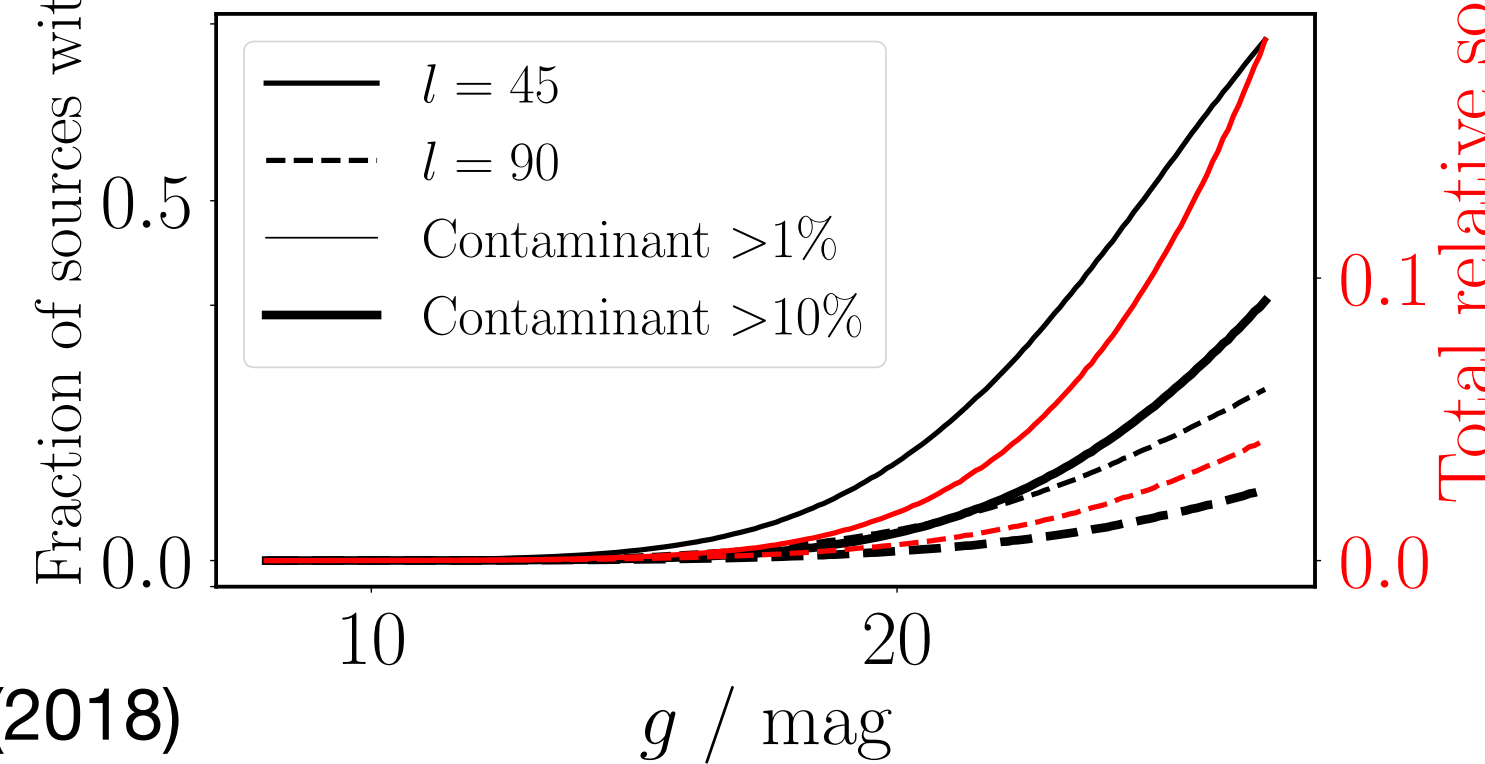
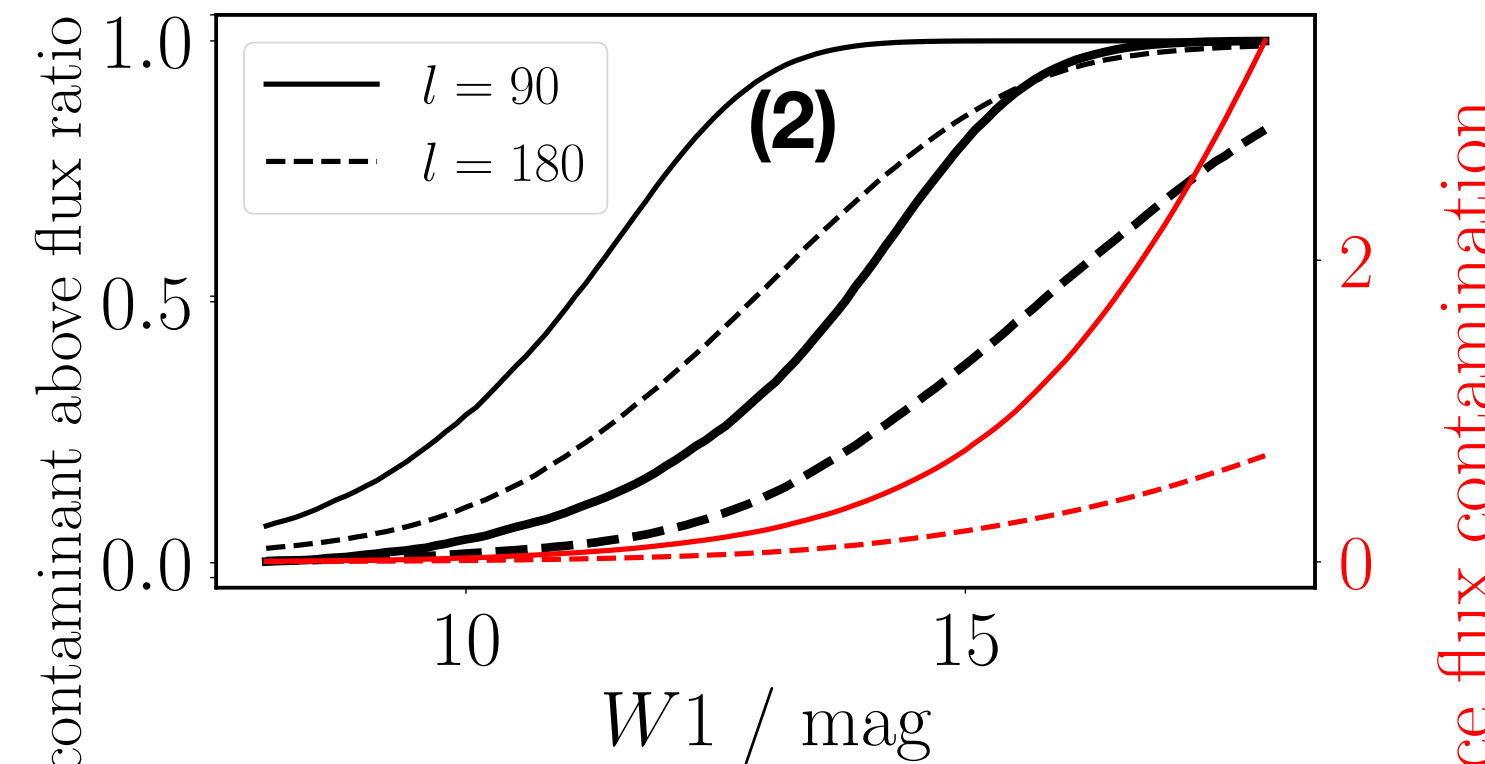
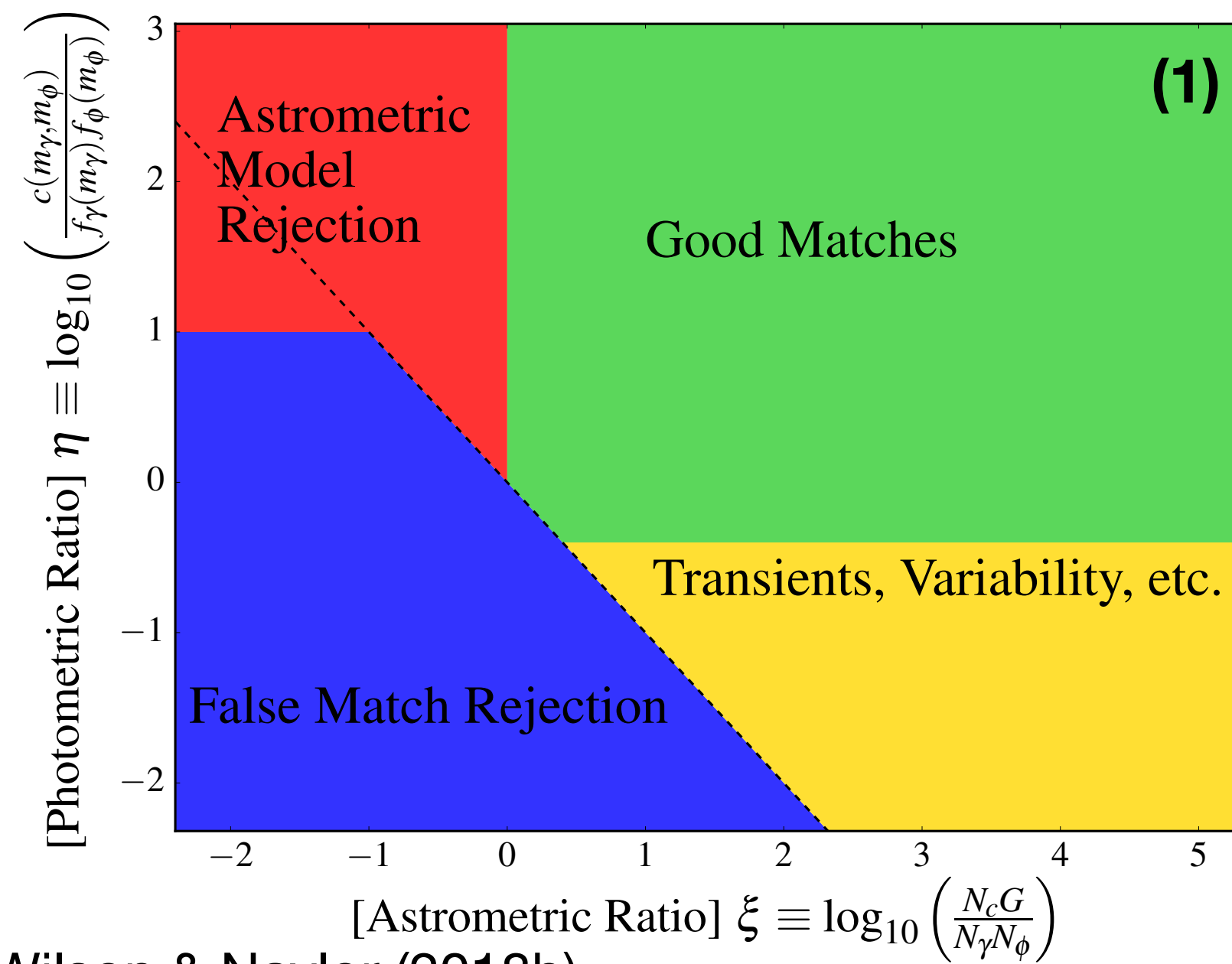
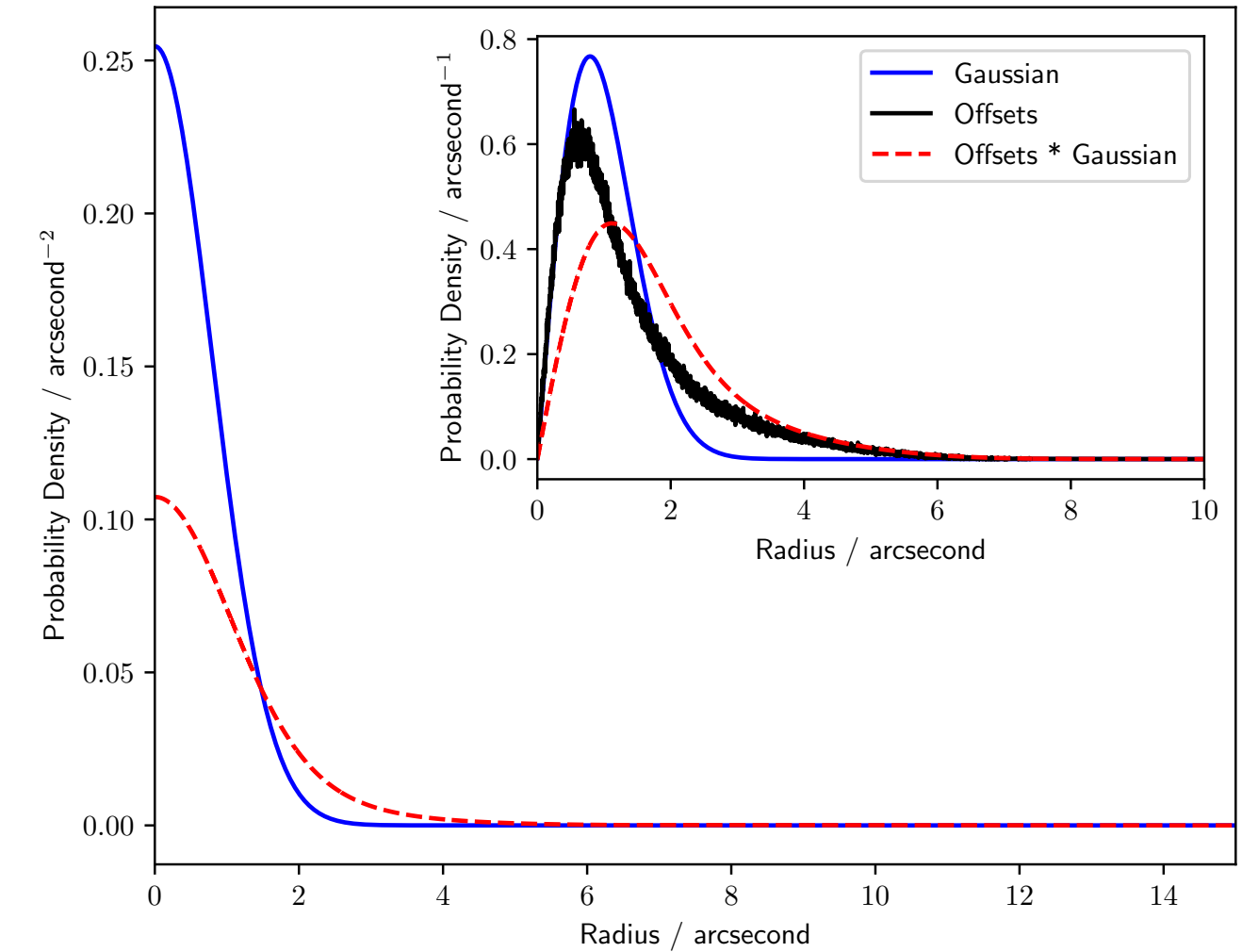
# Why Use Our Cross-Matches (and Extensions)?

0) Getting cross-matches, even for “well behaved” fields

1) Finding “odd” objects, either using the inclusion vs non-inclusion of the photometry in the two match runs, or via the likelihood ratio space – separately-planned “real time” matching service for transient objects

2) Removing e.g. IR excess or correcting for extinction-like crowding brightening, through Average Contamination; crucial for “1% photometry” in both precision *and* accuracy

3) Recovering additional sources missed by other match services – either in crowded fields (we recover up to twice as many *Gaia-WISE* matches than the *Gaia* best neighbour matches), or with our extension to unknown proper motion modelling as an extra systematic



Wilson & Naylor (2018b)  
*WISE* - Wright et al. (2010)  
*Gaia* matches - Marrese et al. (2019)  
*Gaia* DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

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# Conclusions

- **Upcoming LSST:UK cross-match service macauff** – let me know your thoughts/needs/hopes/dreams
  - **Provide tables of cross-matches between LSST and <your favourite catalogue here!>**
- **Our cross-matches include two key elements for avoiding issues with the crowded LSST sky**
  - **A generalised approach to the Astrometric Uncertainty Function allows for the inclusion of the effects of perturbation due to blended sources and unknown proper motions – reduce false -ves!**
  - **Use of the photometry of sources allows for the rejection of false matches (with >1 “extra” source per 2 arcsecond circle in most of the LSST sky) – reduce false +ves!**
- **Will include additional information on the crowding of sources, allowing for selection of uncontaminated objects, or modelling of excess flux – crucial for removal of red excess in SEDs**
  - **LSST will suffer of order 10% flux contamination, which could be confused with extinction**
- **macauff cross-match tools are being extended currently**
  - **We will provide an easy-to-use “SED grabber” tool for each LSST source**
  - **And follow up the ~93% of non-matched Rubin objects to confirm flux upper limits in other surveys**



Wilson & Naylor, 2017, MNRAS, 468, 2517  
Wilson & Naylor, 2018a, MNRAS, 473, 5570  
Wilson & Naylor, 2018b, MNRAS, 481, 2148  
Wilson, 2022, RNAAS, 6, 60  
Wilson, 2023, RASTI, 2, 1



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<https://github.com/macauff/macauff>

Tom J Wilson @onoddil



