Enabling Cool Rubin Science with Robust Cross-Matches in the Faint, Crowded LSST Sky

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2024 RUBIN SOLAR NEIGHBORHOOD ULTRACOOL DWARFS MEETING - 26/JAN/24

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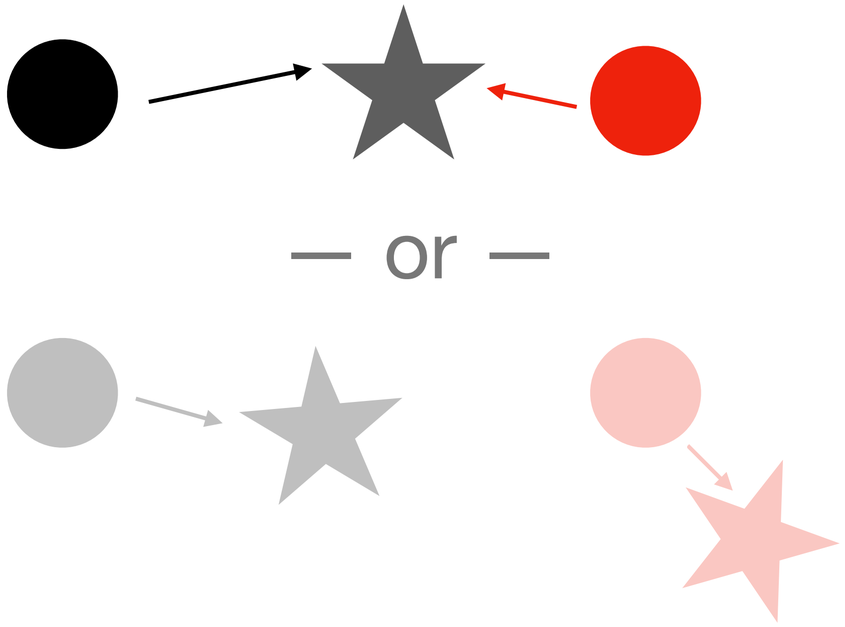
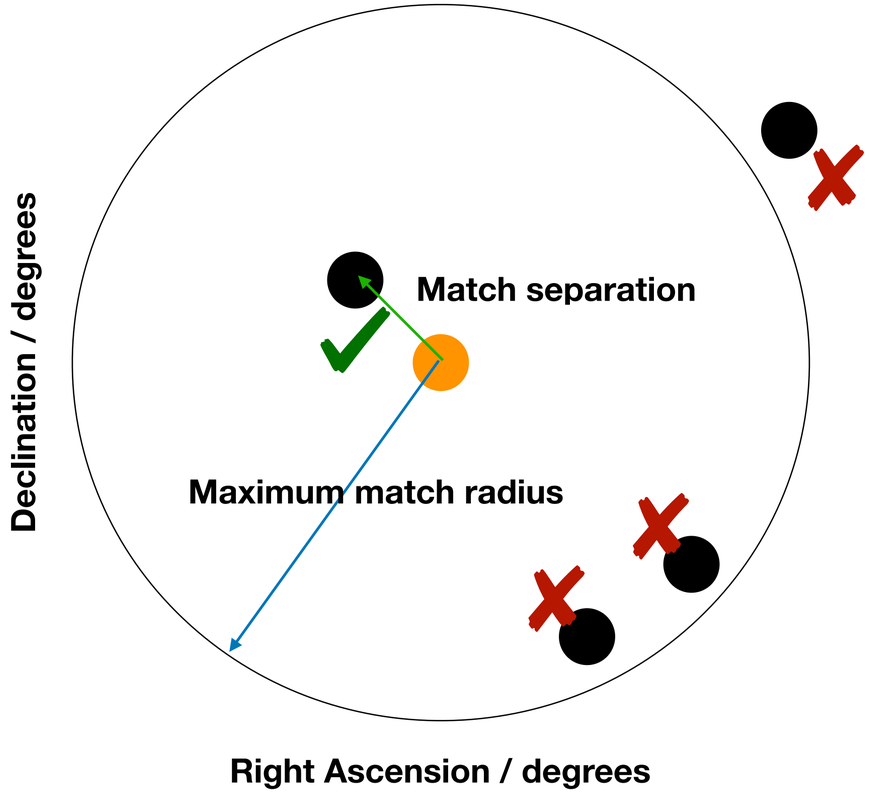
University of Exeter

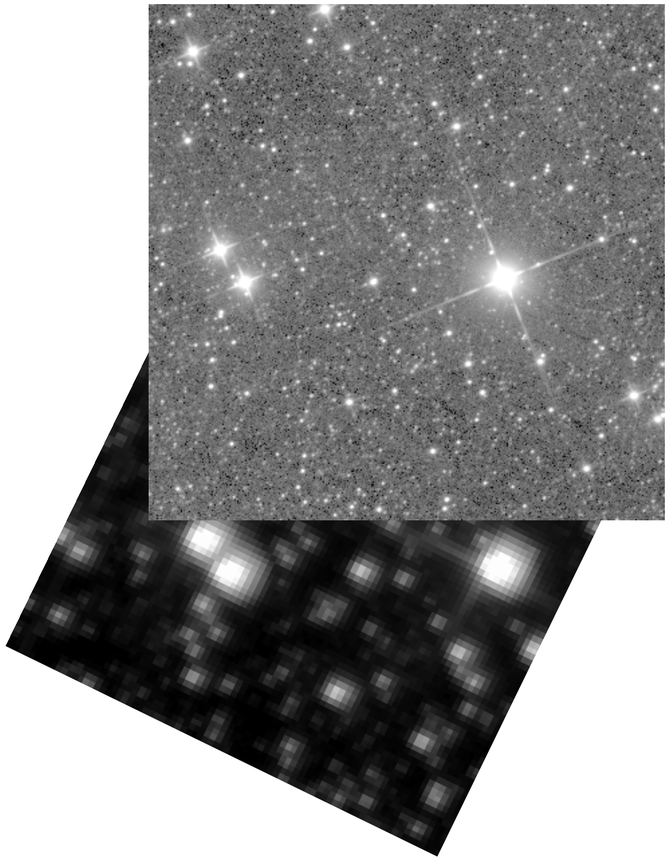
LSST:UK Consortium

Science and Technology Facilities Council

“Simple” Cross-Matching







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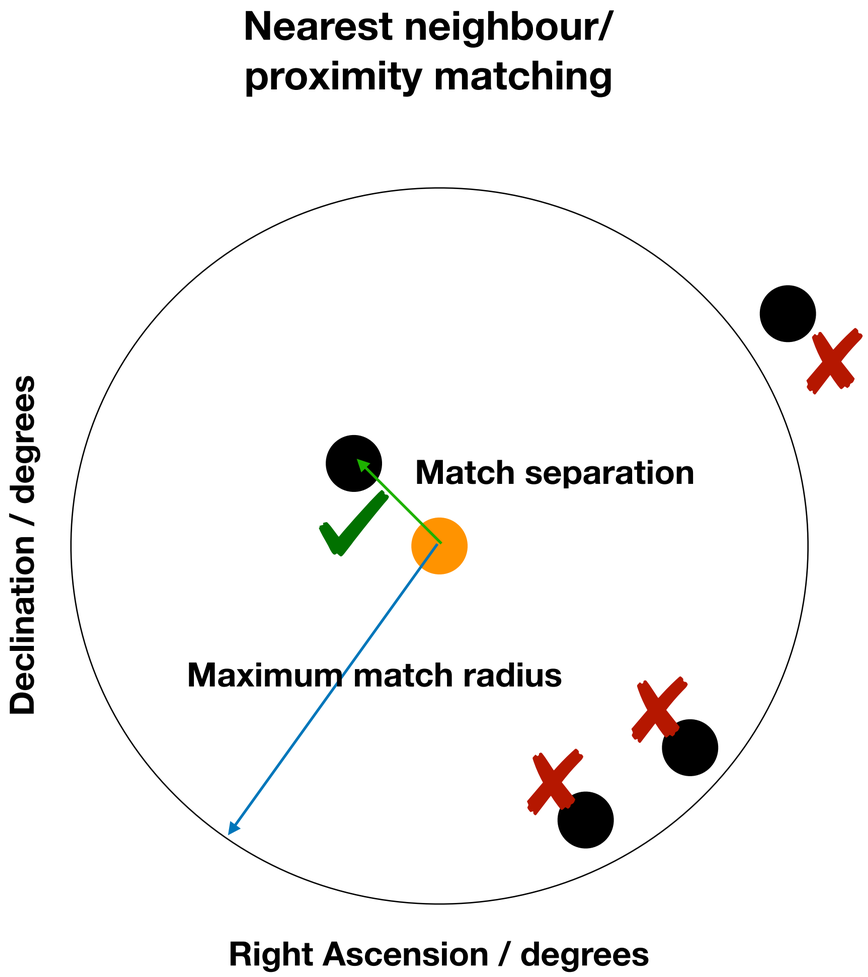
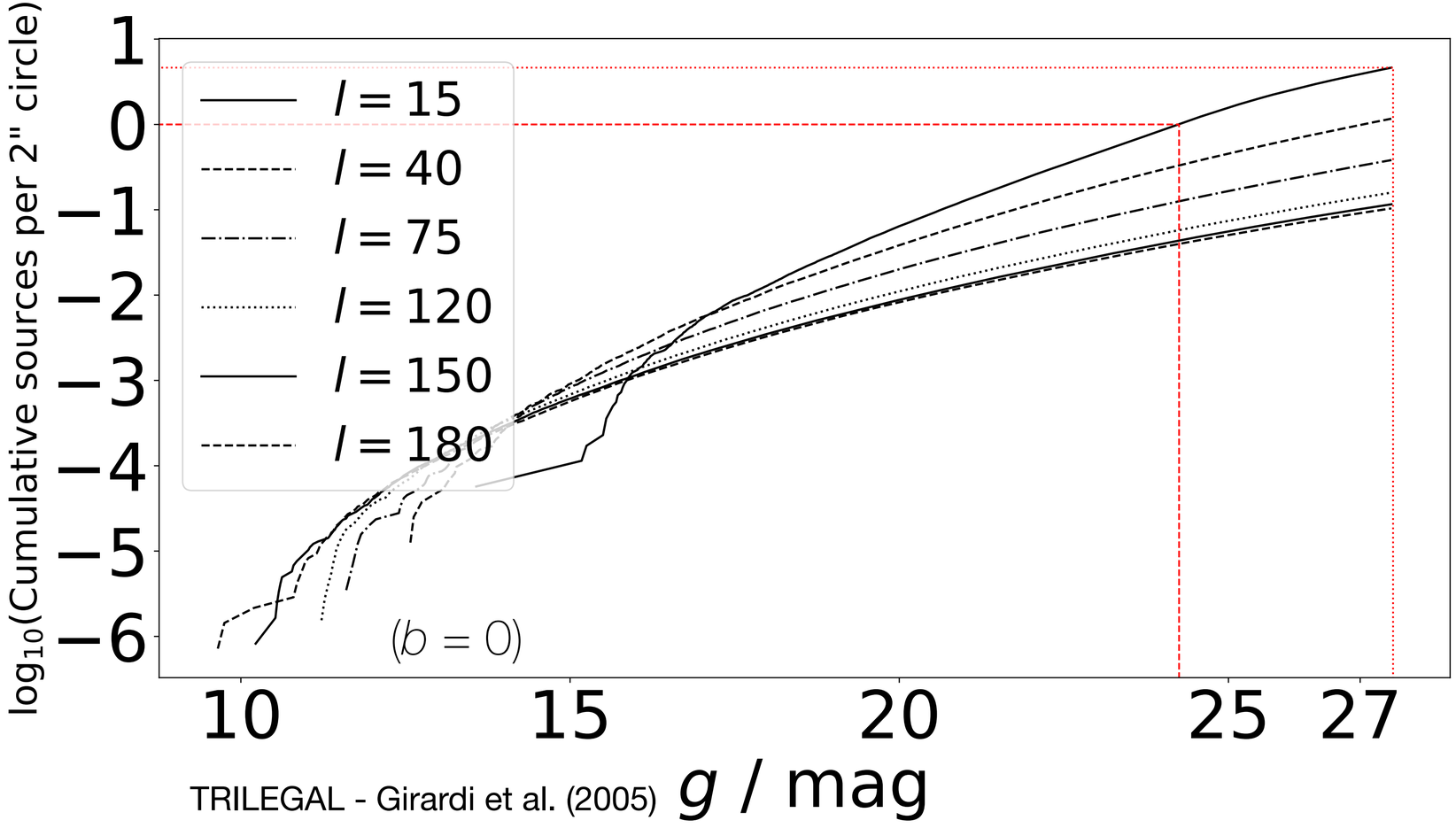
The Problem With LSST





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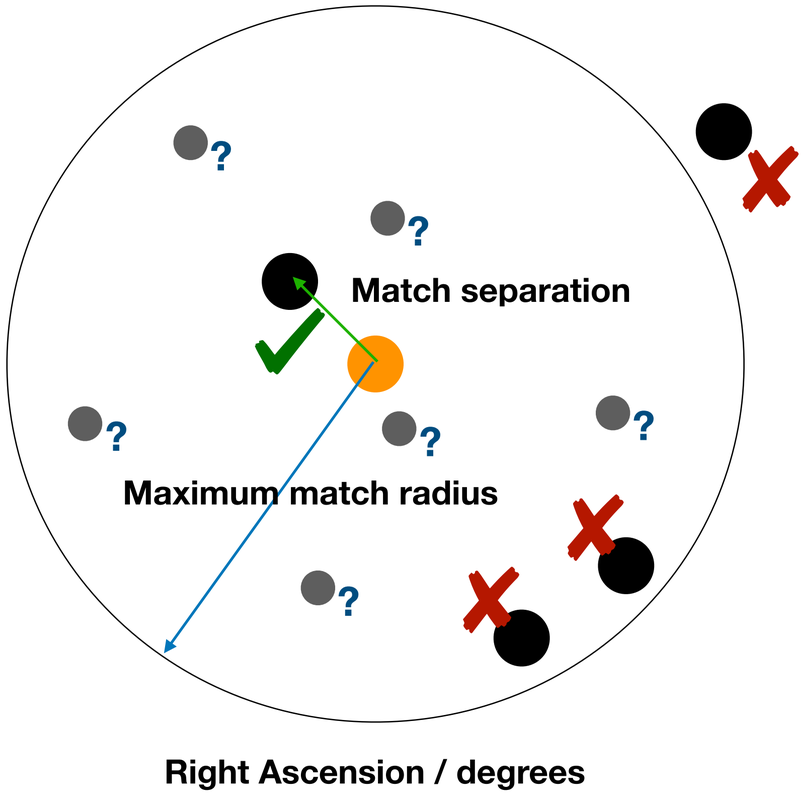
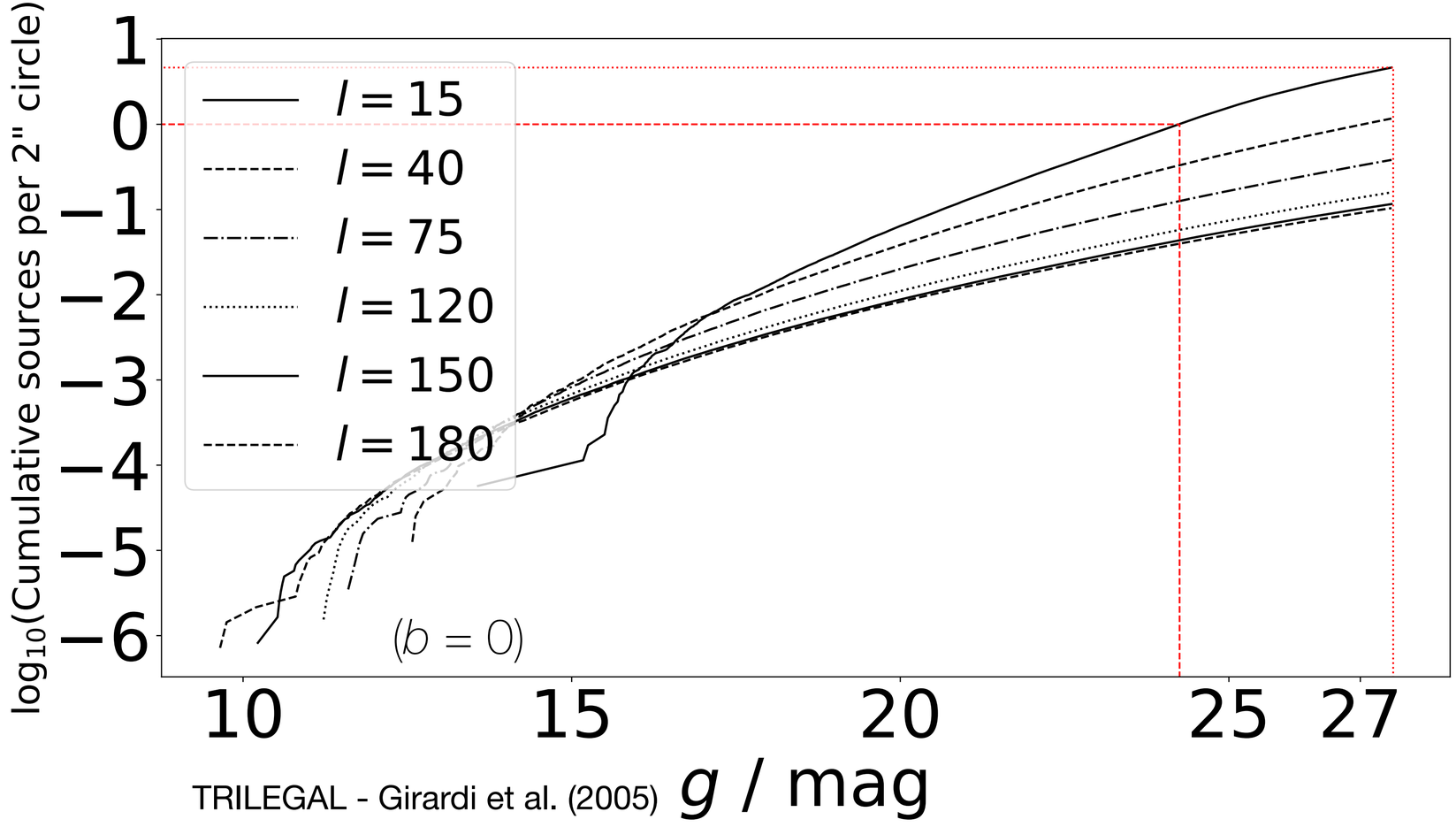
The Problem With LSST

(It's still a few randomly placed objects in every match radius at high Galactic latitudes)

Nearest neighbour/ proximity matching





Nearest-neighbour matching *will not* work in the era of Rubin!

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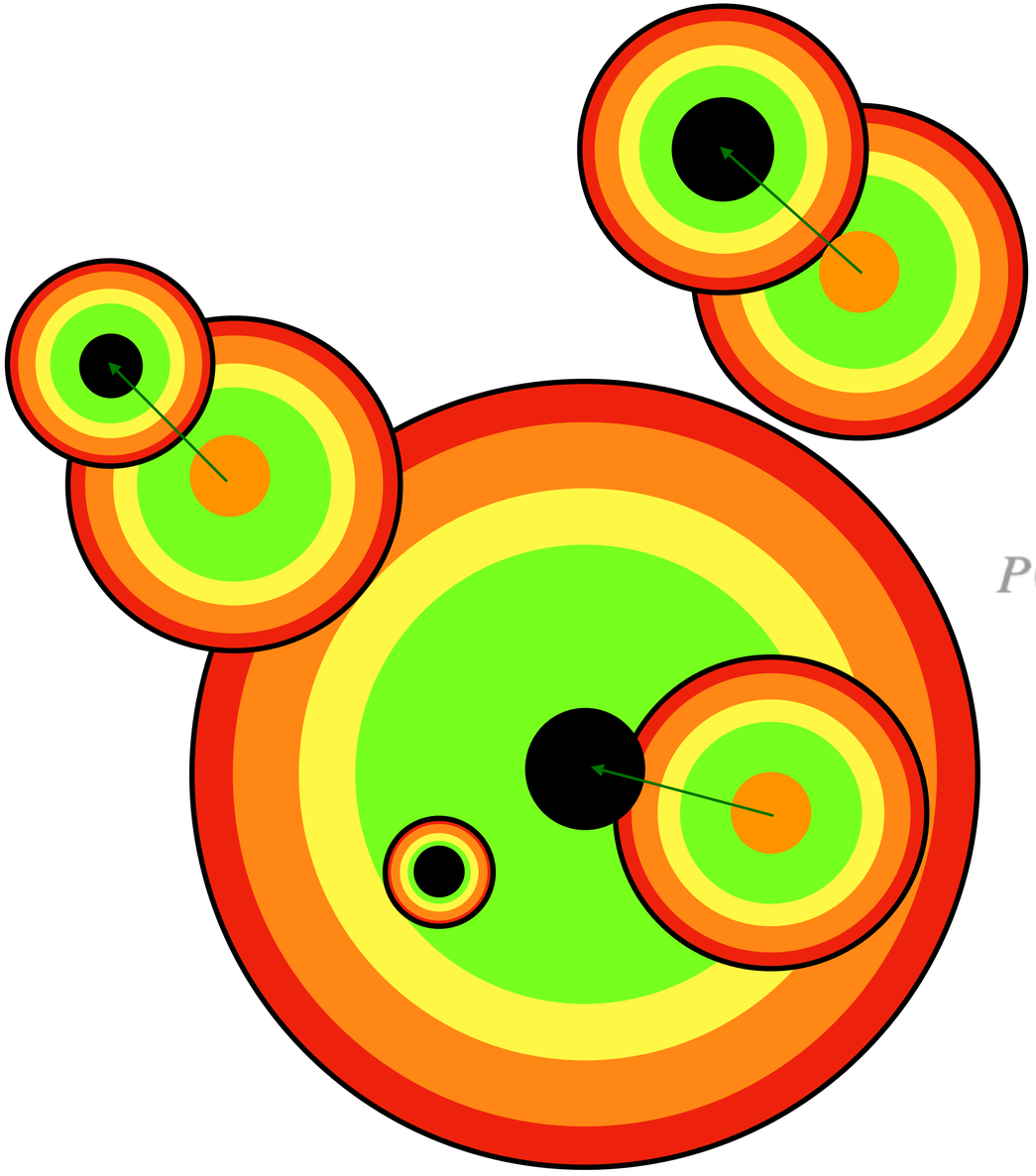
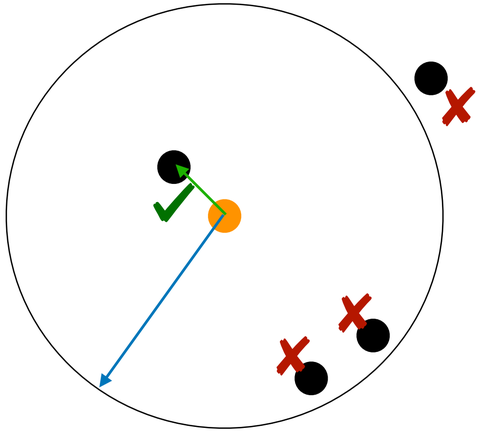
Probabilistic Cross-Matching





Probability of two sources having their <u>on-sky separation</u> given the hypothesis they are counterparts

$$P(\zeta, \lambda, k|\gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \delta \in \gamma} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \omega \in \phi} N_\phi f_\phi^\omega \prod_{i=1}^{k} N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$

Wilson & Naylor (2018a)

Probability of sources having their <u>brightnesses</u> given they are unrelated to one another (“field stars”)

Probability of sources having their <u>brightnesses</u> given they are counterparts

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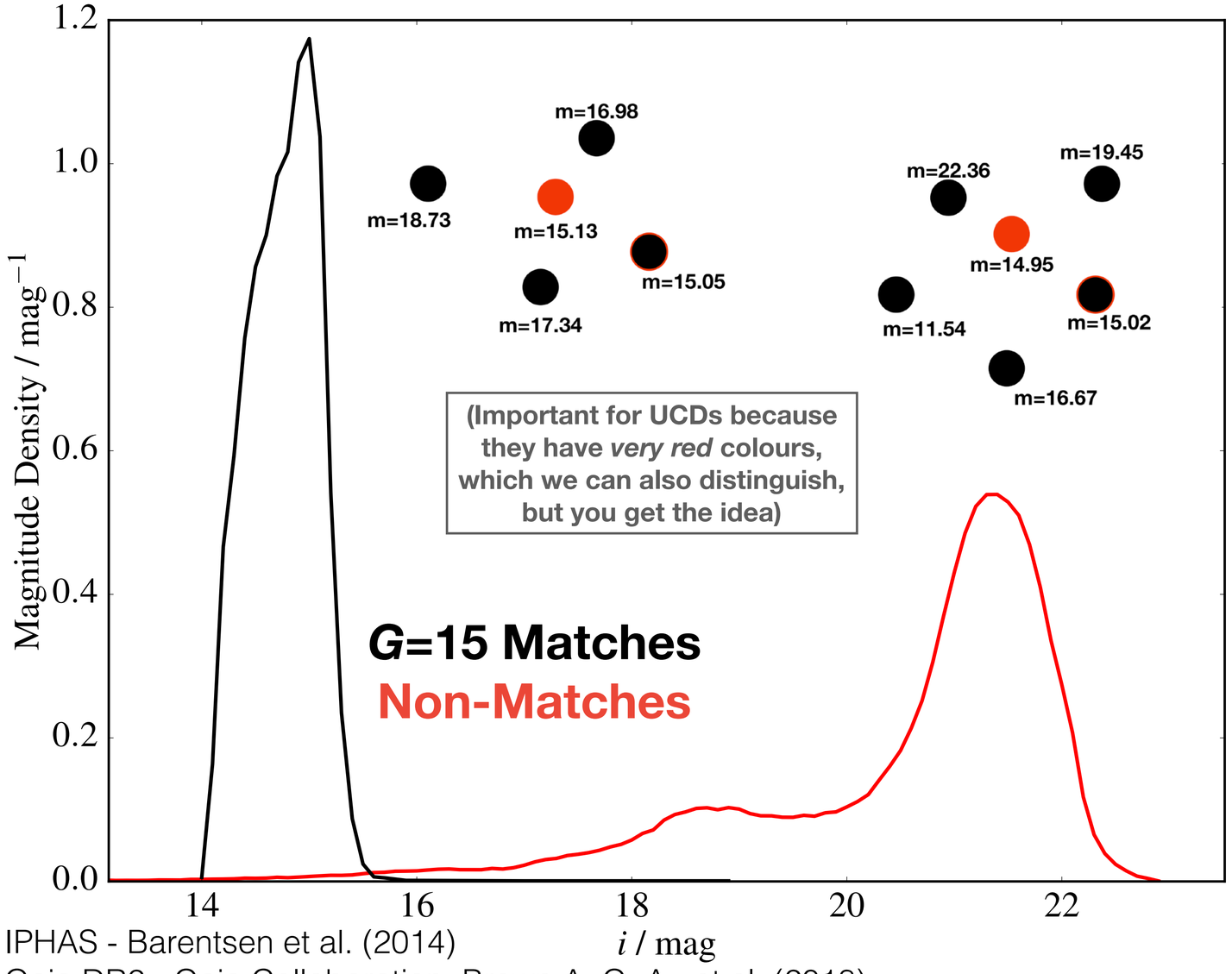
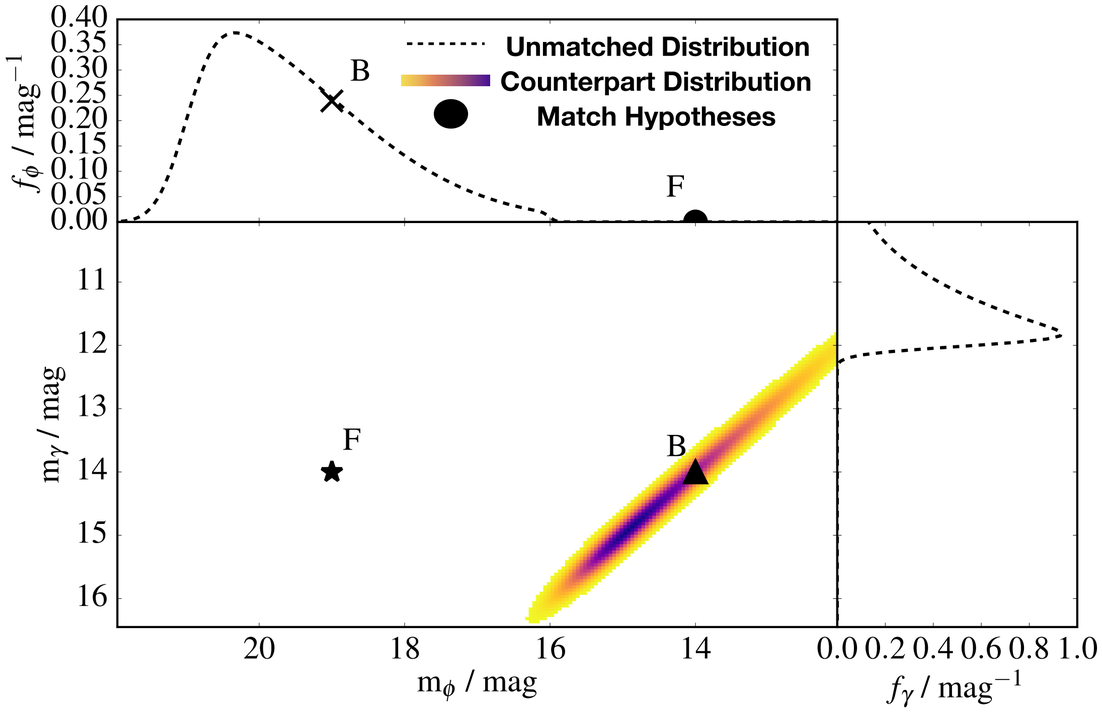
Including Magnitude Information: Rejecting False Positives

$$P(\zeta, \lambda, k|\gamma, \phi) = \frac{1}{K} \times \prod_{\delta \notin \zeta \cap \delta \in \gamma} N_\gamma f_\gamma^\delta \prod_{\omega \notin \lambda \cap \omega \in \phi} N_\phi f_\phi^\omega \prod_{i=1}^{k} N_c G_{\gamma\phi}^{\zeta_i \lambda_i} c_{\gamma\phi}^{\zeta_i \lambda_i}$$



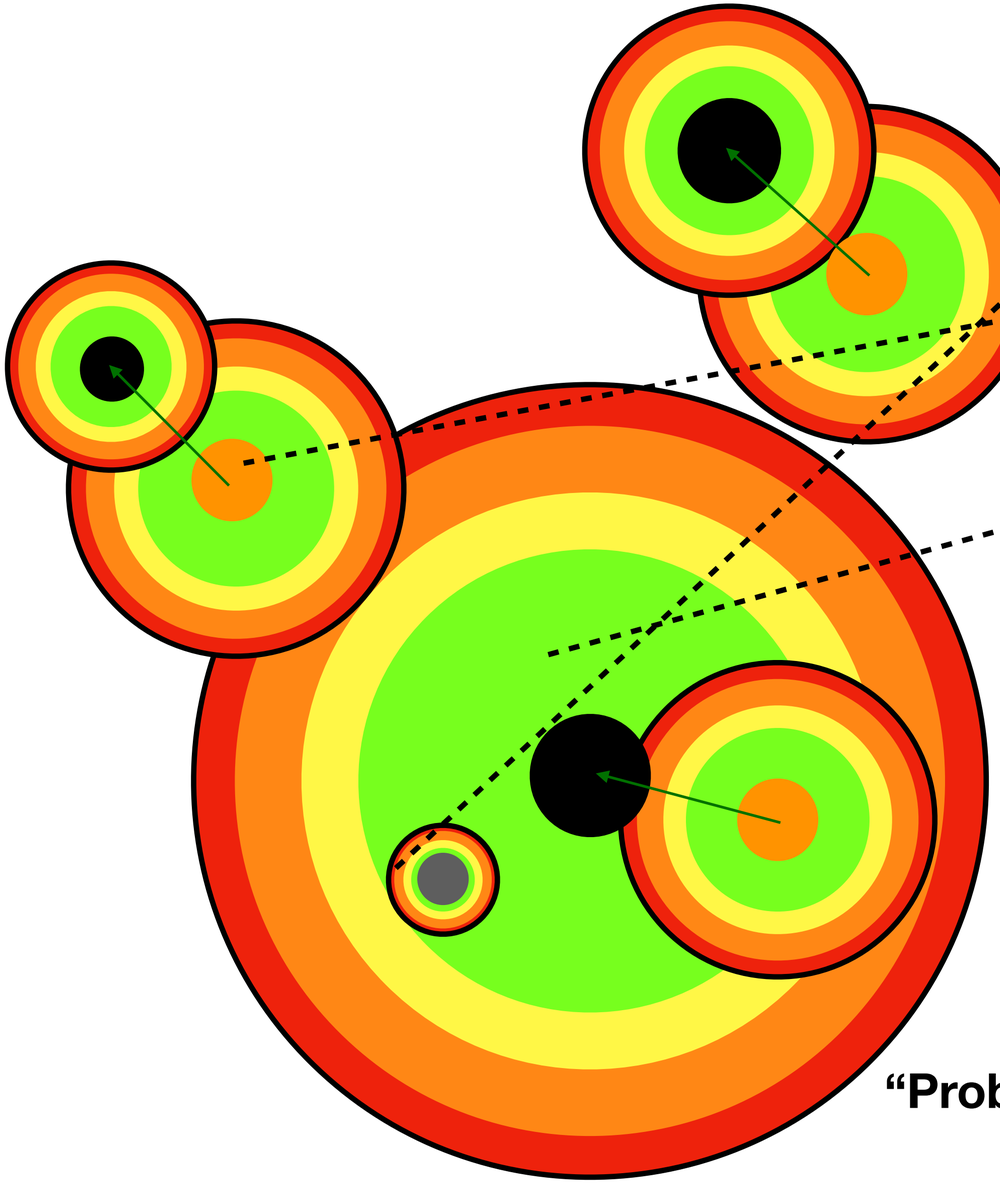
IPHAS - Barentsen et al. (2014)
Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

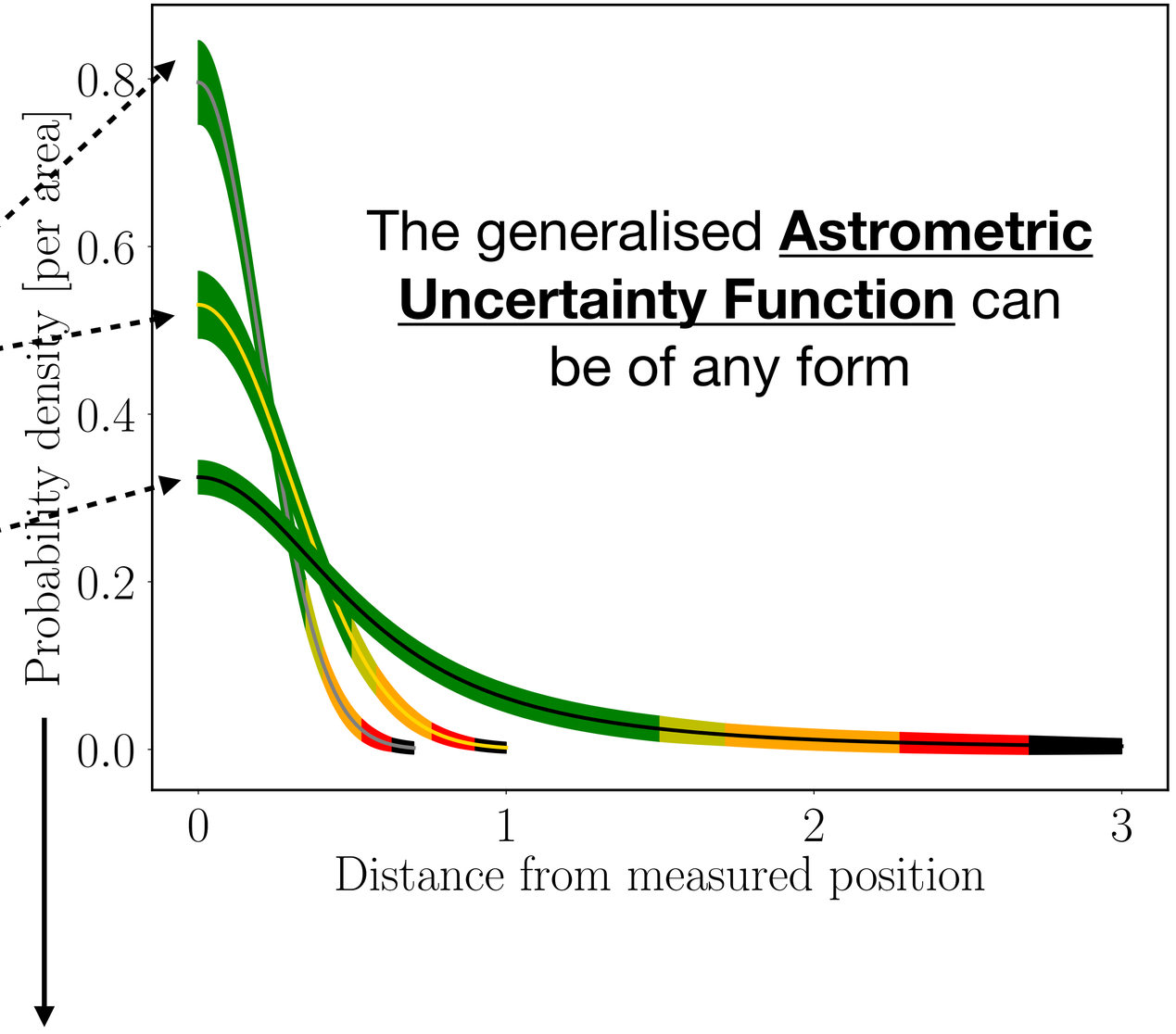


Wilson & Naylor (2018a)

The photometry-based likelihoods (c and f) allow us to mitigate high false positive rate in crowded fields, but now we need the position-based likelihood G

Probabilistic Cross-Matching: the AUF





The generalised **Astrometric Uncertainty Function** can be of any form

"Probability of True Position being this far from the Measured Position"

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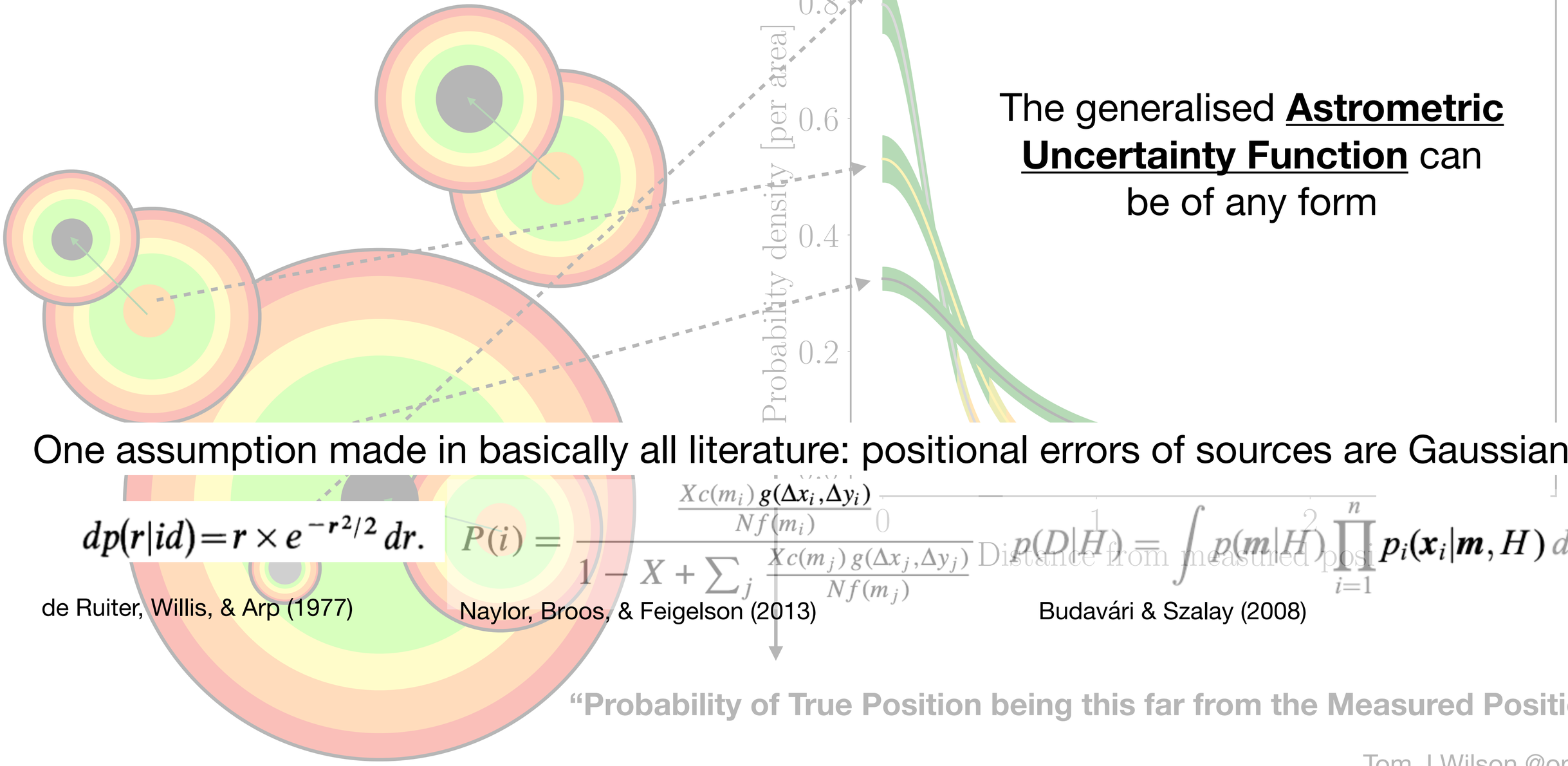
Probabilistic Cross-Matching: the AUF



The generalised **Astrometric Uncertainty Function** can be of any form

One assumption made in basically all literature: positional errors of sources are Gaussian!

$$dp(r|id) = r \times e^{-r^2/2}\, dr.$$

de Ruiter, Willis, & Arp (1977)

$$P(i) = \frac{\frac{Xc(m_i)\, g(\Delta x_i, \Delta y_i)}{Nf(m_i)}}{1 - X + \sum_j \frac{Xc(m_j)\, g(\Delta x_j, \Delta y_j)}{Nf(m_j)}}$$

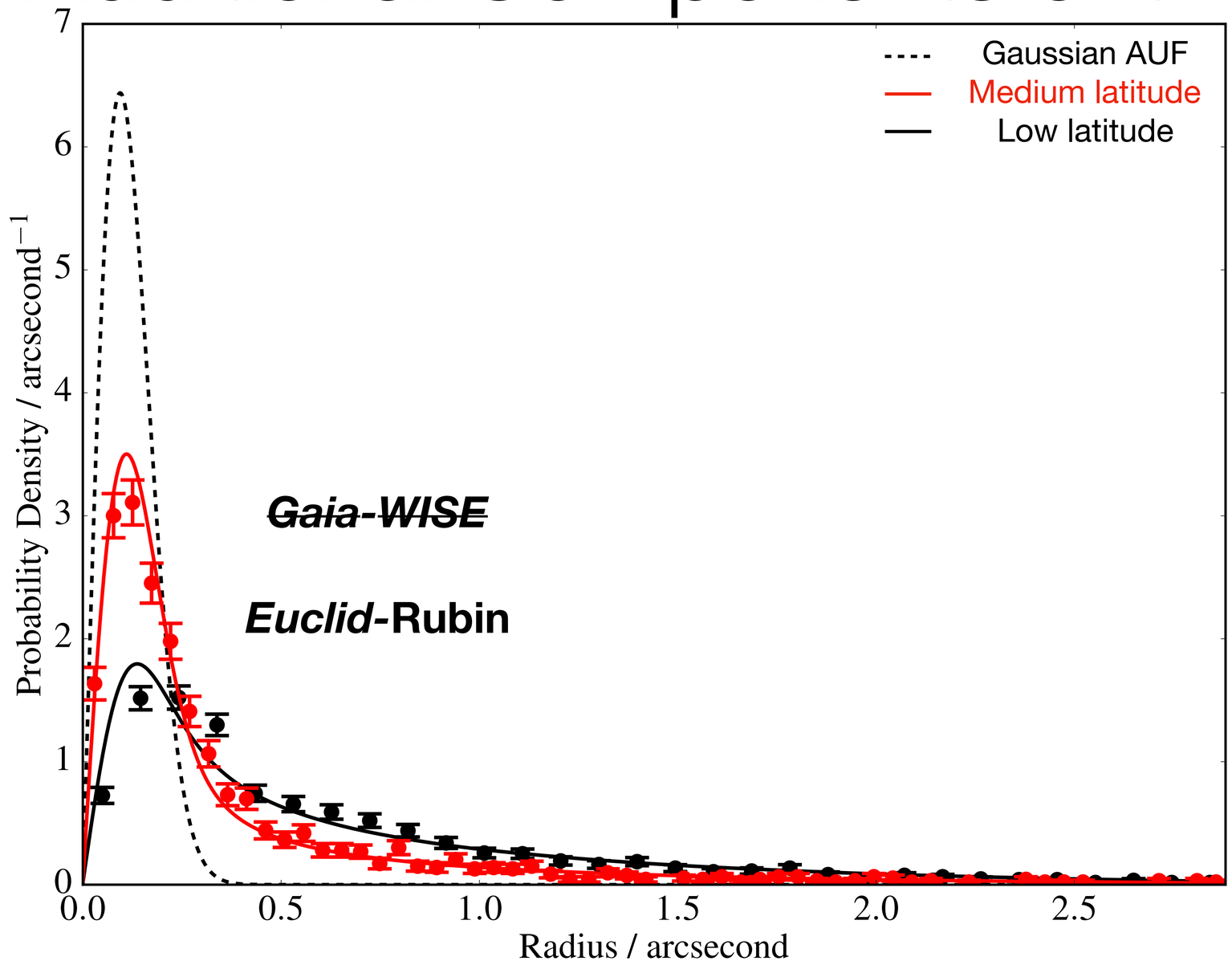
Naylor, Broos, & Feigelson (2013)

$$p(D|H) = \int p(\boldsymbol{m}|H) \prod_{i=1}^{n} p_i(\boldsymbol{x}_i|\boldsymbol{m}, H)\, d^3m$$

Budavári & Szalay (2008)

"Probability of True Position being this far from the Measured Position"

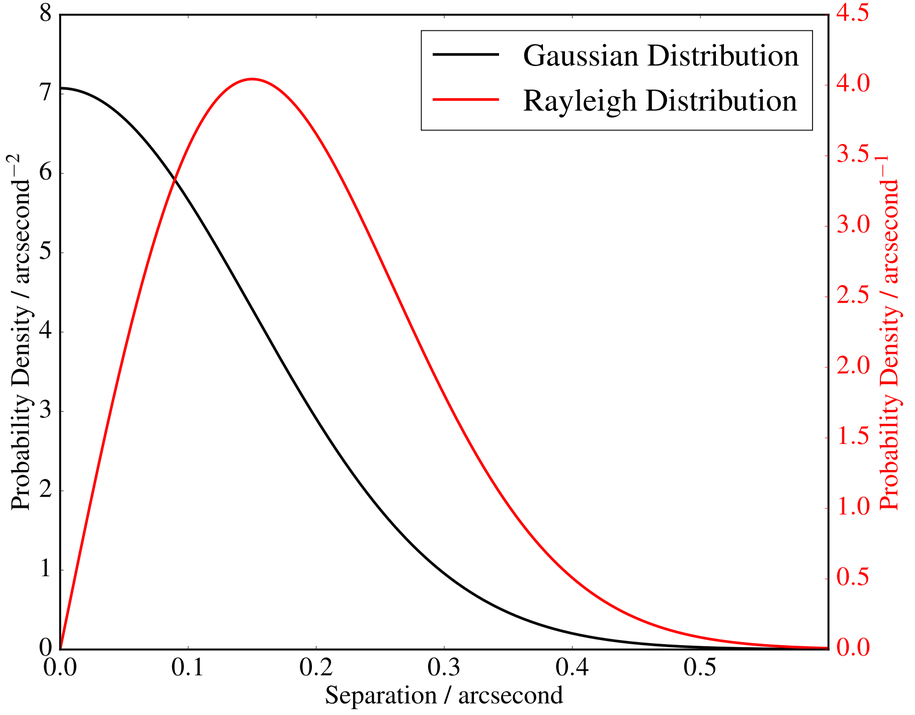
Additional Components of the AUF



$$g(x, y, \sigma) = (2\pi\sigma^2)^{-1}\exp\left(-\frac{1}{2}\frac{x^2+y^2}{\sigma^2}\right)$$

$$\downarrow$$

$$g(r, \sigma) = \frac{r}{\sigma^2}\exp\left(-\frac{1}{2}\frac{r^2}{\sigma^2}\right)$$



WISE - Wright et al. (2010)
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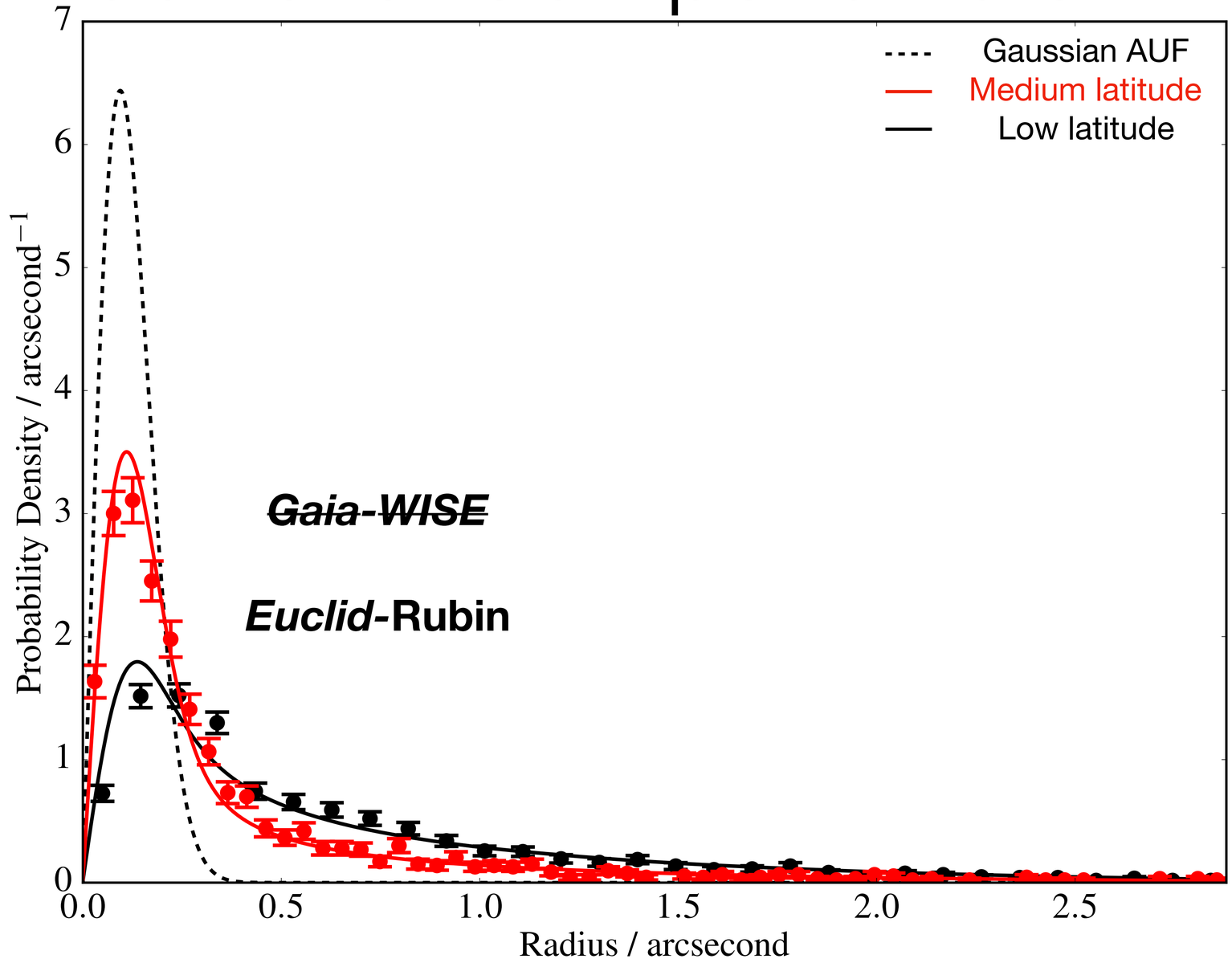

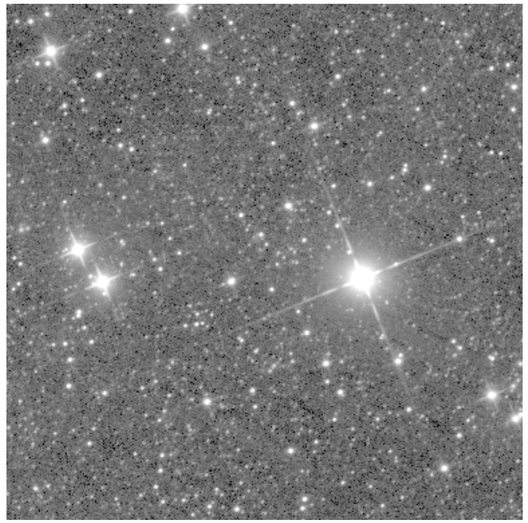

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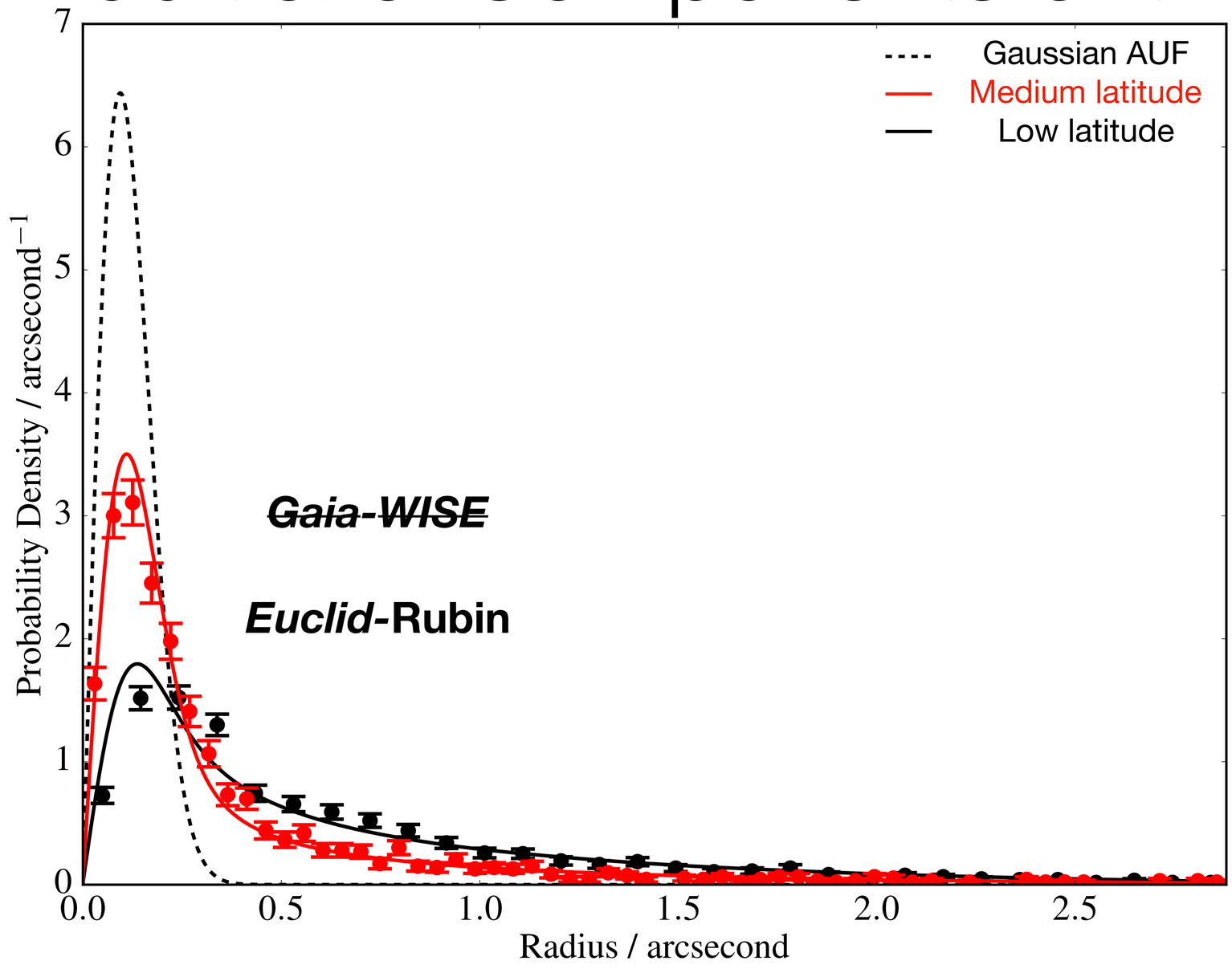
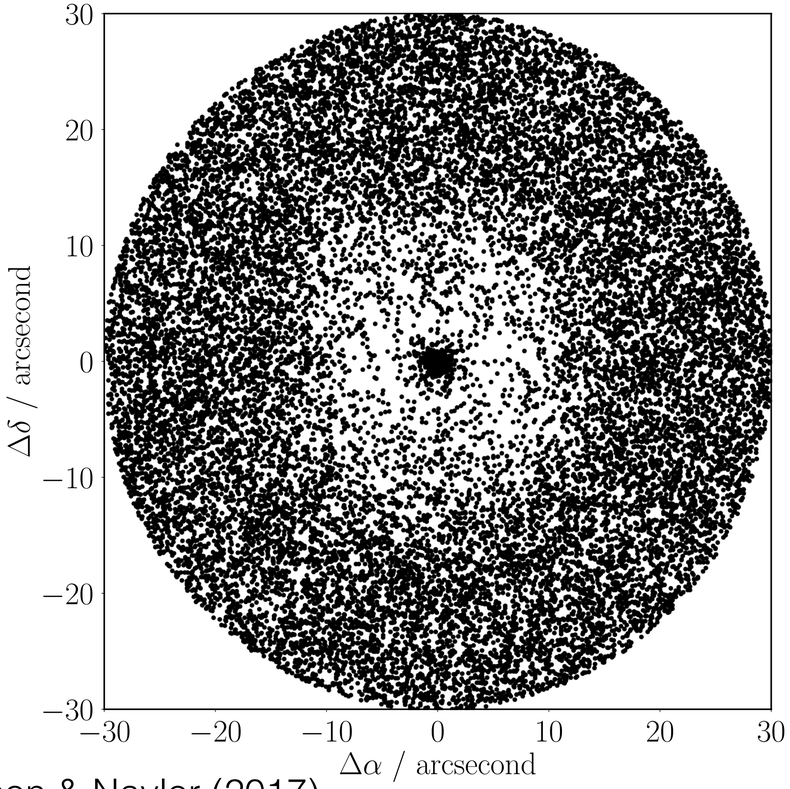
Additional Components of the AUF

(and any other systematic — e.g. proper motions, cf. Wilson 2023, RASTI)





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Wilson & Naylor (2017)

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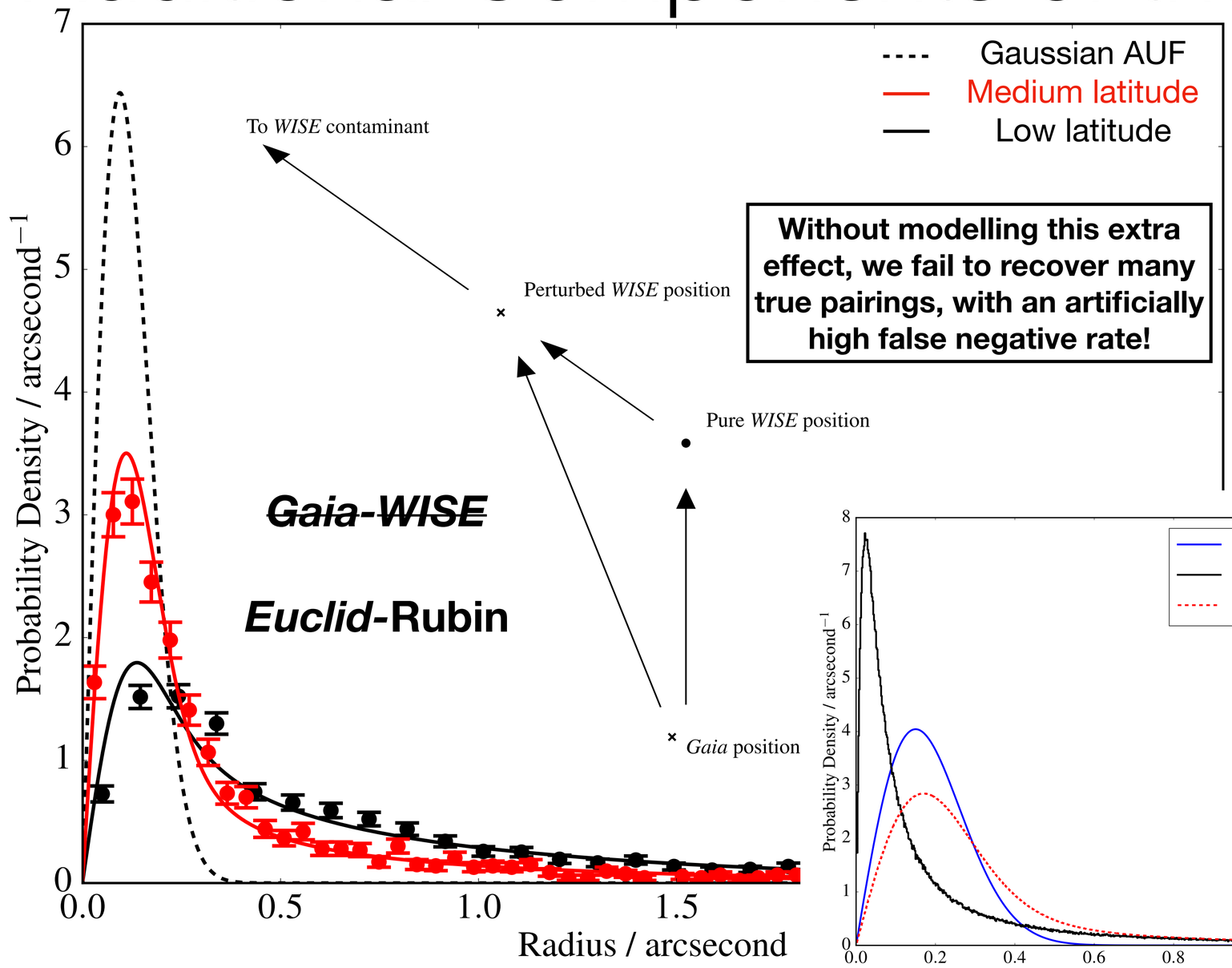
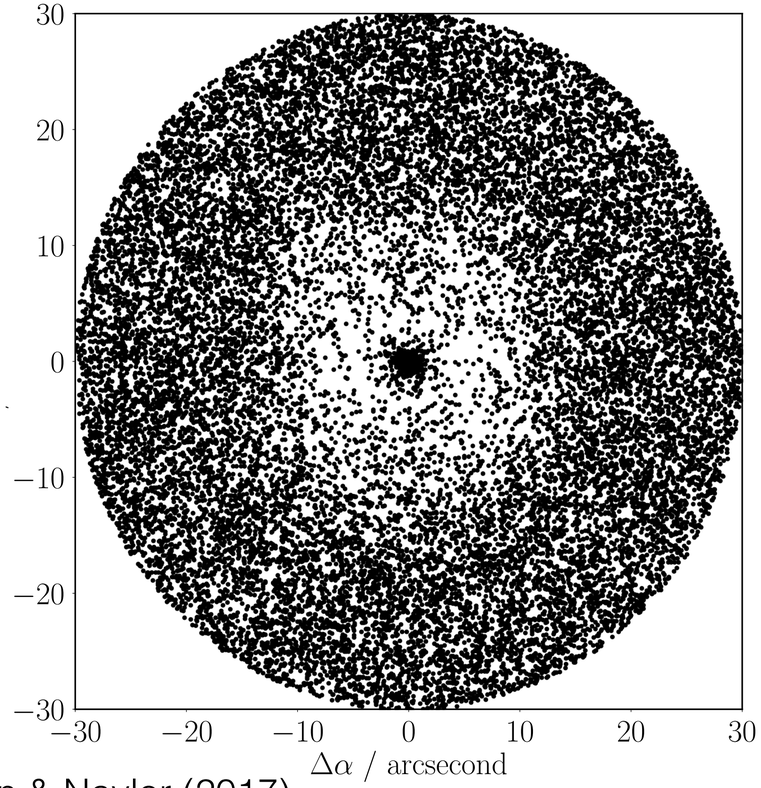


Without modelling this extra effect, we fail to recover many true pairings, with an artificially high false negative rate!



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Wilson & Naylor (2018b)

Wilson & Naylor (2017)

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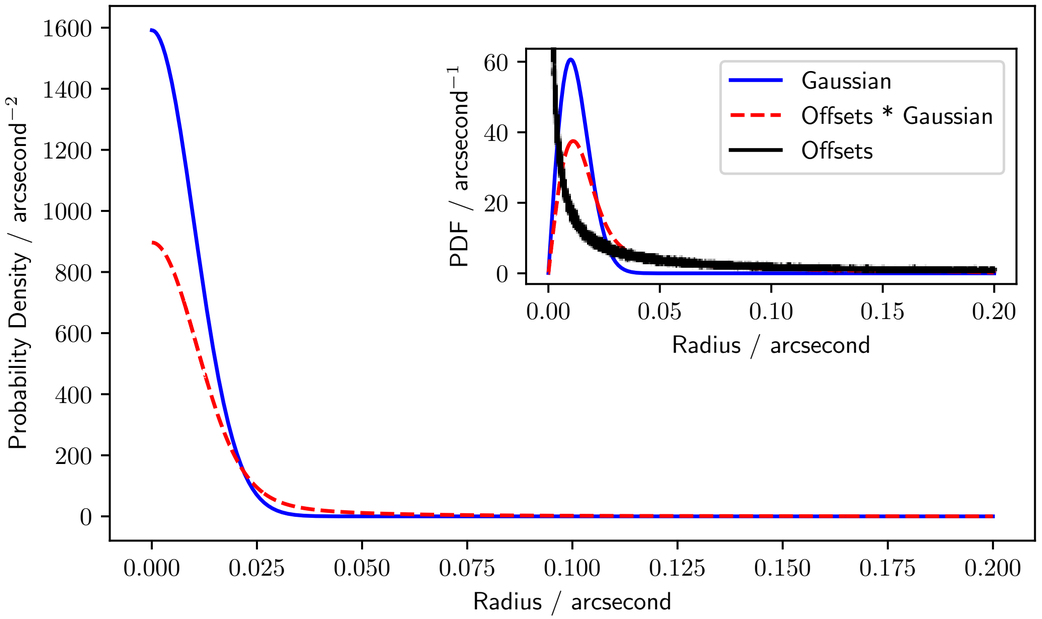
The Rubin AUF: Galactic Plane

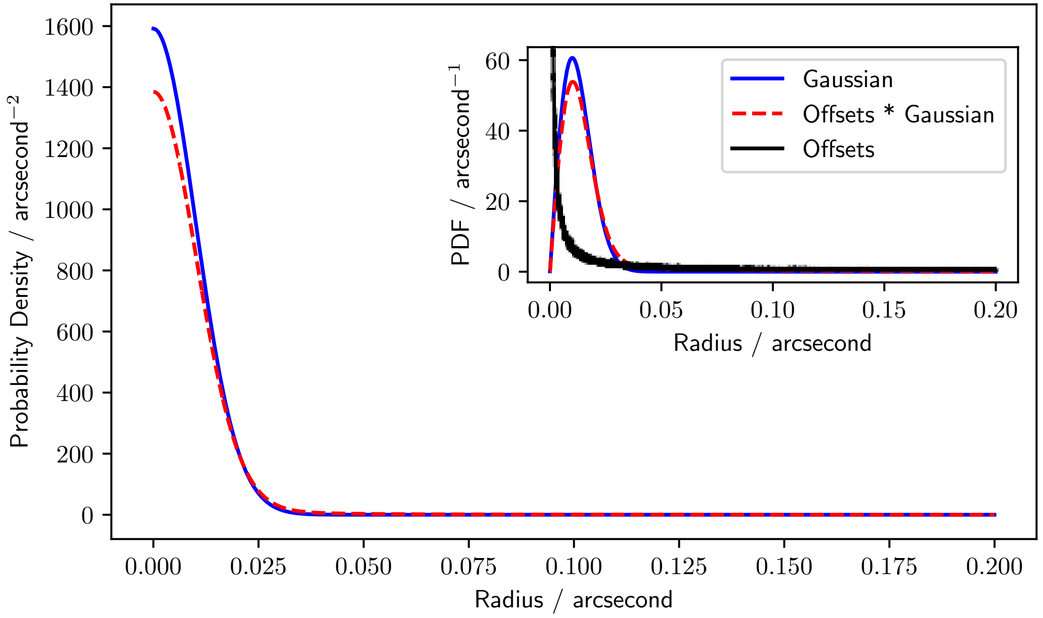
Galactic Centre

Not the Galactic Centre

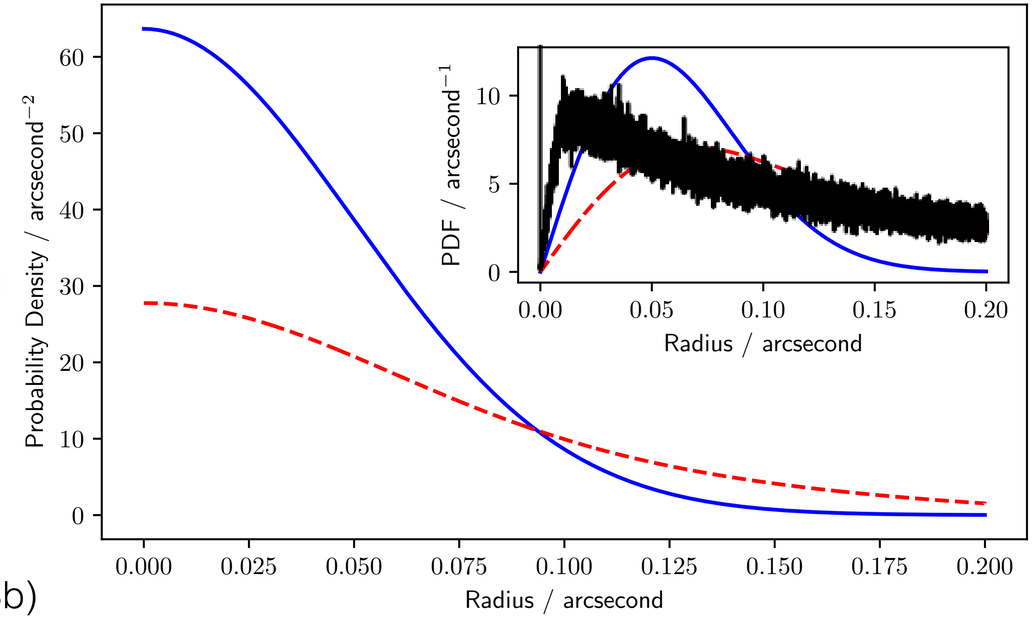
Single-visit

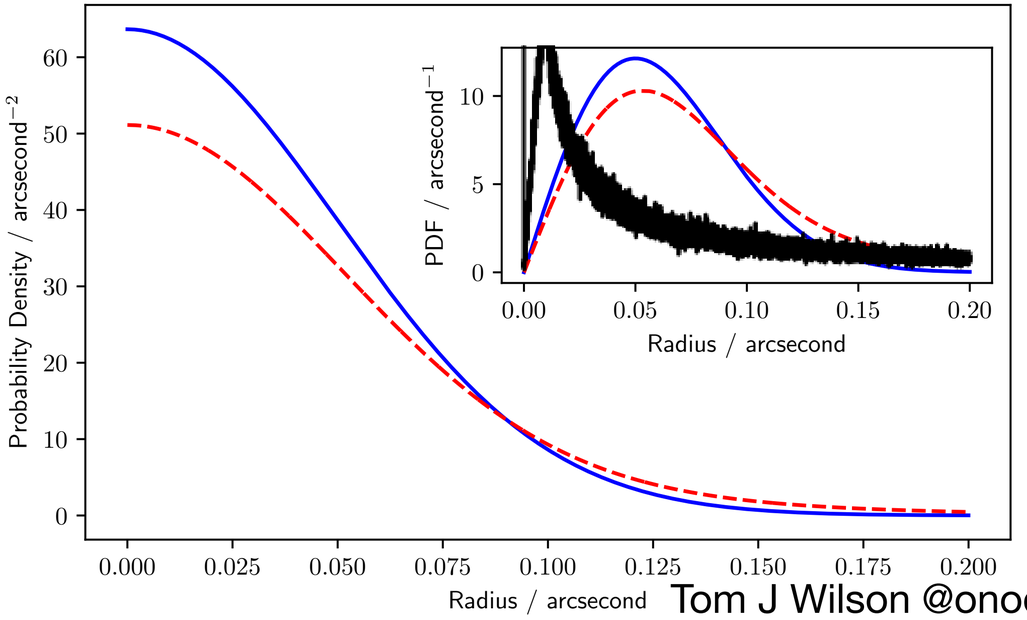
Without modelling this extra effect, we fail to recover many true pairings, with an artificially high false negative rate!





Co-add





Wilson & Naylor (2018b)

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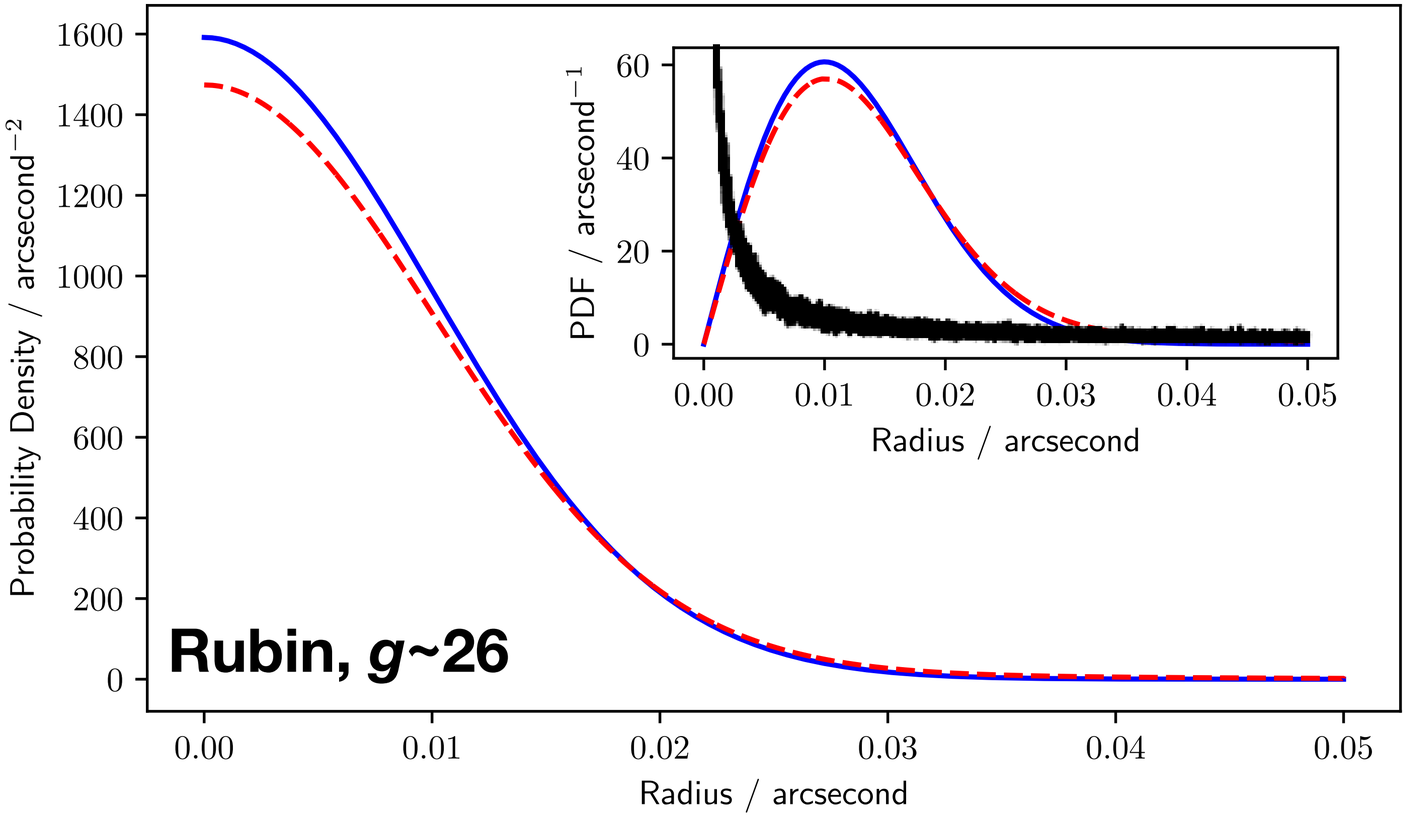
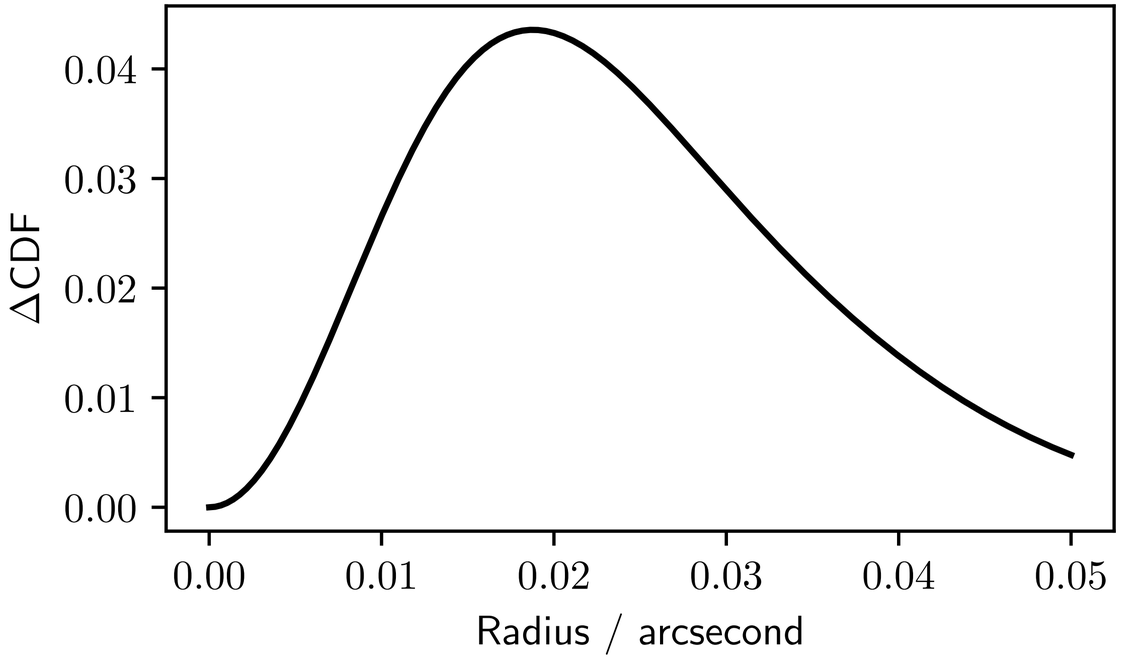
The Rubin AUF: Extra-Galactic





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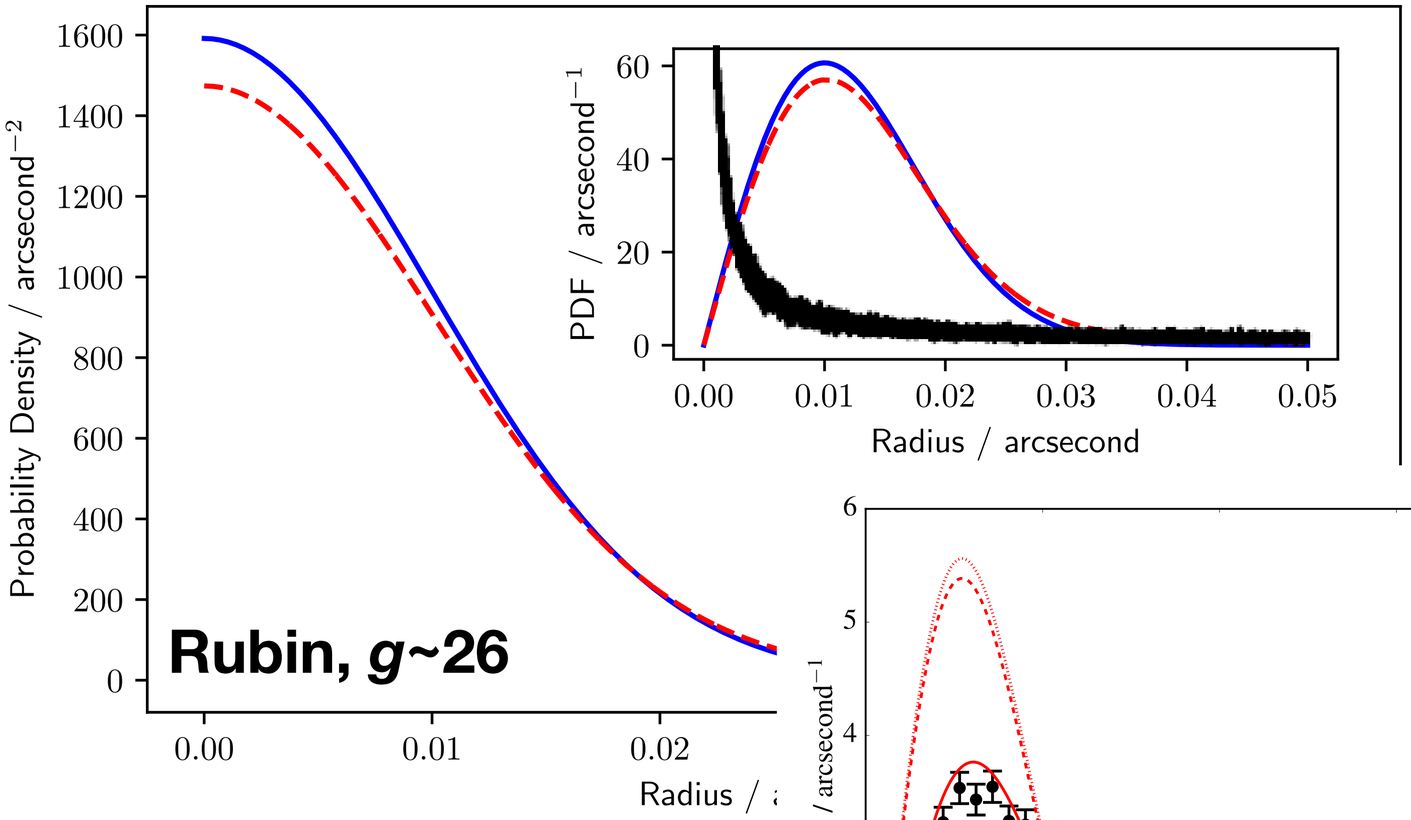
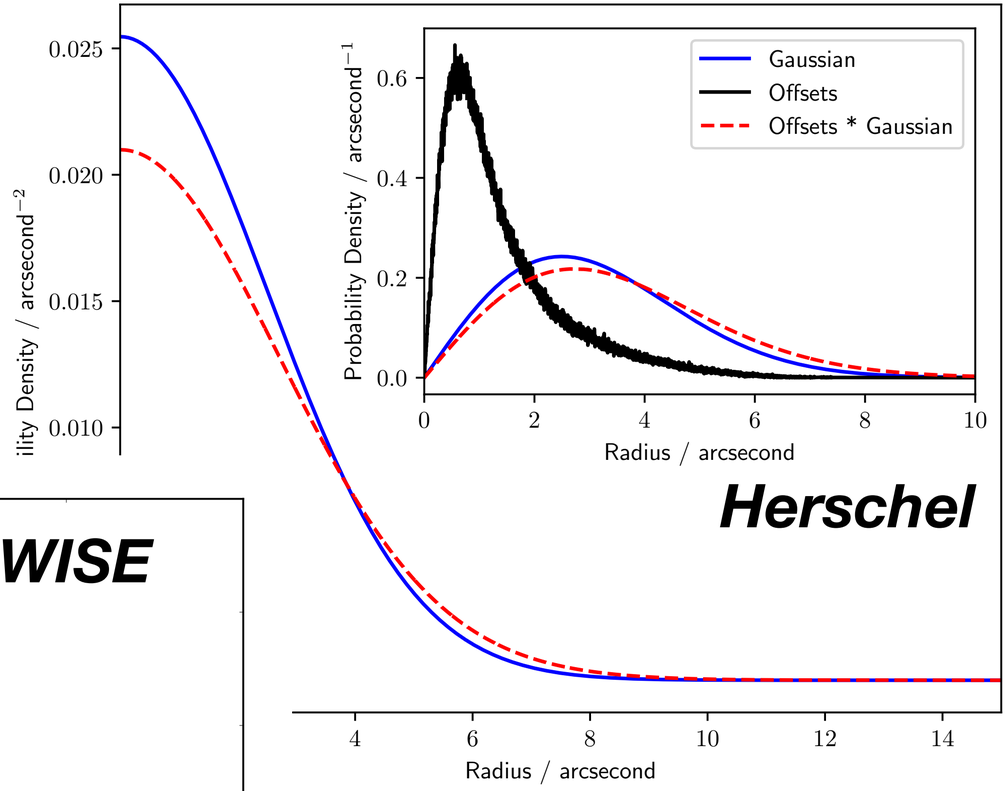
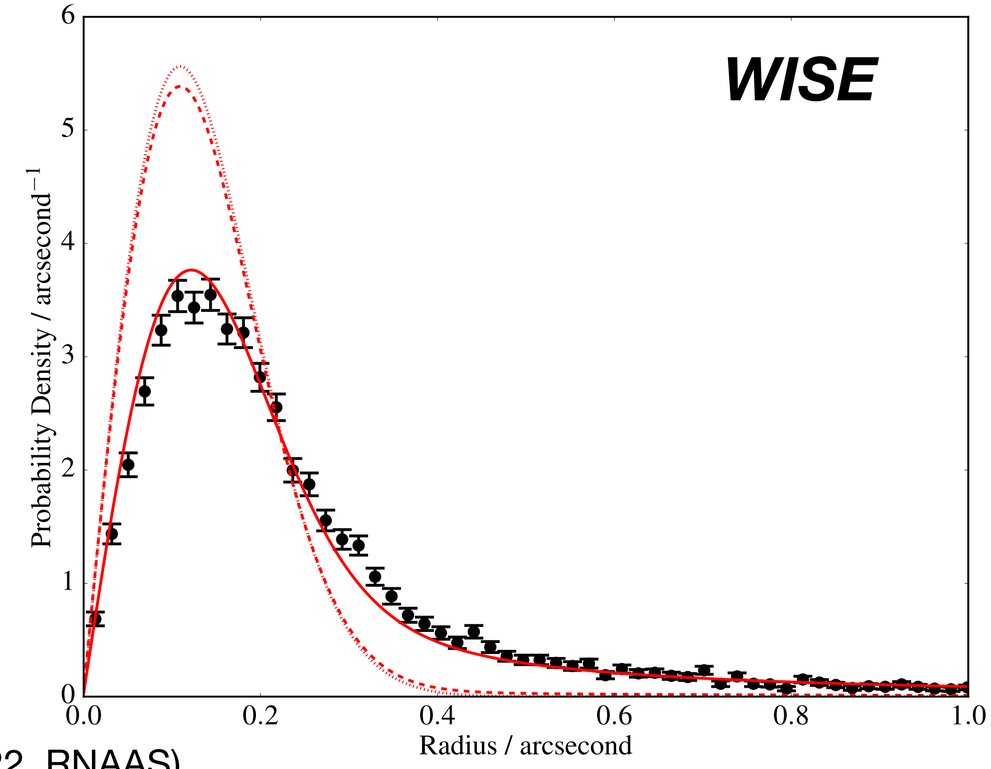
Wilson & Naylor (2018b); also see Wilson (2022, RNAAS)

The Rubin AUF: Extra-Galactic







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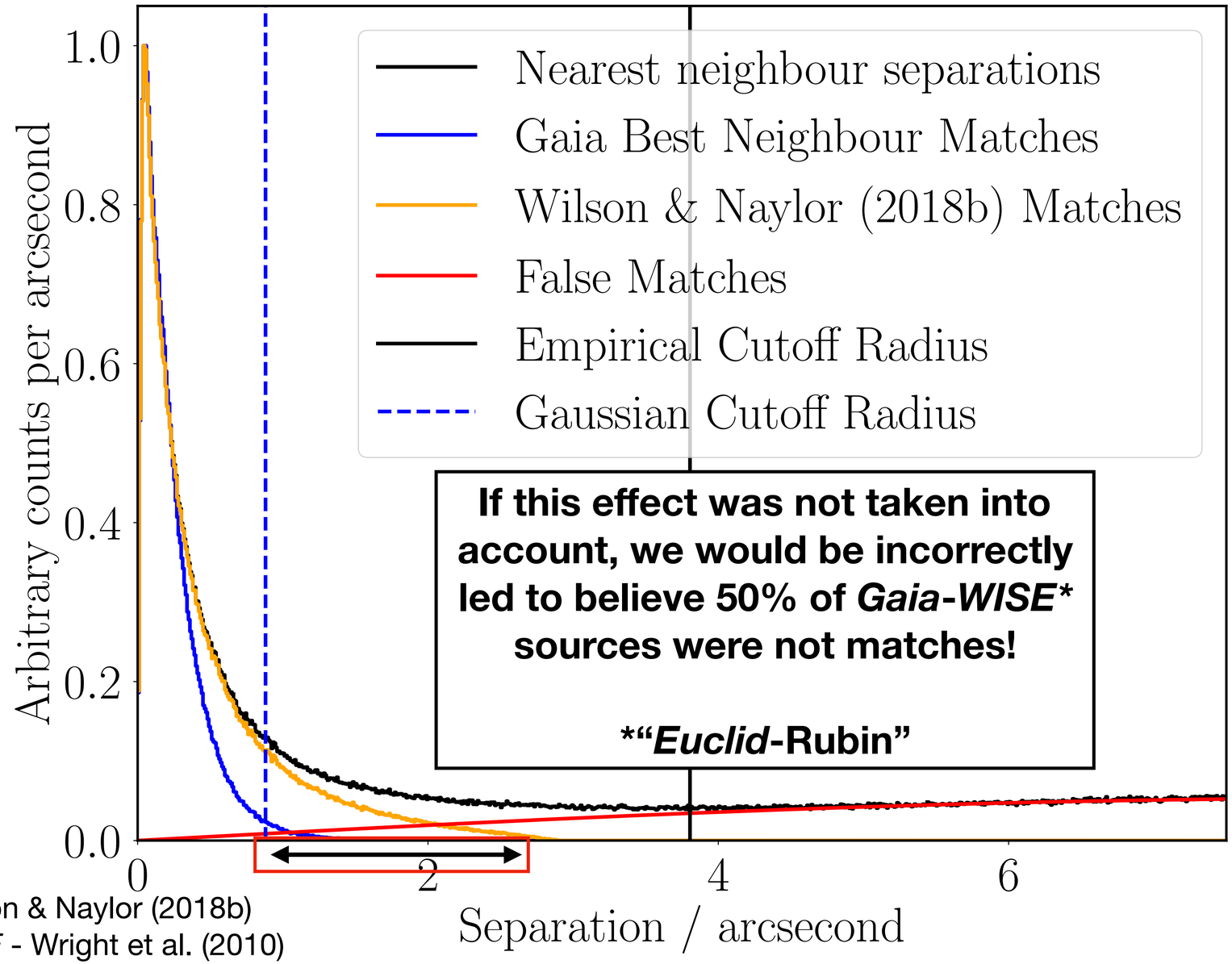
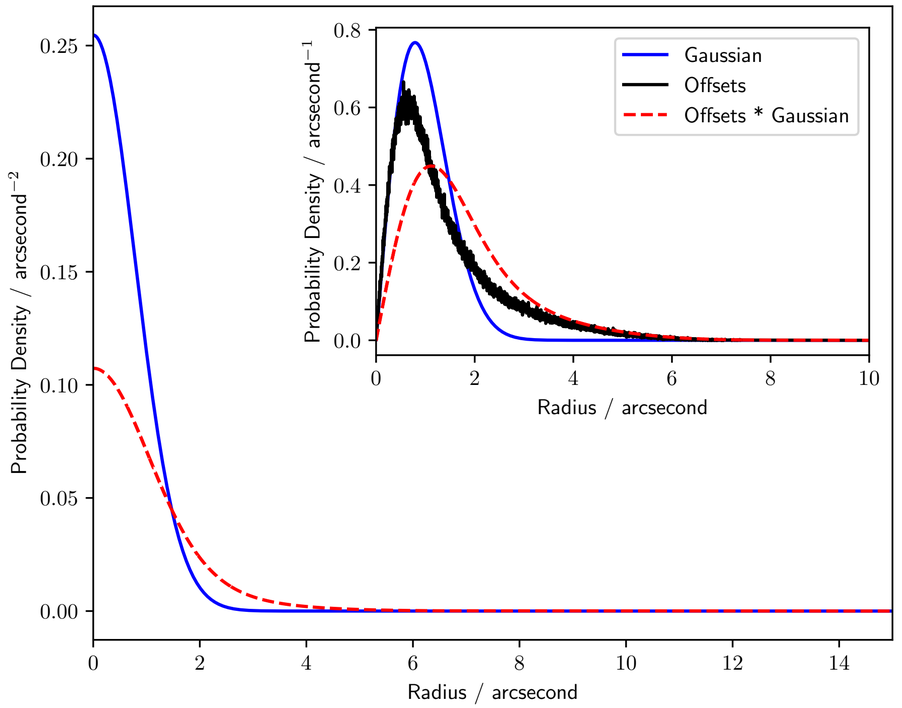
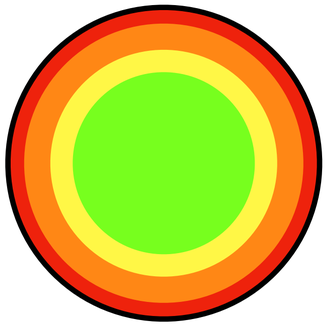
Match Separations



If this effect was not taken into account, we would be incorrectly led to believe 50% of *Gaia-WISE sources were not matches!**

***"*Euclid*-Rubin"**





The AUF does not need to, and in fact quite often <u>should *not*</u>, be Gaussian!

Wilson & Naylor (2018b)
WISE - Wright et al. (2010)
Gaia matches - Marrese et al. (2019)
Gaia DR2 - Gaia Collaboration, Brown A. G. A., et al. (2018)

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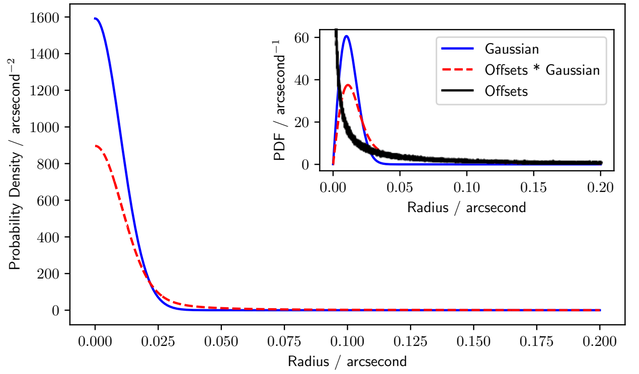
Conclusions

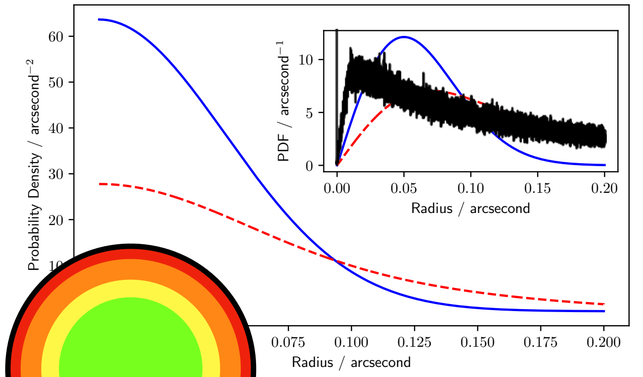
- **Our cross-match algorithms include two key elements to avoid issues with crowded & confused data**
  - **A generalised approach to the Astrometric Uncertainty Function allows for the full inclusion of the effects of perturbation due to blended sources — reduce false -ves!**
  - **Use of (two-sided) photometry to sort out multiple competing matches— reduce false +ves!**

- **Software package macauff developed to cross-match catalogues, including the effect of unresolved contaminant sources (and rejection of interloper objects using photometry in the static sky)**
  - **Developed through an IKC to Rubin/LSST:UK, matches planned to *Gaia*, *WISE*, VISTA, SDSS, …**
  - **We have compute time to cross-match datasets — let me know your favourite combo, and what you need matched (to LSST or otherwise)!**

- **Incorporating this extension of position uncertainty into real-time matches allows for more robust counterpart identification in the alert stream and a more accurate and precise transient SED**

- **Furthermore, we can provide *statistical* information on the level of photometric contamination unresolved contaminant sources cause, which can be subtracted in a probabilistic framework!**





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Wilson & Naylor, 2017, MNRAS, 468, 2517
Wilson & Naylor, 2018a, MNRAS, 473, 5570
Wilson & Naylor, 2018b, MNRAS, 481, 2148
Wilson, 2022, RNAAS, 6, 60
Wilson, 2023, RASTI, 2, 1

https://github.com/macauff/macauff

Macauff

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